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# Revised Edition.

# ELEMENTARY ARITHMETIC

#### FOR

# CANADIAN SCHOOLS,

#### BY

REV. BARNARD SMITH, M.A., St. Peter's College, Cambridge,

#### AND

# ARCHIBALD MCMURCHY, M.A.,

UNIVERSITY COLLEGE, TORONTO.

Juthorized by the Council of Public Instruction for Ontario.

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athom 1 cable

In this ELEMENTARY ARITHMETIC the same method of treating the subject that was adopted in MR. BARNARD SMITH'S Arithmetic for Schools has been retained; and especial care has been taken to adapt the book, in every respect, to the wants of the Junior Pupils in the Schools of the Dominion.



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# ARITHMETIC.

# SECTION L

1. ARITHMETIC teaches us the use of NUMBERS.

2. A UNIT OF ONE is any single object or thing, as an orange, a tree.

3. A WHOLE NUMBER, OF AN INTEGER, is a UNIT OF ONE, or a collection of UNITS OF ONES: if a boy, for instance, have one orange, and then another orange is given to him, he will have two oranges; if another be given to him he will have three oranges; if another, he will have four oranges, and so on. One, two, three, four, &c., are called WHOLE NUMBERS OF INTEGERS.

4. NOTATION is the art of writing any number in figures or letters.

There are two methods of Notation: 1st, The ARABIC; 2nd, The ROMAN.

5. The ARABIC NOTATION is the method of expressing numbers by means of the following *figures*, called sometimes *digits*.

1, 2, 3, 4, 5, 6, 7, 8, 9, called one, two, three, four, five, six, seven, eight, nine, representing (if we express a unit by a dot; thus.),

or one unit,	or two units,	or three units,	or four units,	or five units,	or six units,
				********	
	or seven	or eig	ht	or nine	
	units.	units	i.	units.	

and 0, called *nought*, because when standing by itself, it has no value, and represents nothing. 0 is sometimes called zero or *cypher*.

Note. Any one of the figures 1, 2, 3, 4, 5, 6, 7, 8, 9, when standing alone, or as the last figure on the right hand of any number, expresses so many *single* objects or things, or ones, ..... or *nine* units are the greatest number of units which can be expressed by one figure.

If another unit be placed to the right hand of the nine units, we have ..... or *ten* units, written in figures thus, 10; the 1 in 10 standing in the second place from the right hand, now expresses not *one* unit, but *one ten* units.

Hence we see that although 0, when standing by itself, has no value, still when placed to the right hand of any figure, it *alters* the value of that figure.

The number next after ten represents .......... or eleven units, written in figures thus, 11, where the 1 in the second place from the right hand expresses ten units, and the 1 in the right-hand place of the number one unit. Thus 11 units equal 1 ten units and 1 unit more.

Next we come to 12 (twelve) or one ten units and 2 more units, 13 (thirteen), 14 (fourteen), 15 (fifteen), 16 (sixteen), 17 (seventeen), 18 (eighteen), 19 (nineteen), which represent 1 ten units, and 3, 4, 5, 6, 7, 8, 9, more units respectively.

Next we come to 20 (twenty), 21 (twenty-one), 22 (twentytwo), 23 (twenty-three), 24 (twenty-four), 25 (twenty-five), 26 (twenty-six), 27 (twenty-seven), 28 (twenty-eight), 29 (twentynine); the 2, when followed by 0 or any single figure, representing two tens or twenty units, the figures in the right-hand place of each number expressing so many single units.

Next we come to 30 (thirty), 31 (thirty-one), &c., 3 expressing three tens, or thirty, and so on up to 40 (forty), 4 expressing four tens or forty, to 50 (fifty), to 60 (sizty), to 70 (seventy), to 80 (eighty), to 90 (ninety), 5, 6, 7, 8, 9, expressing five, six, seven, eight, nine tens respectively; the numbers between any two of them as 40 and 50, being formed in the same way as those between 20 and 30.

We thus come at length to 99 ninety-nine) or nine tens and nine, the greatest number which can be expressed by two figures.

### Ex. I.

Write the following numbers in figures.

(1) Three, four, two, seven, nine, six, eight.

(2) Ten, one, twelve, nineteen, five, eleven, sixteen.

(3) Fourteen, twenty, twenty-seven, thirty-three, fortynine, sixty, fifty-five, seventeen, thirty-six.

. (4) Eighty-eight, thirty-five, sixty-three, twenty-nine, seventy six, eighty, ninety-four, thirteen, fifty-two.

(5) Write down in figures all the numbers between eight and eighteen, between forty-five and fifty-one, and between eighty-seven and ninety-nine.

The next number after 99 is one hundred, written in figures thus, 100; the l in 100, standing in the third place from the right hand, now expressing not one unit, nor one ten units, but one hundred units.

All numbers from 100 to 200 (two hundred) are formed exactly in the same way, as we formed those from 0 to 100; thus we go on 101 (one hundred and one), 102, &c., up to 110 (one hundred and ten), then 111 (one hundred and eleven), 112, &c., up to 120 (one hundred and twenty), then 121, (one hundred and twenty-one), 122, &c., up to 130 (one hundred and thirty), and so on, up to 200; then 201, 202, &c., up to 300 (three hundred), and so on up to 400 (four hundred), 500 (five hundred), 600 (six hundred), 700 (seven hundred), 800 (eight hundred), 900 (nine hundred), 999 (nine hundred and ninetynine), or nine hundreds, nine tens, and nine, the greatest number which can be expressed by three figures.

## Ex. II.

Write down the following numbers in figures.

(1) One hundred and six, one hundred and fifty, two hundred, two hundred and eighty-seven, three hundred and ten, four hundred and thirty-one, five hundred and fifty-five, nine hundred and nineteen, eight hundred and sixty-seven.

(2) Write all the numbers in figures from one hundred and ninety-five to two hundred and fourteen, from six hundred and eleven, to six hundred and twenty, and from nine hundred and forty-seven to nine hundred and seventy.

The next number after 999 is one thousand, written in figures thus, 1000; the 1 in 1000, standing in the fourth place from the right hand, now expressing one thousand units.

All numbers from 1000 up to 9999 (nine thousand nine hunddred and ninety-nine), are formed thus, 1001 (one thousand and one), 1002, &c-, up to 2000 (two thousand), up to 3000 (three thousand), and so on.

The next number after 9999 is ten thousand, written in figures, thus, 10000; the 1 in 10000 standing in the fifth place

# ARITHMETIC.

place from the right hand, now expressing one ten thousand units.

All numbers from 10000 up to 99999 (ninety-nine thousand nine hundred and ninety-nine), are formed thus, 10001 (ten thousand and one), 10002, &c., up to 20000 (twenty thousand), then 20001 (twenty thousand and one), 20002, &c., up to 30000 (thirty thousand), and so on.

#### Ex. III.

Write the following numbers in figures.

(1) Four thousand five hundred and eighty-five, seven thousand three hundred and twenty-one, nine thousand seven hundred and ninety-eight, seven thousand and six.

(2) Five thousand and four, five thousand four hundred, five thousand and forty, eight thousand and thirth-six, eight thousand three hundred and six, eight thousand three hundred and sixty, nine thousand nine hundred and nine.

(3) Seventy-five thousand six hundred and thirty-five, ninety thousand nine hundred and nine, ten thousand and four, eighty-seven thousand and fifty, ninety thousand and one, sixty-four thousand and sixty-four, eighty-three thousand.

The next number after 99999 is one hundred thousand, written in figures thus, 100000, the 1 in 100000 standing in the sixth place from the right hand, now expressing one hundred thousand units, and so on up to 999999 (nine hundred and ninety-nine thousand nine hundred and ninety-nine), then we come to one million, written in figures thus, 1000000, the 1 expressing one million units, and so on up to tens of millions, (10000000), hundreds of millions (100000000), billions (100000000), and so on.

Thus	one is written	1
	ten	10
	one hundred	100
	one thousand	1,000
	ten thousand	10,000
	one hundred thousand	100,000
	one million	1.000.000
	ten million	10,000,000
	one hundred million	100.000.000
	one billion.	.000.000.000
6.	From the above table, we see that dividir	ng any num-

12

# NOTATION.

ber into periods of three figures each, beginning at the right hand, the names of those periods will be,

First	period	Units.
Second	- ec	Thousands.
Third	66	Millions.
Fourth	66	Billions.
Fifth	66	Trillions.
80	the	

Also, that the names of the places in each of those periods are the same, namely:

First	place,	Units.
Second		Tens.
Third	66	Hundreds.

7. The following plan is recommended to enable the scholar to write in figures any number dictated by the teacher.

Let the scholar write on his slate a number of noughts, or zeros; thus 000,000,000,000, marking them off into periods of three places each from the right:

Put U over the first period for Units.

T					sec	ond			Thousands.
М					thi	rd			Millions.
B					fou	$\mathbf{rth}$			 Billions.
					Ð	M	m	TT	

And so on. Thus 000,000,000,000. Then when a number is dictated to the pupil, all he has to do is to put each figure under its proper place and fill up vacancies, if any, with 0's.

Thus, two thousand and five will be writ-

ten thus in figures	2,005
Eighty-six thousand four hundred and three	86,403
Four hundred and thirty thousand three	
hundred and forty	430,340
Eight hundred and three millions one	
thousand and eleven	803,001,011
Five billions thirty-seven millions and six	5,037,000,006

# Ex. IV.

Write the following numbers in figures.

(1) One hundred and five, eight thousand seven hundred and ninety, thirty-seven thousand and seventy-one, thirty thousand four hundred and two, seventy-seven thousand seven hundred, twenty-four thousand eight hundred and seventeen.

(2) One hundred and five thousand four hundred and

# ARITHMETIC.

nine, eight millions eight thousand and thirteen, seven millions six hundred and fifty thousand and ninety, sixty-four millions four hundred, eighty-nine millions forty-four thousand and one, five hundred and four millions six hundred and twenty-three thousand and twenty-four, nine hundred millions three hundred thousand eight hundred, fifty-three millions five hundred and three.

(3) Six billions six millions seventy thousand and seven. eighty-three billions four hundred and one millions one thousand and ten, seven billions and four millions eighty-nine thousand two hundred, nine hundred and ninety millions.

8. NUMERATION is the art of writing in words the meaning of any number, which is already given in figures.

This follows from what has been already said: thus

27 means two tens and seven units, or twenty-seven.

503 means five hundreds, no tens, and three units, or five hundred and three.

0610 means no thousands, six hundreds, one ten, and no units, or six hundred and ten.

5634 means five thousands, six hundreds, three tens, and four units, or five thousand six hundred and thirty-four.

6,070,084 means six millions, seven tens of thousands, eight tens and four units, or six millions seventy thousand and eighty-four.

803,968,005 means eight hundreds of millions, three millions, nine hundreds of thousands, six tens of thousands, eight thousands, and five units, or eight hundred and three millions nine hundred and sixty-eight thousand and five.

# Ex. V.

#### Write in words the meaning of

7, 13, 4, 9, 18, 5, 20, 11, 05, 50, 34, 29, 3, 17, 53.

- 19, 8, 041, 88. 27, 72, 94, 49, 16, 61, 98, 80, 56, 28. (2)
- (3)
- 107, 170, 017, 430, 691, 080, 800, 008, 956, 803, 684. 4506, 5870, 5087, 6900, 6009, 02580, 7045, 7591, 6275. 24714, 12500, 10025, 10205, 70457, 74007, 77000. (4)
- (5)
- 300863, 30080630, 96400250, 800400307, 572060495. (6)
- (7) 120192703. 890647560. 1050060429. 100000000001.

### SIMPLE ADDITION.

9. SIMPLE ADDITION is the method of finding a number. hich is equal to two or more numbers of the same kind ken together

By the same kind we mean all apples, or all horses, or all nce, and so on.

The numbers to be added are called ADDENDS.

The SUM, or AMOUNT, is the number so found.

Before learning the Rule for Simple Addition, it will be all for a child to learn the following Table, called the ODITION TABLE. The child should satisfy himself that this whe is true by means of counters, or strokes on a slate.

Qand	2 and	Aand	5 and
2 and	3 and	4 and	Danu
1 make 3	I make 4	1 make 5	I make 6
2 4	2 5	2 6	2 .: 7
3 5	3 6	3 7	3 8
4 6	4 7	4 8	4 9
E	E 0	<b>E</b> 0	5 10
0 /	ə ə	0 9	.0 10
6 8	6 9	6 10	6 11
7 9	7 10	5 11	7 12
8 10	8 11	8 12	8 13
9 11	9 12	9 13	9 14
10 10	10 12	10 14	10 15
10 12	10 15	10 14	10 15
Gand	7 and	l Q and	0 and
6 and	7 and	8 and	9 and
6 and 1 make 7	7 and 1 make 8	8 and 1 make 9	9 and 1 make 10
6 and 1 make 7 2 8	7 and 1 make 8 2 9	8 and 1 make 9 2 10	9 and 1 make 10 2 11
6 and 1 make 7 2 8 3 9	7 and 1 make 8 2 9 3 10	8 and 1 make 9 2 10 3 11	9 and 1 make 10 2 11 3 12
6 and 1 make 7 2 8 3 9 4 10	7 and 1 make 8 2 9 3 10 4 11	8 and 1 make 9 2 10 3 11 412	9 and 1 make 10 2 11 3 12 4 13
6 and 1 make 7 2 8 3 9 4 10 5 11	7 and 1 make 8 2 9 3 10 4 11 5 12	8 and 1 make 9 2 10 3 11 4 12 5 12	9 and 1 make 10 2 11 3 12 4 13 5 14
6 and 1 make 7 2 8 3 9 4 10 5 11	7 and 1 make 8 2 9 3 10 4 11 5 12	8 and 1 make 9 2 10 3 11 4 12 5 13	9 and 1 make 10 2 11 3 12 4 13 5 14
$\begin{array}{c} 6 \text{ and} \\ 1 \text{ make 7} \\ 2 \\ . \\ 8 \\ 3 \\ . \\ 9 \\ 4 \\ . \\ 10 \\ 5 \\ . \\ 11 \\ 6 \\ . \\ 12 \end{array}$	$\begin{array}{c} 7 \text{ and} \\ 1 \text{ make 8} \\ 2 \dots 9 \\ 3 \dots 10 \\ 4 \dots 11 \\ 5 \dots 12 \\ 6 \dots 13 \end{array}$	8 and 1 make 9 2 10 3 11 4 12 5 13 6 14	9 and 1 make 10 2 11 3 12 4 13 5 14 6 15
$\begin{array}{c} 6 \text{ and} \\ 1 \text{ make 7} \\ 2 \ \ 8 \\ 3 \ \ 9 \\ 4 \ \ 10 \\ 5 \ \ 11 \\ 6 \ \ 12 \\ 7 \ \ 13 \end{array}$	7 and 1 make 8 2 9 3 10 4 11 5 12 6 13 7 14	8 and 1 make 9 2 10 3 11 4 12 5 13 6 14 7 15	9 and 1 make 10 2 11 3 12 4 13 5 14 6 15 7 16
6 and 1 make 7 2 8 3 9 4 10 5 11 6 12 7 13 8 14	7 and 1 make 8 2 9 3 10 4 11 5 12 6 13 7 14 8 15	8 and 1 make 9 2 10 3 11 4 12 5 13 6 14 7 15 8 16	9 and 1 make 10 2 11 3 12 4 13 5 14 6 15 7 16 8 17
6 and 1 make 7 2 8 3 9 4 10 5 11 6 12 7 13 8 14 9 15	7 and 1 make 8 2 9 3 10 4 11 5 12 6 13 7 14 8 15 9 16	8 and 1 make 9 2 10 3 11 4 12 5 13 6 14 7 15 8 16 9 17	$\begin{array}{c} 9 \text{ and} \\ 1 \text{ make 10} \\ 2 \dots 11 \\ 3 \dots 12 \\ 4 \dots 13 \\ 5 \dots 14 \\ 6 \dots 15 \\ 7 \dots 16 \\ 8 \dots 17 \\ 9 \dots 18 \end{array}$
6 and 1 make 7 2 8 3 9 4 10 5 11 6 12 7 13 8 14 9 15 10 16	7 and 1 make 8 2 9 3 10 4 11 5 12 6 13 7 14 8 15 9 16 10 17	8 and 1 make 9 2 10 3 11 4 12 5 13 6 14 7 15 8 16 9 17 10 18	9 and 1 make 10 2 11 3 12 4 13 5 14 6 15 7 16 8 17 9 18 10 19

This Table can easily be carried on for numbers larger han 10; for instance since 2 and 1 make 3, 2 and 11 make 0 more than 2 and 1, *i. e.* make 13. Again since 9 and 4 take 13, 9 and 14 will make 23, and so on, the result in each ase being 10 more than in the corresponding case in the lable. Also 2 and 51 make 53, 9 and 54 makes 63, and so n, the result in each case being 50 more than the corresonding result in the Table.

10. The	sign +, called	PLUS, place	ed betwe	en two num-
2 apples +	3 apples, mean	s that 2 ap	ples and	3 apples are
to be adde	d together, there	fore 2 apple	es + 3 a	pples make 5
apples. Ag	gain 2 + 3 + 4 r	neans that 2	and 3 a	nd 4 are to be
added toge	ther; $2 + 3 \max$	e 5, therefor	e 2 + 3	+ 4 make 5 +
4, which m	ake 9.	r mlassed h	aturaan	two numbers
means that	the numbers are	L, placed b	e anothe	two numbers,
The sign	means THERE	FORE.	io anotic	~~ .
Ex. 1.	Find the sum of,	or add toget	ther 5	if so, we say
5, 4, and 7.		1 0 0	4	7 and 4 make
We add	thus, 5 and 4 n	nake 9, 9 an	1d 7 7	II, II and 5
make 16;		or t	thus 16	make 16.
. the su	m of 5, 4, and 7,	or $5 + 4 +$	7 = 16	•
Ex. 2.	Add together 4, 8	8, 3, 0, 9.	4	1.0
4 and 8 r	nake 12, 12 and	3  make  15,	8 9 al	nd 3 make 12,
15 and 0 m	8 + 3 + 0 + 9	= 24:	9 20 8	and 4 make 24.
	0101010	,	0	
		or thus	24	
		0.0.0.0		10 1 15
Ex. 3.	Find the sum of	9, 3, 7, 6,	9 8 ai	nd 9 make 17,
0, 9, and 3 m	ake 19 19 and 7	make 10	5 1/a 7 99 a	nd 5 make 22,
19 and 6 m	ake 25, 25 and 5	make 30.	6 28 a	nd 7 make 35.
30 and 9 m	ake 39, 39 and 8	make 47,	5 35 a	nd 3 make 38,
sum of s	9, 3, 7, 6, 5, 9, an	d 8 = 47;	9 38 a	nd 9 make 47.
			8	
		or thus	47	
	1	Ex. VI.		
Add (1)	2	(2) 3		(3) 5
	3	7		6
	8.	8		8.7
	0	J		

(4), Find the sum of two, seven and two; of five, seven, and four; of six, three, and nine; of five, five, aud eight; of nine, eight, nought, and six; of six, two, and nine; of four, eight and three; of seven, nine and two; of nine, five, three, and eight.

(5). Find the value of 3 + 4 + 8 + 3 + 2 + 5; 6 + 4 + 0 + 0 + 7 + 3; 5 + 8 + 1 + 6 + 5 + 9; 3 + 6 + 8 + 5 + 4 + 2; 9 + 5 + 7 + 8 + 3 + 4; 6 + 9 + 9 + 8 + 8 + 5; 5 + 8 + 3 + 9 + 9 + 6 + 6.

(6). In a boys' school there are four classes. In the first class there are *six* boys; in the second class *seven* boys; in the third class *one* more than in the first class; in the fourth class *two* more than in the second class. How many boys are there in the school?

(7). John's age is 2 years, Ellen is two years older than John, Walter's age is the sum of the ages of the other two. Find the sum of all their ages.

(8). A woman sold two chickens to A, to B three more than to A, to C as many as to A and B, to D four more than to B; had C bought as many more chickens as he did buy, the woman would have sold all her chickens; how many chickens had she to sell?

# Rule for Simple Addition.

11. RULE. Write down the given numbers under each other, so that units may come under units, tens under tens, hundreds under hundreds, and so on: then draw a line under the lowest number.

Find the sum of the column of units: if it be less than ten, write it down under the column of units below the line just drawn, but if it be greater than ten, then write down the units' figure (*i.e.* the last figure on the right hand) of the sum under the column of units, and carry to the column of tens the remaining figure or figures.

Add the column of tens and the figure or figures you carry as you have added the column of units, and treat its sum in exactly the same way as you have treated the column of units.

Treat each succeeding column (viz. hundreds, thousands, &c.) in the same way.

Write down the full sum of the last column on the left hand.

The entire sum thus obtained will be the sum or amount of the given numbers.

Ex. 1. Add together 35, 56, and 282. By the Rule.  $35 \\ 56 \\ 282$ 

Method of adding. 2 and 6 are 8, 8 and 5 are 13, *i.e.* 1 ten and 3 units; write down 3 under the column of units, and carry 1 ten.

sum = 373

Then 1 and 8 are 9, 9 and 5 are 14, 14 and 3 are 17, *i.e.* 17 tens, or 10 tens (1 hundred),

and 7 tens, write down 7 under the column of tens and carry one hundred.

Then 1 and 2 are 3, *i.e.* 3 hundreds, write down 3 in the hundreds' place.

E. 2. Find the sum of three thousand eight hundred and sixty-seven, seven hundred and nine, fifty-six thousand and thirty, eight thousand eight hundred and ninety-six, and fifteen thousand and twenty-nine, and write down the meaning of the sum in words.

By the Rule,

 $\frac{15029}{84531}$ 

9 and 6 are 15, 15 and 9 are 24, 24 and 7 are 31, or 3 tens and 1 unit: write down 1 under the units, and carry 3 tens.

Then 3 and 2 are 5, 5 and 9 are 14, 14 and 3 are 17, 17 and 6 are 23, *i.e.* 23 tens, or 2 hundreds and 3 tens; write down 3 tens, and carry 2 hundreds.

eighty-four Then 2 and 8 are 10, 10 and 7 are 17, 17 thousand five and 8 are 25, *i.e.* 25 hundreds, or 2 thoushundred and and 5 and 5 hundreds; write down 5 hundthirty-one. reds, and carry 2 thousands.

Then 2 and 5 are 7, 7 and 8 are 15, 15 and 6 are 21, 21 and 3 are 24, *i.e.* 24 thousands, or 2 tens of thousands and 4 thousands; write down 4 thousands, and carry 2 tens of thousands.

Then 2 and 1 are 3, 3 and 5 are 8, *i.e.* 8 tens of thousands; write down 8 tens of thousands.

Note 1. Though the method of adding, as in the above examples, is the one a teacher can follow at first with his pupils; the following method should be insisted on as soon as possible.

Suppose we have to add:

276	Add thus: 7, 16, 22; put down 2 under the
389	units and 2 to be added to the tens; then 2, 8,
467	16, 23, &c., &c.: thus saving much time; in-
1132	stead of saying 7 and 9 make 16, 16 and 7 make 23, &c.

Note 2. The truth of all sums in Addition may be proved

# SIMPLE ADDITION.

by adding the columns first upwards, and afterwards downwards; if the result be the same in both cases, the numbers will probably have been added correctly.

			E	x. VII.				
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	
Add	11	22	33	10	27	33	24	
	12	13	• 45	8	15	16	25	
	14	<u>34</u>				10		
	(8)	(9)	(10)	(11)	(12)	(13)	(14)	
	12	79	87	98	43	68	78	
	56	27	68	55	69	48	66	
	42	94	59	60	74	<b>9</b> 8	97	
(15)	(16	)	(17)	(18)	(19)	(20)	(21)	
310	342	2	704	87	889	500	682	
• 40	- 974	5	400	586	500	110	902	
14/	010	-	515				210	
(22)	(23	)	(24)	(25)	(26)	(27)	(28)	
378	79	ź	828	654	729	888	674	
423	46	5	939	546	909	517	789	
748	28	9	747	465	813	743	555	
	_	-						-
(29)	(30)	(	<b>31)</b> . j	(32)	(33)	(34	4) (	35)
2865	785	6	769	9479	6045	58	53 9	80€
108	0700	8	967	9921	4500	90		932
2402	9540	0 7	680	0408	0647	-88		1980
0.100	0000	-			3047	00		009

(36) One boy had nineteen marbles, another had seventeen more than the first, and another had nine more than the second, how many marbles had they among them?

(37) In a school section there are two and thirty men, sixty-five more women than men; the number of young men, young women and school children all together equals the number of men and women together, and there are twenty-nine infants; what is the population of the school section?

(38) 5 apple trees produced as follows: the lst, six hundred and fifty-seven; the 2nd, two hundred and thirty-one

# ARITHMETIC.

more than the 1st; the 3rd, eight hundred and ninety-two; the 4th, eleven more than all the first three; the 5th, as many as all the others. How many apples were there on all the trees?

(39) A gentleman left his property by will, thus: to his wife, nine thousand and eighty dollars; to each of his two younger sons, five thousand eight hundred and ninety-four dollars; the rest of his property in two equal shares between his three daughters and eldest son; the eldest son's share was fifteen hundred and twenty dollars more than the mother's share; what did the gentleman die worth?

(40) A grocer bought 4 chests of oranges. In the 1st chest there were five hundred and eighty-nine oranges; in the 2nd, two hundred and fifteen more than in the 1st; in the 3rd; one hundred and ninety-seven more than in the 1st; in the 4th, as many as there were in the 1st and 3rd. How many oranges did he buy?

				Ex.	VIII					
Add	(1)	22 + 30	+29+	67		(6)	219 + 31	5+6	12+70	)5
	(2)	63 + 93	+87+	73		(7)	602 + 52	8+3	846+64	18
	(3)	72 + 90	+37+	57 + 3	9	(8)	736+93	2+7	12+8	36
	(4)	38 + 47	+96+	83+2	7	(9)	968+86	4+3	45+98	39
	(5)	78+89	+68+	58 + 4	7	(10)	940+76	0+7	12+5	52
	(11)		(12)		(13)		(14)		(15)	
	7140	7	82079		96748		33456		15161	
	9078	1	88099		25003		84771		8098	
	6894	3	67005		84067		66854		958	
	3260	0	74387		95674		72984		49790	
	7277	7	12345		98765		99999		78368	
	(1	-		171		(10)			(10)	
	046	CADE	=	1/)		(10)	140	-	(19)	
	940	0490 5470	011	0146		57691	J40	050	08400	
	104	0000	91	14000		20020	2017	903	20039	
	900	9099	004	7400		590398	150	0.40	0949	
	- 498	0007	769	22700		79524	210	049	00007	
	792	2929	260	24702		102034	59A	795	62410	
	100	0410	900	rt199	-	1304/1	104	100	00412	

(20) Add together nine hundred and twelve, two thousand and fifty-eight, three thousand four hundred and fortyfive, nineteen thousand three hundred and sixty, twentyseven thousand six hundred and forty-three, thirty-nine. thousand seven hundred and ninety, fifty-five thousand eight hundred and seventy-nine, sixty-four thousand nine hundred and seventy-seven, eight thousand two hundred and eleven.

(21) In the census of 1861, the population of the counties on Lake Huron, was as follows: Of Lambton, twenty-four thousand nine hundred and sixteen; of Huron, fifty-one thousand nine hundred and fifty-four; of Bruce, twentyseven thousand four hundred and ninety-nine; of Grey, thirty-seven thousand seven hundred and fifty; of Simcoe, forty-four thousand seven hundred and twenty. What was the whole population of the above five counties in 1861?

(22) In 1861 the population of the counties on the Ottawa river, was: of Prescott, fifteen thousand four hundred and ninety-nine; of Russell, six thousand eight hundred and twenty four; of Carlton, twenty-nine thousand six hundred and twenty; of Renfrew, twenty thousand three hundred and twenty-five. What was the total population of these four counties in 1861?

(23) In 1861 Toronto contained forty-four thousand eight hundred and twenty-one inhabitants; Montreal, ninety thousand three hundred and twenty-three; Hamilton, nineteen thousand and ninety-six; Ottawa, fourteen thousand six hundred and sixty-nine; Kingston, thirteen thousand seven hundred and forty-three; London, eleven thousand five hundred and fifty-five. Find the total population of these cities in 1861?

	Ex. IX.				
Find the sum of	(1)	$\binom{2}{2012}$	(3) 22793		
	212907	75005	27812		
	616848	700764 ,	38614		
	703003	93869	45693		
	1090090	4202073	92075		
(4)	(5)	•	(6)		
278653	2612856	376	13906		
972009	8906783	273	05638		
2673627	912227	2096	17382		
5009607	6804398	3726	372637867		
27693	27635398	9683	63352		
986735	33297653	273	06468		

(7)	(8)	(9)
276608567	306738672	397203685
76293568	68345658	28678326
683927285	928327368	206738638 .
938668589	9283678	728397328
211839297	238906594	563435639
26302562	93567836	912368834
397612397	207867398	6383563
583967323	30673612	83297609
960039368	928327563	603536239
543832586	568302126	736397564
782395678	202386517	932506593
(10)	(11)	(12)
72867853	368936709	378684976
97605812	76385673	79683886
7638516	467308753	468976395
316527308	900009900	786347512
275607836	90909999	927607038
97673904	938568378	90809008
268937318	712050750	758385006
718768926	77807689	703209600
203685738	234593368	87967339
96359568	99213567	862006764
397569387	837346395	993387535

(13) Add together nine millions four hundred and sixtysix thousand four hundred and ninety-five, three hundred and seventy-five millions five hundred and seventy-three thousand seven hundred and thirty-five, seven hundred and fifty-four thousand five hundred and forty-seven, three millions seven hundred and eighty nine thousand two hundred and eighty-four, twenty-nine millions eight hundred and eighty-six thousand seven hundred and ninety-nine, nine hundred and ninety-two thousand and eighty-four, two hundred and ninety-three thousand six hundred and ninety-five, two millions six hundred and eighty-four thousand four hundred and eighty-seven, three millions five hundred and uinety-two thousand eight hundred and seventy-three, seven millions eight hundred and forty-nine thousand three hundred and forty-six.

(14) A farmer had forty-four sheep, thirty-five head of cattle, fifteen pigs, six horses. How many animals had he altogether?

(15) In one year a farmer's crop was as follows: Five hundred and twenty-three bushels of wheat, a hundred and twenty bushels of oats, sixty-four bushels of peas, two hundred and thirty-seven bushels of potatoes, thirty-eight bushels of turnips. How many bushels had he?

(16) A man bought a farm for sixteen hundred and fifty dollars, he spent a hundred and sixty in putting on it new fences, five hundred and seventy-five in building a new house, in repairing the barn and sheds two hundred; he then sold it and made a profit of six hundred dollars. How much did he get for the farm?

(17) In 1861 the population of the counties on Lake Erie was: Essex, twenty-five thousand two hundred and eleven; Elgin, thirty-two thousand and fifty; Kent, thirty-one thousand one hundred and eighty-three; Norfolk, twenty-eight thousand five hundred and ninety; Haldimand, twenty-three thousand seven hundred and eighty; Welland, twenty-three thousand nine hundred and eighty-eight. What was the total population of the six counties on Lake Erie?

# SIMPLE SUBTRACTION.

12. SIMPLE SUBTRACTION is the method of finding what number remains, when a smaller number is taken from a greater number of the same kind.

The number so found is called the REMAINDER, or DIF-FERENCE.

The number subtracted from, is called the MINUEND; the number subtracted, the SUBTRAHEND.

13. The sign — called MINUS, placed between two numbers, means that the second number is to be subtracted from the first number: thus 7-3, or 7 minus 3, means that 3 is to be subtracted from  $7, \therefore 7-3 = 4$ .

### Rule for Simple Subtraction.

14. RULE. Write down the less number under the greater number, so that units may come under units, tens under tens, hundreds under hundreds, and so on; then draw a straight line under the lower number.

Take, if you can, the number of units in each figure of the lower number from the number of units in each figure of the upper number which stands directly over it, and place the remainder under the line just drawn, units under units, tens under tens, and so on.

But, if the units in any figure in the lower number bo

greater than the number of units in the figure just above it, then add ten to the upper figure, and then subtract the number of units in the lower figure from the number in the upper figure thus increased, and write down the remainder as before.

Add one to the next number in the lower number, and then take this figure thus increased from the figure just above it, by one of the methods already explained.

Go on thus with all the figures.

The whole difference, or remainder, so written down, will be the difference or remainder of the given numbers.

Ex. 1. Subtract 547 from 859.

By the Rule,

859 Method. 7 from 9 leave 2, i.e. 7 units from 9 547 units leave 2 units; write down 2 in the units' diff. = 312 place. 4 from 5 leave 1; i.e. 4 tens from 5 tens leave 1 ten; write down 1 in the tens' place.

5 from 8 leave 3, *i.e.* 5 hundreds from 8 hundreds leave 3 hundreds; write down 3 in the hundreds' place.

Ex. 2. Find the difference between seven hundred and forty-two and two hundred and sixty-eight.

By the Rule.

742 I cannot take 8 from 2, i.e. 8 units from 2 268 units,  $\therefore$  I add 10 to 2, which makes 12, 8 from diff. =  $\overline{474}$  12 leave 4; write 4 in the units' place.

un. -4.12 I have added 10 to the upper number 742, I must. add 10 to the lower number 268 (so as not to alter the difference between 742 and 268), *i.e.* 268 must be made 278, or 1 must be added to the 6.

Then I cannot take 7 from 4, *i.e.* 7 tens from 4 tens,  $\therefore$  I add 10 to the 4, really 10 tens or 1 hundred to the 4 tens, which makes it 14, really 14 tens, then 7 from 14 leave 7, really 7 tens; write 7 in the tens place.

I have just added 10 tens, or 1 hundred to the upper number, I must ... add 1 hundred to the lower number, *i.e.* I must add 1 to the 2, really 1 hundred to 2 hundreds, making it 3, really 3 hundreds, then 3 from 7 leave 4, really 4 hundreds; write 4 in the hundreds' place.

Ex. 3. How much greater is eight thousand two hundred than six thousand three hundred and nine?

8200 6309 =1891 9 from 0 I cannot, then 9 from 10 leave 1; write 1 in the units' place; carry 1, really 1 ten, then 1 from 0 I cannot, then 1 from 10 leave 9, really 1 ten from 10 tens leaves 9 tens; write 9 in the tens' place; carry 1, really 1 hundred, then 4 from 2 I [cannot, then 4 from 12 leave 8, really 4 hundreds from 12 hundreds leave 8 hundreds; write 8 in the hundreds' place, carry 1, really 1 thousand, then 7 from 8 leave 1, really 7 thousands from 8 thousands leave 1 thousand; write 1 in the thousands' place.

Note, The truth of all sums in subtraction may be proved by adding the less number to the difference or remainder; if this sum equals the larger number, the isum will probably have been worked correctly.

Thus, Proof of Ex. 3. Less number + remainder = 6309 + 1891 = 8200, the greater number.

				EX. A.			
From Take	(1) 18 14	(2) 27 15	(3) 39 11	(4) 55 5	(5) 86 60	(6) 568 22	(7) 759 603
	(8) 24 18	(9) 51 49	(10) 64 6	(11) 83 . <u>47</u>	(12) 98 89 —	(13) 70 54	(14) 64 29
	(15) 200 16	(16) 547 380	(17) 896 708	(18) 702 504	(19) 800 199	(20) 650 56	(21) 912 707
	(22) 563 476	(23) 209 1 <b>20</b>	(24) 608 499	(25) 486 307	(26) 843 745	(27) 900 791	(28) 505 107

(29) Subtract thirty-seven from fifty; twenty-nine from seventy-one; sixty-six from one hundred and four; ninetyseven from two hundred and eleven; one hundred and five from three hundred and three; four hundred and seventyfive from six hundred and forty-nine.

(30) A gentleman bought a horse "and a carriage for five hundred and sixty dollars, the horse was valued at three hundred dollars. How much was the carriage worth ? and how much was the horse worth more than the carriage ?

(31) In a school there are 75 children, there are 28 girls. How many more boys than girls are there?

(32) Oharles had 167 marbles, he gave John 49, James 65,

Thomas all the rest but 19; how many marbles had Thomas less than James?

(33) By how much does the sum of 6 and 4 exceed their difference ?

(34) A boy's father gave him 40 cents to pay 10 cents for a slate, 3 cents for pencils, 8 cents for a copy-book, 5 cents for ink, 3 cents for a postage stamp; after paying for the above he lost all but 4 cents through a hole in his pocket; how much did he lose ?

			Ex. XI.			
From Take	(1) 5467 3546	(2) 7601 3890	(3) 300 200	0	(4) 4536 2297	(5) 5480 996
	(6) 7009 5080	(7) 8052 4847	(8) 5281 597	(9) 7210 3809	(10) 8888 999	(11) 5600 2575
	(12) 14748 13942	(13) 54832 29648	(14) 80408 59385	( 70 69	15) 1007 1999	(16) 43520 25347
	(17) 445673 277594	(18 9200 560	8) 000 506	(19) 8712539 6805009		(20) 50030042 94090096

(21) What number taken from three thousand will leave one hundred and one? What number added to seventytwo thousand five hundred and seventy-six will make one million seventy thousand four hundred and nine.

(22) The sum of three numbers is twenty-three thousand two hundred and fifty-seven; the first is 9277, and the second is twelve hundred and eighty-three less than the first; find the third number.

(23) What is the difference between 23047 + 175 - 368 + 495 - 132 and 10000 - 8406 - 704 + 7305?

(24) When will the Prince of Wales, who was born in the year 1841, be as old as the Queen now, in the year 1869, is, who was born in the year 1819? How old will the Queen then be?

(25) John says to Henry, I have 97 marbles; Henry re-

plies, I have 29 less than you: Charlie adds, I have as many as both of you, less 25. How many marbles had Henry, and how many had Charlie?

(26) A man whose yearly income is 1000 dollars, spends 84 dollars for house rent, 135 dollars for servants, 39 dollars in travelling, 58 dollars in clothing, as much on his garden as in travelling and clothing, 804 dollars in household bills. Will he have saved anything, or be in debt at the end of the year, and to what amount?

(27) Harry goes up sixteen steps of a ladder, which has 45 steps, then down 7 steps, then up 10, then down 2, then down 4, then up 11, then down 9, then up 7, then up 5, then down 8, what step from the top and bottom will he then be standing upon?

(28) In a union workhouse there are 133 inmates. The number is made up thus: infirm and able-bodied 70; ablebodied and children 105; children and officers 63; officers 5. Find the number of each class.

(29) A basket contained oranges, nuts, and eggs; in all 1769; there were 1696 oranges and nuts, and 1262 nuts and eggs. How many more nuts were there than oranges?

(30) The population of the counties on the river St. Lawrence in 1861, was one hundred and seventeen thousand nine hundred and eighty-six, that of those on the Ottawa river was seventy-two thousand two hundred and sixty-eight. Find the difference between the population of these counties?

(31) What is the difference between thirty-seven millions nine hundred and six thousand seven hundred and three, and forty-five millions three thousand and eight?

(32) The subtrahend is fifty-six millions two hundred and twelve thousand three hundred, the remainder seventy-seven thousand three hundred and thirteen. What is the minuend?

(33) The minuend is sixty-six millions three hundred and four thousand, the difference twelve thousand five hundred and eighty-six. Find the subtrahend.

(34) A man bought 305 sheep for 3 dollars a head, and after spending 45 dollars on them for food, sold them for 4 dollars a head; how many dollars did he gain by his bargain?

(35) For the year 1861 the Imports into Canada were forty-three millions fifty-four thousand eight hundred and thirty-six dollars, and the Exports were thirty-four millions seven hundred and seventeen thousand two hundred and forty-eight dollars. Find by how much the Imports exceeded the Exports for the year 1861.

15. · ROMAN NOTATION. I, denotes one; V, five; X, ten; L, fifty; C, one hundred; D, five hundred; M, one thousand.

RULE. Where any one of the above letters is *after*, or to the right hand of, one of equal or greater value, it is to be *added* to it, but when put *before* one of greater value, it is to be *subtracted* from it.

Thus II = 1 + 1 = 2, III = 1 + 1 + 1 = 3, IV = 5 less I = 4, VI = 5 + 1 = 6, VIII = 5 + 1 + 1 + 1 = 8, IX = 10 less I = 9, XIII = 10 + 1 + 1 + 1 = 13, XIV = 10 plus 5 less I = 10 + 4 = 14, LXXIX = 50 + 10 + 10 + 10 less I = 70 + 9 = 79, XC = 100 less 10 = 90.

Note. A line over a letter or letters, increases their value a thousandfold; thus V=5,  $\overline{V}=5000$ ; C=100,  $\overline{C}=100000$ .

#### Ex. XII.

1. Express in the Roman Notation, three; seven; eleven; nine; twelve; sixteen; 18; 25; 28; 37; 40; 53; 59; 62; 77; 84; 103; 157; 190; 200; 651; 783; 1204; 1527; 1865.

2. Express in words, and also in Arabic figures, III; VI; VIII; XIII; XV; XVII; XX; LIV; LXXXI; CXI; DCV;  $\overline{V}$ II;  $\overline{MC}$ ; MM; DCCXLIX; MDCCCLXV.

# SIMPLE MULTIPLICATION.

16. SIMPLE MULTIPLICATION is a short method of repeated addition; thus, when 2 is multiplied by 3, the number obtained is the sum of 2 repeated three times, which sum=2+2+2=6.

The number, which is to be repeated or added to itself, is called the MULTIPLICAND: thus, in the above example, 2 is the multiplicand.

The number which shows how often the multiplicand is to be repeated, is called the MULTIPLIER: thus, in the above example, 3 is the multiplier.

The number found by multiplication, for instance 6 in the above example, is called the PRODUCT.

The multiplier and multiplicand are sometimes called Factors, because they are factors, or makers, of the product.

The sign x, called INTO, OR MULTIPLIED BY, placed be-

# SIMPLE MULTIPLICATION.

tween two numbers means that the numbers are to be multiplied together.

The following Table, called the MULTIPLICATION TABLE, ought to be learned correctly:

Twie	e	3 ti	mes	4	tim	es.	5 t	imes	6	time	s	7 t	imes
1 make	2 3 2	ma	kes 3	<b>1</b> p	nak	es 4	1 ma	akes	51 n	nakes	6	lma	kes7
2	4	2	. 6	2		8	2	1	0 2		12	2	14
3	6	3	. 9	3		12	3	1	5 3		18	3	21
4	8	4	. 12	4		16	4	2	0 4		24	4	28
5	10	5	. 15	5		20	5	2	5 5		30	5	35
6	12	6	18	6		24	6	3	<b>6</b>		36	6	. 42
7	14	7	. 21	7		28	7		5 7		42	7	. 49
8	16	8	. 24	8		32	8	. 4	0 8		48	8	
9	18	9	. 27	9		36	9	. 4	5 9		54	9	. 63
10	201	ŏ	. 30	10		40	10	5	010		$\tilde{60}$	10	
ii	221	ĩ	33	11		44	11	5	5 11		66	11	
12	241	2	36	12		48	12	. 6	0 12		72	12	. 84
		-											
8 tin	aes	9	time	s	10	tim	ies	11	tim	es	1	2 ti	mes
l mal	ces 8	1	make	s 9	11	mak	es 1	0 1	mak	es 11	1	mak	es 12
2	16	2		18	2		2	0 2		22	2		24
3	24	3		27	3		3	0 3		33	3		36
4	32	4		36	4		4	0 4		44	4		48
5	40	5		45	5		5	0 5		55	5		60
6	48	6		54	6		6	0 6		66	6		72
7	56	7		63	7		70	0 7		77	7		84
8	64	8		72	8		8	0 8		88	8		96
9	72	9		81	9		9	9 0		99	9		108
10	80	10		90	10		10	0 10		110	10		120
11	88	lii		99	11		110	011		121	11		132
12	96	12	1	108	12		12	112		132	12		144
	00		4 4 4							-0-	-		

17. Rule for Simple Multiplication, when the multiplier is a number not larger than 12.

RULE. Place the multiplier under the multiplicand, units under units, and (if the multiplier be 10, 11, or 12) tens under tens; then draw a line under the multiplier.

Multiply each figure of the multiplicand, beginning with the units, by the figure, or figures of the multiplier (by means of the Multiplication Table).

Write down and carry as in Simple Addition.

29

Ex. 1. Multiply 531 by 2. By the Rule.

Twice 1 unit makes 2 units; write 2 in the units' place of the product. Twice 3 tens of units

<u>2</u> make 6 tens of units; write 6 in the tens' place

1062 of the product. Twice 5 hundreds of units make 10 hundreds of units, or 1 thousand 0 hundred; write 0 in the hundreds' place, and 1 in the thousands' place.

Ex. 2. Find the product of 5063 and 6.

By the Rule.

5063 6 times 3 units = 18 units = 1 ten and 8 units; 6 write 8 units, carry 1 ten. Next 6 times 6

\_\_\_\_

tens = 36 tens, which added to the 1 ten carried

30378 = 37 tens = 3 hundreds and 7 tens; write 7 tens and carry 3 hundreds.

Next 6 times 0 hundreds = 0, which added to the 3 hundreds carried = 300 hundreds, write 3 in the hundreds' place.

Next, 6 times 5 thousands = 30 thousands = 3 tens of thousands and 0 thousands; write 0 in the thousands' place, and 3 in the tens of thousands' place.

Note. It will be seen from the Multiplication Table, that to multiply any number by ten, we have only to write 0 to the right-hand of the number, thus,  $3 \times 1 = 3$ ,  $3 \times 10 = 30$ ; also  $5893 \times 10 = 58930$ , and  $58930 \times 10 = 589300$ .

Similarly  $3 \times 100 = 300$ ,  $3 \times 1000 = 3000$ , and so on.

Also if any number be multiplied by 20, the result is the same as if the number were multiplied by 2, and 0 written on the right hand of the product; thus,  $6 \times 20 = 6 \times 2 \times 10 = 12 \times 10 = 120$ ; also,  $60 \times 20 = 1200$ , for  $60 \times 20 = 60 \times 2 \times 10 = 120 \times 10 = 1200$ ; and so of any other number.

Similarly  $60 \times 200 = 12000$ ,  $60 \times 2000 = 120000$ , and so on.

			E	x. XII	I.				
Multiply By	(1) 53 2 	$\overset{(2)}{\overset{47}{-}}$	(3) $88$ $2$	(4) 56 2	(5) 48 3		(7) 29 3	(8) 75 3	(9) 27 4
(10) 51 4	(11) 83 4	(12) 90 5	(13) 67 5	$(14) \\ 43 \\ 5 \\ -$	(15 36 6	5)	(16) 99 6	(17) 78 6	(18) 27 7

# SIMPLE MULTIPLICATION.

(19) 53 7	$(20) \\ 45 \\ 8$	(21) 77 8	(22) 69 9	(23) 54 9	(24) 20 10	(25) 99 10	(26) 53 11	(27) 87 11
	-	_	_			_	_	
(28)	(29)	(30)	(31)	(32)	(33)	(34)	(35)	(36)
91	60	49	687	800	697	<b>276</b>	777	497
11	12	12	<b>2</b>	3	3	4	5	6
		_						
(37)	(38)	(39)	(4)	0) (4	41)	(42)	(43)	(44)
479	905	835	48	7 5	60	538	888	704
7	7	8		9	10	11	12	12

(45) Supposing an acre of land to produce 39 bushels of wheat, how many bushels will 11 of such acres produce, and what will be their value at 6 shillings a bushel?

(46) There are 21 shillings in 1 guinea, and 12 pence in 1 shilling; how many pence are there in 3, 7, 12 guineas?

(47) Charlie bought of Quintin 11 rabbits at 23 cents each, and Quintin bought of Charlie 9 hens at 33 cents each, how many cents had Quintin to give to Charlie?

(48) What is the difference between 12 dozen and 8, and 8 dozen and 12? [Note, 1 dozen=12.]

(49) A has seven thousand four hundred and one potatoes; he sells B fifty-seven dozen and five; C one hundred and twelve dozen and eleven; D two hundred and fifty-nine dozen and nine; and E the remainder. How many more did E buy than C?

# Ex. XIV.

Multip	(1) bly 9048 By 2	$\begin{array}{c} (2) & (3) \\ 5849 & 98 \\ \hline 2 & \end{array}$	$\begin{array}{ccc} 3) & (4) \\ 573 & 38076 \\ 3 & 3 \\ \hline \end{array}$	(5) 6057 4	(6) 97068 5
(7) 69360 <u>6</u>	(8) 80965 5	(9) 439090 7	(10) 48508 8	(11) 33069 7	$\begin{array}{r}(12)\\38476\\9\end{array}$
	(13) 49216 12	(14) 69432 12	(15) 21357 11	(16) 91537 12	7

# ARITHMETIC.

(17) Multiply (1) 3870492, (2) 4609758, (3) 85973864, (4) 9090853, (5) 55880092, (6) 987654321, by each of the following, 2, 5, 3, 7, 4, 9, 6, 8, 11, and 12.

(18) Two persons start from the same place, and travel in the same direction, one at the rate of 93 miles a day, the other at the rate of 79 miles a day; how far apart will they be at the end of a week?

(19) If the second person at the end of two days turn back, and travel each day in the opposite direction the same number of miles as before; how far will they be apart at the end of a week?

18. Rule for Simple Multiplication, when the Multiplier is a number larger than 12.

RULE. Place the multiplier under the multiplicand, units under units, tens under tens, and so on; then draw a line under the multiplier.

Multiply each figure of the multiplicand, beginning with the units, by the figure in the units' place of the multiplier (by means of the table given for Multiplication); write down and carry as in Addition.

Then multiply each figure of the multiplicand, beginning with the units, by the figure in the tens' place of the multiplier, placing the first figure so obtained under the tens of the line above, the next figure under the hundreds, and so on.

Proceed in the same way with each succeeding figure of the multiplier.

Then add up all the results thus obtained by the rule of Simple Addition.

Ex. Multiply 2307 by 358.

By the Rule,

358	
18456	
11535	
6921	

since 358 = 30 + 0 50 + 8, when we multiply by the 5, we in fact multiply by 50, and  $2307 \times 50 = 115350$ ; again, when we multiply by the 3, we in fact multiply by 300, and  $2307 \times 300 = 692100$ ; hence it is quite clear that we may multiply

product = 825906 by the simple figures 5 and 3, if we only take care to place the first figure in the second line under the tens' place of the first line, and the first figure of the third line under the hundreds' place. Ex. 2. Find the product of 758 and 609.

758

609

6822

4548

461622

Since 758, or any other number, multiplied by 0 gives 0 as a product.  $\therefore$  in this case we multiply by 9 and then by 6, writing the first figure of the second line under the hundreds' place, and not under the tens' place of the line above, for 609 = 600 + 9.

Note 1. If the MULTIPLIER or MULTIPLICAND, or both, end with cyphers, we may omit them in the working; taking care to place on the right hand of the product as many cyphers as we have omitted from the end of the multiplier or multiplicand, or both. Thus, if 270 be multiplied by 507, and 2700 be multiplied by 50700, we have

270	270	In the first case, when we
507	50700	multiply 7 by 7, in fact we
190	190	multiply 70 by 7, and $70 \times 7$
125	195	=490.
100	100	In the second case, when
136890	13689000	we multiply 7 by 7, in fact
we multiply 70	by 700, and 70	$\times$ 700 = 49000.

Note 2.  $2 \times 3 = 2 + 2 + 2 = 6$ , and  $3 \times 2 = 3 + 3 = 6$ .:  $2 \times 3 = 3 \times 2$ ; and this is true of all numbers.

Note 3. If more than two factors have to be multiplied together, as  $2 \times 4 \times 9$ , it is termed CONTINUED MULTIPLICA-TION, and since  $2 \times 4 = 8$ , and  $8 \times 9 = 72$ , and  $.2 \times 4 \times 9 = 72$ , we shall of course obtain the same result, whether we multiply any number by 72, or by its factors 2, 4, and 9, by continued multiplication, and so of any other number.

 $35 \times 72 = 2520$ , and  $35 \times 2 \times 4 \times 9 = 70 \times 4 \times 9 = 280 \times 9 = 2520$ .

19. Numbers which are produced by multiplying together two or more numbers respectively greater than unity, are called COMPOSITE NUMBERS. Thus  $4 = 2 \times 2$ ,  $36 = 6 \times 6$ , or  $= 2 \times 3 \times 2 \times 3$ , and such like, are COMPOSITE NUMBERS.

Numbers which cannot be broken up into factors, as 3, 5, 7, 11, and such like, are PRIME NUMBERS.

Note 4. The truth of all results in Multiplication may be proved by using the multiplicand as multiplier, and the multiplier as multiplicand; if the product thus obtained be the same as the product found at first, the results are in all probability true.

## ARITHMETIC.

			Ex. A	V.			
Multi	(1) ply 463 By 18		) (3 8 27 27 3	3) ( 76 6 33 -	4) 01 9 54	(5) 94 <b>6</b> 61	(6) 837 39
(7) 793 30	(8) 407 55	(9) 869 89	(10) 917 46	(11) 692 73	(12) 909 88	(13) 305 715	(14) 463 608
	(15) 1263 36	(1 56	6) 13 54	(17) 96732 72		(18) 57628 64	
(19) 495 370	(20) 690 480	(21) 417 739	(22) 278 900	(23 90 8 90 80		4) 259 197	(25) 15900 3300
(26) 50738 9706	(27 8637 9090	) 4 )0 4	(28) 7672 5126	(29) 68109 2065	(3 450 78	80) 194 1338	(31) 56888 6049
(32) 92035 8007	(: 84 7	33) <sup>'</sup> 009 '898	(34 6780 8760	4) 000 000	(35) 90058 90009		(36) 80108 7770

(37) Find the product of seven thousand and thirty-nine by four thousand seven hundred and nine; three thousand nine hundred and ten by three hundred and fifty thousand; eighty-seven thousand nine hundred by nine thousand and six; seven millions eight thousand and five by four hundred thousand seven hundred and three.

(38) Find the product of the sum and difference of four hundred and ninety-six, and three hundred and twelve.

(39) Multiply (1) 973 by 63, and also by its factors 3, 3, and 7, and (2) 33000 by 1560, and also by its factors 13, 5, 4, and 6.

(40) As in (39) do also, (15), (16), (17), (18).

# Ex. XVI.

	(1)	(2)	(3)	(4)
Multiply	78689	275832	729817	46481
By	547	476	6736	936
## SIMPLE DIVISION.

(5)	(6)	(7)	(8)	(9)
40930	9264397	6707936	6078908	708670567
779	9584	<u>9878</u>	6725	97806
	(10) 6835675 2689	(11) 27083679 3709	250	(12) )58612 6289

(13) Find the product of 3523725 and 2538.

(14) " 2778588 and 9867.

(15) " " 79068025 and 1386.

(16) " 79094451 and 764095.

(17) Multiply five millions seventy-six thousand eight hundred and twelve by ninety-seven thousand six hundred and thirteen.

(18) Multiply nine millions five hundred and seven thousand three hundred and forty by seven thousand and seventy-one.

(19) Required the product of twelve millions four hundred and eighty-one thousand six hundred and thirty, and fifteen hundred and nine.

## SIMPLE DIVISION.

20. SIMPLE DIVISION is a short method of repeated Subtraction; or, it is the method of finding how often one number called the DIVISOR is contained in another number called the DIVIDEND. The number, which shews this, is called the QUOTIENT.

Thus, the dividend 12 divided by the divisor 4 gives the quotient 3; and for this reason, 4 + 4 + 4 = 12, and therefore if we subtract 4 from 12, and then a second 4 from the remainder 8, and then a third 4 from the remainder 4, nothing remains.

If however some number be left, after the divisor has been taken as often as possible from the dividend, that number is called the REMAINDER; thus, 11 divided by 4 gives a quotient 2, and a remainder 3; for after subtracting 4 from 11 once, there is a remainder 7; after subtracting 4 a second time from the remainder 7, there is a remainder 3.

The sign ÷, called By, or DIVIDED BY, placed between

two numbers, signifies that the first is to be divided by the second.

Division is just the opposite of Multiplication. By the Multiplication Table,  $3 \times 4 = 12$ , and  $12 \div 4 = 3$ , or  $12 \div 3 = 4$ .

21. Rule for Simple Division, when the Divisor is a number not larger than 12.

RULE. Place the divisor and dividend thus: divisor) dividend.

Take off from the left hand of the dividend the least number of figures which make a number not less than the divisor.

Find by the Multiplication Table how often the divisor is contained in this number; write the quotient under the units' figure of this number, and take notice of the remainder, whether it be any number or 0.

On the right of the remainder (whether it be any number or 0), conceive in your mind to be placed the least number of the figures next following in the dividend which will, affixed to the remainder, make a number not less than the divisor. Proceed, as above, with this new dividend to find the next figure of the quotient; taking care to place after the first figure in the quotient a cypher for every figure just brought down from the dividend except the last.

Continue this process till all the figures in the dividend have thus been brought down.

If there be a remainder at the end of the operation, write it as a remainder distinct from the quotient.

Ex. 1. Divide 756 by 3.

By the Rule,

3)756 Method of working. 3 in 7 goes 2 times and 1 over, write 2 under the 7; 3 in 15 goes 5 times.

252 1 over, write 2 under the 7; 3 in 15 goes 5 times, write 5 under the 5; 3 in 6 goes 2 times, write 2 under the 6.

Reason. In 756 the 7 = 700, the 5 50, = and the 6 = 6. Now 3 in 700 goes 200 times, and 100 over, therefore write 2 in the hundreds' place, and carry the 100; then 3 in 100 + 50, or 150, goes 50 times, therefore write 5 in the tens' place; then 3 in 6 goes 2 times, therefore write 2 in the units' place. Ex. 2. Find the quotient of 21406 by 7.

7)21406 Method of working. 7 in 2 goes no times,

but 7 in 21 goes 3 times, write 3 under the 1; 7 in 4 goes no times, 7 in 40 goes 5 times and 5 over; write 0 under the 4 and 5 under the 0; then 7 in 56 goes eight times, write eight under the 6.

<sup>c</sup> Reason. In 21406 the 21 is = 21000, the 4 = 400, and the 6 = 6.

 $\therefore$  the 3 in the quotient = 3000, the 5 = 50, the 8 = 8. and the quotient is 3058.

Ex. 3. Into how many classes of eleven each can a population of eight hundred and ninety thousand three hundred and eighty-nine to be divided?

11)890389

80944 rem. 5. *i. e.* 80944 classes and 5 people over, or 890389=80944 × 11 + 5 11 in 8 will not go, 11 in 89 goes 8 and 1 over, write 8 under the 9; 11 in 10 will not go, 11 in 103 goes 9 and 4 over, write 0 under the 0, and 9 under the 3; 11 in 48 goes 4 and 4 over, write 4 under the 8; 11

in 49 goes 4 and 5 over, write 4 under the 9, and rem. 5.

Ex. 4. Distribute six hundred thousand four hundred and fifty-five apples in equal portions between 12 families.

12)600455

50037 rem. 11 .\*. each family receives 50037 apples, and there are 11 apples over; or 600455 less 11=50037 × 12 12 in 60 goes 5; for the next dividend we have 045, ... we write two cyphers or 00 after the 5; 12 in 45 goes 3 and 9 over,...write 3 after 0; then 12 in 95 goes 7 and 11 over, ... write 7 after 3, and rem, 11.

### Ex. XVII.

Note. Each of the given numbers is to be divided by each of the different divisors.

(1) 88, 93, 98, 103, 100, by 6, 9, and 8.

(2) 105, 110, 119, 128, 117, by 5, 11 and 10.

(3) 130, 141, 153, 168, 147, by 6, 12, and 11.

(4) 172, 195, 206, 257, 240, by 6, 8, and 12.

(5) 462, 682, 840, 405, 555, by 4, 10, and 11.

(6) 600, 763, 842, 999, 717, by 11, 8 and 12.

(7) 1210, 6876, 6063, 5000, by 9, 12, and 11.

(8) 2760, 9604, 8267, 6548, by 8, 12, and 10.

(9) 86246, 72635, 85490, 35298, by 12, 10, and 7.

(10) 76002, 90009, 53027, by 11, 8, and 12.

(11) 5470698, 93700682, 2060198, by 8, 10, and 11.

(12) 8360047, 6789643, 9889989, by 7, 9, and 12.

(13) How many times can you subtract twelve from eight hundred thousand seven hundred and nine? What number besides 11 will exactly divide 218581?

(14) (1) If the dividend be 84, the quotient 9, the remainder 3, what is the divisor? (2) If the divisor be 11, the remainder 7, the quotient 146, what is the dividend?

(15) A woman bought 11 fowls at 36 cents each, and sold them so as to gain 198 cents; what did she sell each fowl for?

(16) A boy, having a basket containing 214 plums, distributed them equally between his eight schoolfellows and himself; the number which remained over he gave to his schoolmaster; how many did the schoolmaster receive?

(17) The sum of two numbers is 4563, and the less number is 9; find their quotient.

(18) Find the difference between the product of 40687 and 503, and the quotient of 93710562 by 11.

(19) A Bachelor, who died worth 5427 dollars, left 1500 dollars to charities, and the rest of his property between his housekeeper, manservant, and cook; the manservant was to have twice the cook s share, and the housekeeper was to have twice the manservant's share; what did each receive.

(20) If the sum of 18 and 30 be divided by their difference, and the quotient be multiplied by the product of 16 and 27, what is the result?

(21) Find the product of nine hundred and seven thousand and fifty seven by six millions and six, and find what number added to the result will make it exactly divisible by nine.

(22) A basket contained 282 apples and oranges; there were 230 more apples than oranges. Find the number of oranges.

(23) How many penknives, worth 16 cents each, ought to be exchanged for 4 gross of penholders at 10 cents per dozen, and twenty-five score envelopes at 16 cents a hundred? Note, 1 score = 20, 1 gross = 12 dozens.

## SIMPLE DIVISION.

22. Rule for Simple Division, when the Divisor is a number larger than 12.

### RULE. Place the divisor and dividend thus: divisor) dividend (

leaving a space for the quotient on the right of the dividend. Take off from the left hand of the dividend the least num-

ber of figures which make a number not less than the divisor.

Find how many times the divisor is contained in this number: write the quotient as the left-hand figure of the whole quotient; multiply the divisor by this figure, and bring down the product under the number taken off from the left of the dividend, and subtract.

On the right of the remainder (whether it be any number or 0) place the least number of figures next following in the dividend which will, affixed to the remainder, make a number not less than the divisor. Proceed as above with this new dividend to find the next figure of the quotient; taking care to place after the first figure in the quotient a cypher for every figure just brought down from the dividend except the last.

Continue this process till all the figures in the dividend have thus been brought down.

If there be a remainder at the end of the operation, write it as a remainder distinct from the quotient.

Note. If any remainder be equal to or greater than the divisor, the last figure of the quotient must be changed for one greater.

Ex. 1. Divide 1368 by 57. By the Rule,

Method of Working. 136 is the least num-57) 1368 (24 ber taken from the left of the dividend, into 114 which 57 will go; we then say 5 into 11 goes 228 2; write 2 as the first figure of the quotient 228 on the right hand, write also 114 (product of

57  $\times$  2) under 136 and subtract; we obtain a remainder 22. Then place 8, the next figure in the dividend, to the right of the remainder; we thus obtain a new dividend 228; as before 5 into 22 goes 4; write the 4 to the right of the 2 in the quotient; and so proceed till all the figures in the dividend are brought down.

1368 = 1360 + 8; ... the 1st dividend is really Reason. 1360; now 57  $\times$  20 = 1140,  $\therefore$  the 1st number in the quotient is 20; and 1360 - 1140 = 220; ... the second dividend is 220 +

8 or 228, and as  $57 \times 4 = 228$ ,  $\therefore$  the second figure in the quotient is 4, and the quotient is 20 + 4 or 24.

Note. Since  $136\hat{8} \div 57 = 24$ , it follows that  $1368 \div 24 = 57$ , and also that  $57 \times 24 = 1368$ .

Ex. 2. Find the quotient of 1039888 by 5048.

 $\begin{array}{ccccccc} 5048 & 1039888 & (206 & 10398 & is the$ *least* $number, taken from the left of the dividend, into which 5048 will go; we then say 5 in 10 goes 2, and 5048 <math>\times 2 = 10096$ ; write 2 as the left-hand figure of the quo-

tient, 10096 under 10398, and subtract; we obtain a remainder 302. Then we have to place the next *two* figures 88 of the dividend to the right of this mainder to form a number 30288 greater than the divisor,  $\therefore$  we must write 0 in the quotient after 2; then 5 in 30 goes 6 times, and 5048  $\times$  6 = 30288, write 6 in the quotient after 0, 30288 under 30288, and subtract; there being no remainder, 206 is the quotient required.

Ex. 3. How many times does 318493585 contain 8607? 8607)318493585(37004

After obtaining 37 in the quotient, 3 figures of the dividend have to be brought down to get the next significant figure in the quotient,  $\therefore$  write two cyphers in the quotient.

8607 is contained 37004 times in 318493585, and there is a remainder 157; in other words  $318493585 = 37004 \times 8607 + 157$ , or 318493585 less  $157 = 37004 \times 8607$ .

23. When the divisor is a composite number, and made up of two factors, neither of which exceeds 12, the dividend may be divided by one of the factors in the way of Short Division, and then the result by the other factor. If there be a remainder after each of these divisions, the true remainder will be found by multiplying the second remainder by the first divisor, and adding to the product the first remainder.

Ex. 4. Divide 56732 by 45. (  $\partial$  + 56732, *i. e.* 56732 units,

5)

5 6303 rem. 5, *i. e.* 6303 nines and rem. 5 units,

1260 rem. 3, *i.e.* 1260 forty-fives, and rem. 3 nines, .: the true rem.  $=9 \times 3$  units + 5 units = 27 + 5, or 32 units.

## SIMPLE DIVISION.

Therefore the quotient arising from the division of 56732by 45 is 1260 with a remainder 32 over.

## Ex. XVIII.

## D'vide

- (1) 192 by 16; 720 by 18; 795 by 15; 1786 by 19.
- (2) 1035 by 23; 1073 by 37; 2730 by 42; 5432 by 56.
- (3) 4560 by 80; 3871 by 49; 7744 by 88; 6935 by 95.
- (4) 5375 by 25; 29526 by 37; 25665 by 29; 4590 by 45.
- (5) 69230 by 86; 37510 by 55; 10287 by 81; 23919 by
   67; 25760 by 56; 538840 by 76.
- (6) 35626 by 94; 31339 by 77; 80840 by 86; 28782 by 39; 9009196416 by 96; 41765256 by 72.
- (7) 88832 by 256; 175252 by 308; 321776 by 104.
- (8) 653723 by 329; 3577926 by 506; 542100 by 834.
- (9) 8189181 by 909; 4049820 by 745; 342604 by 883.
- 10) 7848600 by 365; 2339100 by 678; 90625 by 727.
- (11) 27291888 by 478; 30387310 by 397; 3273068 by 703.
- (12) 37624792 by 843; 90273189 by 513; 53006751 by 609; 30073074 by 358; 630762540981 by 652.
- (13) 519387042 by 2731; 10101255 by 2185; 154725876 by 3076; 632798014 by 7243.
- (14) 2015029 by 1004; 131686100 by 6487; 395494875 by 6007; 50696184 by 1617.
- (15) 4519559744 by 5008; 16322853 by 9306; 23617103000 by 1579; 2106144185 by 2735.
- (16) 142997420 by 3782; 19554707200 by 6016; 2828882701578 by 38706.

(17) What number multiplied by 79 will give the same product as 257 multiplied by 553?

(18) How many pairs of stockings, at 66 cents a pair, should be given for 9 dozen pairs of gloves, at 110 cents a pair?

(19) What number must be added to thirty millions nine hundred and eighty-four thousand and fifty-one, that the sum may be exactly divisible by two hundred and eightyeight?

(20) If the sum of 274 and 108 be multiplied by their

difference, and the product be divided by 176, what will be the quotient?

(21) A farmer bought 75 sheep at 4 dollars each; 94 sheep at 3 dollars each; and 106 sheep at 2 dollars each; at what price per head must he sell the sheep, so as to gain 147 dollars by his bargain?

(22) A hatter sold 267 hats for 1068 dollars, gaining thereby 1 dollar on each hat, what did each hat cost him?

(23) If the sum of 103, 29, and 267 be divided by 19, and the quotient be multiplied by 57, and the product be diminished by 197, what will the remainder be?

(24) 8 lambs are worth 16 dollars, and 15 sheep are worth 60 dollars; how many of such sheep ought to be given in exchange for 840 of such lambs?

(25) The sum of the product of two numbers and 355 is eighty-seven thousand four hundred and three; one of the numbers is 216; find the other number.

(26) What number must 416 be multiplied by to produce 154979552?

(27) What number subtracted 28 times from 479632 will leave 20 as a remainder ?

(28) A farmer bought 29 bullocks for 1885 dollars, and after keeping them for 3 months, and spending on each 5 dollars per month, he sold all the bullocks for 2610 dollars; what was his gain on each bullock?

24. If the Divisor terminate with a cypher or cyphers, the process of Division can be shortened by the following Rule.

RULE. Cut off the cypher or cpyhers from the divisor, and as many figures from the right-hand of the dividend, as there are cyphers to cut off at the right-hand end of the divisor; then proceed with the remaining figures according to the Rule, Art. 21 or Art. 22. as the case may be; and to the last remainder affix the figures cut off from the dividend for the true remainder.

### Ex. 1 Divide 57 by 20.

2,0)5,7 2 rem. 1.  $10, \therefore$  when the 5 is divided by the 2, the rem.  $10, \Rightarrow$  really 1 ten, or 10, and the true rem. = 10 + 7 or 17.

### Ex. 2. Divide 46431 by 500.

5,00)464,31	46431 = 46400 + 31, and $46400$ divided by $500 = 92$ with rem. $400$ , $\therefore$ when the
92 rem. 4.	464 is divided by the 5, the rem. 4 is really 400, and the true rem. 431.

Ex. 3. Divide 375340 by 5900.

59,00)3753,40(63

354	$\therefore$ quotient = 63, and re				
213	=	3640.			
177					
36					
		1000	1.1		***

Ex. 4. Divide 563854 by 10, by 1000, and by 100000. We may write down the quotient and remainder for each question at once.

Thus: 1st quotient = 56385, and rem. = 4. 2nd .... = 563, .... = 854. 3rd .... = 5, .... = 63854.

### Ex. XIX.

(1) Divide 34, 43, 56, 80, 135, 260, 1504, by 10, 20, and 30.

(2) Divide 237, 840, 673, 291, 6019, 7820, 81229, 327800, by 40, 60, 70, 100, and 200.

(3) Divide 79048, 6870, 890061, by 240, 1000, 1500, and 2600; and 830678103490 by 100000000.

- (4) 806753245 9067.
- (5)  $612709066 \div 70602$ .
- (6) 60005836÷896.
- (7)  $70867509 \div 9986.$
- (8)  $8673456954 \div 868$ .
- (9)  $200006783 \div 93256$ .

(10) Multiply 14609 by 719 and divide the product by 8067.

(11) How many regiments of 1000 men, and also of 1200 men, can be formed out of one million one hundred thousand men?

(12) Add together twenty-five millions seven hundred and sixty thousand and thirty-four, 75211379 and 4637862; subtract ten millions and seventy-five from the sum; divide the remainder by 100000.

## SECTION II.

## MONEY TABLES.

### CANADIAN CURRENCY.

25.	The silver coins	are	: a	5	cent	piece.	
			a	10	66		
			a	20	66	66	
			a	25	66	66	
			a	50	66	66	

100 cents make one dollar, or \$1.

Note 1. The cent which is made of bronze, is one inch in diameter, and 100 cents weigh one pound avoirdupois.

#### HALIFAX OR OLD CANADIAN CURRENCY.

26.

2 Farthings make 1 Half-penny, or 1d. 

 2 Half-pence
 1 Penny
 1d.

 12 Pence
 1 Shilling
 1s.

 5 Shillings
 1 Dollar
 \$1.

 4 Dollars ..... 1 Pound .....£1.

Note 2. The farthing is written thus, 1d; and three farthings thus, ad.

### ENGLISH OR STERLING CURRENCY.

27.

2	Farthings make	1	Half-penny, o	r Id.
2	Half-pence	1	Penny	. 1d.
0	Domos	1	Shilling	10

- 12 Pence ..... 1 Shilling ..... 18. 20 Shillings ..... 1 Pound .....£1.

The sovereign, a gold coin = 20 shillings. The guinea, a gold coin not now in use = 21 shillings. Note 3. The sterling pound = \$4.86<sup>2</sup> Canadian currency

UNITED STATES CURRENCY.

10	Mills make	1	Cent.
10	Cents	1	Dime.
10	Dimes	1	Dollar.
10	Dollars	1	Eagle.

45

## WEIGHTS AND MEASURES.

### TABLE OF TROY WEIGHT.

29. TROY WEIGHT is used in weighing gold, silver, diamonds, and other articles of a costly nature; and also in determining specific gravities.

24 Grains, grmake 1 Pennyweight	l dwt.
20 Pennyweights 1 Ounce	1 oz.
12 Ounce 1 Pound 1 lb.	or 1 1b.

### TABLE OF AVOIRDUPOIS WEIGHT.

30. AVOIRDUPOIS WEIGHT is used in weighing all heavy articles, which are coarse and drossy, or subject to waste, as butter, meat, and the like, and all objects of commerce, with the exception of medicines, gold, silver, and some precious stones.

16 Drams, drmake 1 Ounce	. 1 oz.
16 Ounces 1 Pound	. 1 lb.
25 Pounds 1 Quarter	. 1 qr.
4 Quarters, or 100 lbs 1 Hundredweight	. 1 cwt.
20 Hundredweights 1 Ton	. 1 ton.
Note 1 lb Avoirdupois weighs 7000 grs Troy	

### TABLE OF APOTHECARIES' WEIGHT.

31. APOTHECARIES' WEIGHT	is used in mixi	ng medicares.
20 Grains, grmake	1 Scruple	I sc. or 1 9
3 Scruples	1 Dram	1 dr. or 13
8 Drams	1 Ounce	1 oz. or 1 3
12 Ounces	1 Pound	1 lb. or 1 HB

### TABLE OF LINEAL MEASURE.

32. In this measure, which is used to measure distances, lengths, breadths, heights, depths, and the like, of places or things:

12 Linesmake 1 Inch	11.
12 Inches 1 Foot	1 ft.
3 Feet, or 36 in 1 Yard	1 yd.
6 Feet 1 Fathom	1 fth.
51 Yards, meaning 5 yards and 1 Rod, Pole, a half ward	1 po.
40 Poles, or 220 yds 1 Furlong	l fur.
8 Furlongs, or 1760 yds 1 Mile	1 mi.
3 Miles 1 League	1 lea.

The following measurements may be added, as useful in certain cases:

4 Inches make 1 Hand (used in measuring horses).

22 Yards..... 1 Chain { (used in measuring land.) 100 Links ..... 1 Chain {

A degree is equal to 60 geographical, or nearly  $69\frac{1}{2}$  English miles.

#### TABLE OF CLOTH MEASURE.

33. In this measure, which is used by linen and woollen drapers;

21 Inches make 1 Nail ..... 1 nl.

4 Nails ..... 1 Quarter .... 1 qr.

4 Quarters... 1 Yard ..... 1 yd.

5 Quarters. . . 1 Ell (English).

6 Quarters. .. 1 Ell (French).

### TABLE OF SQUARE MEASURE.

34. This measure is used to measure all kinds of surface or superficies, such as land, paving, flooring, in fact everything in which length and breadth are to be taken into account.

A SQUARE is a four-sided figure, whose sides are equal, each side being perpendicular to the adjacent sides. See figure below.

A square inch is a square, each of whose sides is an inch in length; a square yard is a square, each of whose sides is a yard in length.

144 Square Inches make 1 Square Foot... 1 sq. ft. or 1 ft.

9 Square Feet. ..... 1 Square Yard .. 1 sq. yd. or 1 yd.

30<sup>‡</sup> Square Yards..... 1 Square Pole...1 sq. po. or 1 po.

40 Square Poles ..... 1 Square Rood .. 1 ro.

4 Roods .....1 Acre.....1 ac.

25000 Square Links = 1 Rood. 100000 ..... = 1 Acre.

 $10 \dots$  Chains = 1 Acre.

4840 ...... Yards = 1 Acre.

 $640 \ldots Acres = 1$  Square Mile.

Note. This table is formed from the table for lineal measure, by multiplying each lineal dimension by itself.

The truth of the above table will appear from the following ronsiderations.

Suppose AB and AC to be lineal yards placed perpendicularly to each other.



Then ABCD is a square yard. If AE, EF, FB, AG, GH, HC, each = 1 lineal foot, it appears from the figure that there are 9 squares in the square yard, and that each square is 1 square foot.

The same explanation holds good of the other dimensions.

### TABLE OF SOLID OR CUBIC MEASURE.

35. This measure is used to measure all kinds of solids, or figures which consist of three dimensions, length, breadth, and depth or thickness.

A CUBE is a solid figure contained by six equal squares; for instance, a die is a cube. A cubic inch is a cube whose side is a square inch. A cubic yard is a cube whose side is a square yard.

- 1728 Cubic Inches.....make 1 Cubic Foot, or 1 c. ft. . 27 Cubic Feet ..... 1 Cubic Yard, or 1 c. yd.
  - 40 Cubic Feet of Rough Timber or
  - 50 Cubic Feet of Hewn Timber 1 Load.
  - 42 Cubic Feet ..... 1 Ton of Shipping.
  - 128 Cubic Feet of Fire-wood .... 1 Cord.
  - 16 Cubic Feet of Fire-wood .... 1 Cord-foot.

The truth of the first part of above table will appear from the following considerations.

If AB, AC, and AD be perpendicular to each other, and each of them a lineal yard in length, then the figure DE is s cubic yard.

Suppose DH a lineal foot, and HKLM a plane drawn parallel to side DC.

By the table Art. 34, there are 9 square feet in side DC. There will therefore be 9 cubic feet in the solid figure DL. Similarly, if another lineal



foot HN were taken, and a plane NO were drawn parallel to HL, there would be 9 cubic feet contained in the solid figure HO.

Similarly, there would be 9 cubic feet in the solid figure NE.

Therefore, there are 27 cubic feet in the solid figure *DE*, or in 1 cubic yard.

Note. A pile of wood 4 feet high, 4 feet wide, and 8 feet long, makes a cord.

## MEASURES OF CAPACITY.

#### TABLE OF WINE MEASURE.

36. In this measure, by which wines and all liquids, with the exception of malt liquors and water, are measured

40	Hills make	1	Pint1	l pt.
2 I	Pints	1	Quart]	gt.
46	Juarts	1	Gallon ]	gal.
33 (	Jallon's	1	Hogshead]	hhd.
21	Togsheads	1	Pipe	l pipe.
2 H	Pipes	1	Tun	tun.

### TABLE OF ALE AND BEER MEASURE.

37. In this measure, by which all malt liquors and water are measured:

2	Pintsmake	1	Quart1	qt.
4	Quarts	1	Gallon1	gal.
9	Gallons	1	Firkin1	fir.
18	Gallons	1	Kilderkin .1	kil.
36	Gallons	1	Barrel1	bar.
13	Barrels, or 54 Gallons	1	Hogshead .1	hhd.
2	Hogsheads	1	Butt 1	butt.
2	Butts	1	Tun 1	tun.

#### TABLE OF DRY MEASURE.

38.	2 Pints		.make 1	Quart1	qt.
	4 Quarts		1	Gallonl	gal
	2 Gallons		1	Peck 1	pk.
	4 Pecks.		1	'Bushell	bu.
	36 Bushels	3	1	Chaldronl	ch.

39. 34 Pounds make 1 Bushel of Oats.

- 48 Pounds .... 1 Bushel of B'kwheat, Barley or Timothy
- 50 Pounds .... 1 Bushel of Flax Seed.
- 56 Pounds .... 1 Bushel of Rye or Indian Corn.
- 60 Pounds .... 1 Bushel of Wheat, Potatoes, Peas,

Beans, Onions, or Red Clover Seed.

Note 1. Grains are sold by the cental (100 lbs.), or by parts thereof.

## MEASURES OF TIME.

#### TABLE OF TIME.

40. 1 Second is written thus 1".

60	Secondsmake 1	Minute	
60	Minutes 1	Hour 1 1	ır.
24	Hours 1	Day1 (	lay.
7	Days 1	Wcek 1 v	wk.
4	Weeks, or 28 days 1	Lunar monthl 1	no.
365	Days 1	Civil or common year.l y	yr.

Note 2. 60 minutes make 1 degree, or 60' make 1°.

A degree is the 360th part of the circumference of a circle.

A year is divided invo 12 months, called Calendar Months, the number of days in each of which may be easily remembered by means of the following lines;

> Thirty days hath September, April, June and November: February has twenty-eight alone, And all the rest have thirty-one : But leap-year coming once in four, February then has one day more.

Note 3. A civil or common year = 52 wks, 1 day. A leap year = 366 days.

Every year which is divisible by 4 without a remainder is a LEAP OR BISSE TILE YEAR; except those years which complete a century (i. e. a hundred years), the numbers expressing which century, are not divisible by four; thus 1600 and 2000 are leap/years, because 16 and 20 are exactly divisible by 4; but 1700, 1800 and 1900 are not leap years, because 17, 18, and 19 are not exactly divisible by 4.

## MISCELLANEOUS TABLE.

<b>41</b> .	12 Unitsmake	1 Dozen.
L	12 Dozen	1 Gross.
	12 Gross	1 Great Gross.
	20 Units	1 Score.
	24 Sheets of Paper	1 Quire.
	20 Quires	1 Ream.
	100 Pounds	1 Quintal.
	196 Pounds	1 Barrel of Flour.
	200 Pounds	1 Barrel of Pork or Beef.

Note. A sheet folded into two leaves is called a folio, into 4 leaves a quarto, into 8 leaves an octavo, into 16 leaves a 16 mo, into 18 leaves an 18 mo, &c.

## REDUCTION.

42. When a number is expressed in one or more denominations, the method of finding its value in one or more other denominations is called REDUCTION. Thus,  $\pounds 1$  is of the same value as 240d., and  $7s. 1\frac{1}{2}d.$  is of the same value as 342 farthings, and conversely; the method or process by which we find this to be so, is REDUCTION.

43. First. To express a number of a higher denomination or of higher denominations in units of a lower denomination.

RULE. Multiply the number of the highest denomination in the proposed quantity by the number of units of the next lower denomination contained in one unit of the highest, and to the product add the number of that lower denomination, if there be any in the proposed quantity.

Repeat this process for each succeeding denomination, till the required one is arrived at.

Ex. 1. How many cents in \$75.65 cents?

By the Rule,

\$75.65

100

7500 + 65 = 7565 cents.

- Reason.
   Since 100 cents make

   one dollar;  $$75 = (75 \times 100 \text{ cts.})$  

   = 7500 cts.,  $\therefore$  \$.5.65 = 7500

   + 65 = 7565 cents.
  - ... \$75.65 = 7565 cents.

## REDUCTION.

Ex. 2. Reduce £2 to farthings. By the Rule,

£	
2	Reason for the Rule.
20	$\pm 1 = 20s., \therefore \pm 2 = (2 \times 20)s. = 40s.$
40s. 12	$1s. = 12d., \therefore 40s. = (40 \times 12)d. = 480d.$
4800	$1d. = 4q., \therefore 480d. = (480 \times 4)q. = 1920q.$
4	$\therefore \pounds 2 = 40s. = 480d. = 1920q.$
1920q.	

# Ex. XX.

### Reduce

- (1) £709. 16s., 8d, to farthings.
- (2) 17 mls., 1 fur., 2 ft., 6 in. to inches.
- (3) 8 tons, 2 cwt., 3 qrs., 5 lbs. to drams.
- (4) 612 ac., 2 r., 27<sup>1</sup>/<sub>2</sub> yds. to square inches.
- (5) 10 mls. 5 fur., 5 po., 5 yds., 0 ft., 5 in., 5 ls. to lines.
- (6) 5 ac., 3 per., 29 yds. to square inches.
- (7) 17 days to minutes.
- (8) 2 lbs., 11 oz., 20 grs. to grains.
- (9) 2 lea., 2 mls., 7 fur. to yards.
- (10) 23 cub. yds., 1000 in. to cubic inches.
- (11) 13 galls., 3 qts. to gills.
- (12) 220 bushels to quarts,
- (13) 3 yrs., 315 days to minutes.
- (14) 27 lbs., 5 oz., 16 dwts. to grains.
- (15) 47 lbs., 11 oz., 6 drs., 2 sc. to grains.
- (16) £200. 17s., 8<sup>1</sup>/<sub>2</sub>d. to half-pence.
- (17) 219 ac., 2 r., 16 per. to square yards.
- (18) 218 yds., 2 qrs., 3 nls. to nails.
- (19) £2376. 19s., 8<sup>1</sup>/<sub>2</sub>d. to farthings.
- (20) 216 cwt., 2 qrs., 17 lbs. to pouuds.
- (21) 25° 36' to seconds.
- (22) 8 mls., 3 fur., 4 yds. to inches.
- (23) £312 17s., 61/2d. to farthings.
- (24) 105 lbs. Troy to grains.

- (25) 26 English ells to nails.
- (26) 37 French ells to nails.
- (27) £567. 0s. 61d. to farthings.
- (28) 287 lbs., 6 oz. to scruples,
- (29) 3 pipes to gallons.
- (30) £200. 19s., 612d. to farthings.

44. Secondly. To express a number of lower denomination or denominations in units of a higher denomination.

RULE. Divide the given number by the number of units which connect that denomination with the next higher, and the remainder, if any, will be the number of surplus units of the lower denomination.

Carry on this process, till you arrive at the denomination required.

Ex. 1. How many tons, cwts., &c., are there in 27658 drams? By the Rule,

1 cwt., 0 qrs., 8 lbs., 0 oz., 10 drs.

... 27658 drams=1 cwt., 0 qrs., 8 lbs., 0 oz., 10 drs.

Ex. 2. In 17392 cents, how many dollars and cents. By the Rule,

 $100 \begin{cases} 10 \\ 10 \\ \hline 1739 \\ \hline 100 \\$ 

Note. From the above example, we see that by cutting off the last 2 figures on the right of any number of cents, gives the dollars, and the figures so cut off will be the cents.

## COMPOUND ADDITION.

## Ex. XXI.

### Reduce.

- (1) 123290 farthings to pounds.
- (2) 13172 grs. to lbs. Troy.
- (3) 18191 pts. to gallons.
- (4) How many leagues in 76787568 inches?
- (5) How many tons, &c., in 2007008 drams?
- (6) How many acres in 93827 perches?
- (7) In 167812 grs., how many lbs. Troy?
- (8) In 8756765637 lines, how many miles, &c.?
- (9) In 7678678956 drs., how many tons, &c.?
- (10) In 121605 in., how many miles, &c.?
- (11) In 98006 grs., how many lbs. Troy, &c.?
- (12) In 2022752 drs., how many tons, & ..?
- (13) How many lbs., ozs., drs., &c., in 702917 grs.?
- (14) How many years (365 ds.), &c., in 1727893 seconds ?
- (15) How many acres, &c., in 172425 yards?
- (16) How many yards in 13856832 cubic inches?
- (17) How many acres in 1244160000 sq. inches ?
- (18) How many yards, &c., in 500 nails?
- (19) In 131075 seconds, how many degrees, &c.?
- (20) In 31557600 seconds, how many days, &c.?
- (21) In 219612 pts., how many hogsheads of beer?
- (22) In 300738 pts., how many hogsheads of wine?
- (23) In 912715 lbs., how many bushels of wheat?
- (24) In 1000000 lbs. of oats, how many bushels?
- (25) In 7263 lbs. of timothy seed, how many bushels?
- (26) In 30747 cents, how many dollars?
- (27) How many pounds, &c., in 973647 farthings?

## COMPOUND ADDITION.

45. COMPOUND ADDITION is the method of collecting several numbers of the same kind, but containing different denominations of that kind, into one sum.

RULE. Arrange the numbers, so that those of the same denomination may be under each other in the same column, and draw a line below them.

Add the numbers of the lowest denominations together, and find by Reduction how many units of the next higher denomination are contained in this sum.

Write the remainder, if any, under the column just added, and carry the quotient to the next column.

Proceed thus with all the columns.

Ex. 1. Add together \$21.97, \$28.76, \$38.39.

By the Rule,

\$21.97 The sum of the right-hand column is 22;
\$28.76 write 2 under that column, and carry 2 to the next; the sum of the next column together with the 2 carried is 21; write 1 under that column and carry 2 to the next, and so on ; the same

way as was done in the Simple Rules, and for the same reason.

Ex. 2. Find the sum of £6. 6s., £3. 13s.  $0\frac{3}{4}d.$ , £33. 15s. 11 $\frac{1}{4}d.$ , and £43. 0s.  $8\frac{1}{4}d.$ 

			$1q. + 2q. + 3q. = 6q. = 1\frac{1}{2}d.$ write down
£	8.	d.	1d., and carry 1d.
6.	6.	0	Then $1d_1 + 8d_2 + 11d_3 = 20d_3 = 18, 8d_3$ :
3.	13.	03	write down 8d., and carry 1s.
35 .	15.	114	Then $1s + 15s + 13s + 6s - 35s - f1$
43.	0.	81	15s.; write down 15s, and carry $\pounds$ 1.
£88 .	15.	81	Then $\pounds 1 + \pounds 43 + \pounds 35 + \pounds 3 + \$6 = $ fs8: write down fs8

Note. The method of proof in the Compound Rules is the same as in the Simple Rules.

### Ex. XXII.

Add together.

(1)	\$26.79 \$39.17 \$28.68	(2)	£ 5	9. 10. 12.	d. 8 4 3	(3)	2. 6. 1.	1bs. 17. 24. 6.	oz. 12 13 8
(4)	lbs. oz. 35.3. 27.8. 41.9. 2.3.	dwt. 4.1 14.2 17.1 13.2	22 22 0	(8	lbs. 5) 17 12 6 17	oz. 8.10 6.11	dr. 2. 6. 4. 7.	sc. 1. 0. 2.	gr. 5 19 18 19

## COMPOUND SUBTRACTION.

	tons cwt. qrs. lbs. oz.
(6) \$ 286.97	(7) 21.16.2.24.10
6126.35	26.5.1.22.9
517.68	1, 17, 3, 19, 12
9612.07	19, 12, 0, 18, 9
719 15	218 10 1 12 8
/12.15	210.10.1.12.0
yds. qrs. nls.	mls. fur. per. yds. ft.
(8) 27 . 2 . 3	(9) 2.3.8.2.2
35 . 3 . 2	25, 7, 21, 4, 1
217 1 3	3 6 23 2 0
89 2 2	17 4 19 3 2
907 3 9	90 5 16 1 1
201.0.2	25.5.10.1.1
£ s. d.	dys. hrs. min. sec.
(10) 38. 6. 7 <sup>1</sup> / <sub>2</sub>	(11) 2.16.16.17
29, 16, 81	27, 22, 22, 33
$39 \cdot 17 \cdot 6^{\frac{3}{2}}$	19, 21, 30, 37
21 18 7	28 23 39 50
15 17 8	36 20 45 55
10.17.0	50.20.40.00
	1.1
	ac. ro. per. yds. ft. in.
(12) \$2219.64 $(13)$	5.0.7.13.2.5
3812.75	7.3.9.22.8.107
913.25	9.1.16.29.2.96
837.19	19 . 2 . 22 . 27 . 6 . 108
687 29	0 3 7 28 3 12
	0.0.7.40.0.14
tons cwt. qrs. lbs. oz	. drs.
(14) 23.15.2.20.5	. 0 (15) \$5617.28
21.17.0.24.1	. 13 208.09
43.19.3.24.15	. 15 516.99
3. 9.2.17.13	. 11 3712.89
6, 6, 1, 0, 7	. 8 984.75

## COMPOUND SUBTRACTION.

46. COMPOUND SUBTRACTION is the method of finding the difference between two numbers of the same kind, but containing different denominations of that kind.

RULE. Place the less number below the greater, so that the numbers of the same denomination may be under each other in the same column, and draw a line below them.

Begin at the right hand, and subtract if possible each number of the lower line from that which stands above it, and set the remainder underneath.

But when any number in the lower line is greater than the number above it, add to the upper one as many units of the same denomination as make one unit of the next higher denomination; subtract as before, and carry one to the number of the next higher denomination in the lower line.

Proceed thus throughout the columns.

Ex. 1. From £51. 0s.  $8\frac{1}{2}d$ ., take £47. 18s.  $7\frac{2}{3}d$ .

By the Rule, £ s. d.

8. Method of working. I cannot take 81 51. 0. 3q. from 2q., so I add 1d., or 4q., to the 47. 18. 73 2q., making it 6q.; then 3q. from 6q. £3. 2. 03 leaves 3q.; write down the 3q.; in order to increase the lower number equally with the upper, I add 1d. to the 7d., making it 8d.; then 8d. from 8d. leaves 0d.; write down 0d. I work the remaining columns in the same way, and find the required answer.

Ex. 2. From \$978.29 take \$678.93.

\$978.29 \$678.93 \$299.36 This example is worked in the same way as Simple Subtraction.

#### Ex. XXIII.

(1)	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	lbs. oz. drs. sc. grs. 27.8.6.2.15 17.9.3.1.19
(3)		mls. fur. per. yds. ft. 25 . 6 . 32 . 4 . 2 22 . 7 . 37 . 3 . 2
(5)	yds. qrs. nls. in. $106 \cdot 1 \cdot 2 \cdot 1$ $92 \cdot 3 \cdot 3 \cdot 1\frac{1}{2}$	c. yds. c. ft. c. in. (6) 325 . 22 . 101 296 . 25 . 386
(7)	ac, ro. per. yds. ft. in. 29 . 2 . 27 . 29 . 2 . 6 27 . 3 . 29 . 27 . 8 . 8	wks. dys.         hrs.         min.         se           (8)         7.5.6.36.17         6.6.20.46.20

COMPOUND MULTIPLICATION.

(9)	$\begin{array}{c} \pounds & s. & d. \\ 129 & 16 & 84 \\ 75 & 18 & 91 \\ \end{array}$	(10	cwt. qrs. 1bs. oz. drs. 7 . 2 . 15 . 6 . 12 6 . 3 . 24 . 10 . 14
(11)	\$2967.78 1898.89	(12) cords. c. 193 . 1 97 . 1	. ft. 07 (13) \$325.68 25 297.99
(14)	ac. ro. per. y 297.1.23.2 189.2,28.2	ds. ft. in. 2 . 1 . 101 2 <sup>1</sup> / <sub>4</sub> . 2 . 127	c. yds. c. ft. c. in. (15) 278 . 3 . 1127 198 . 8 . 1478
(16)	mls. fur. per. ye 117 . 0 . 27 . 4 89 . 7 . 38 . 4	ls. ft. in. 5 . 1 . 9 4 . 2 . 11	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
(18)	tons. cwt. qrs, 293.16.1.2 287.19.2.	lbs. oz. drs. 21.6.15 22.11.14	(19) yds. qrs. nls. in. 1209 . 1 . 1 . 1 1198 . 2 . 2 . 1‡
(20)	bu. pk. gal. qt. 268 . 2 . 1 . 1 197 . 3 . 1 . 3	. (21)	bu. pk. gal. qt. 19672 . 0 . 1 . 1 18998 . 3 . 1 . 3

## COMPOUND MULTIPLICATION.

47. COMPOUND MULTIPLICATION is the method of finding the amount of any proposed compound number, that is, of any number composed of different denominations, but all of the same kind, when it is repeated a given number of times.

RULE. Place the multiplier under the lowest denomination of the multiplicand.

Multiply the number of the lowest denomination by the multiplier, and find the number of units of the next denomination contained in this first product; if there be a remainder, write it down; for the second product, multiply the number of the next denomination in the multiplicand by the multiplier, and after adding to it the above-mentioned number of units, proceed with the result as with the first product.

Carry this operation through with all the different denominations of the multiplicand.

Multiplier not greater than 12.

. Ex. 1. Multi	ply £1. 14s. 9 <sup>3</sup> / <sub>4</sub> d. by 11.
$ \begin{array}{c}                                     $	$3q. \times 11 = 33q. = 8\frac{1}{4}d.;$ write down $\frac{1}{4}d.;$ then $9d. \times 11 + 8d. = 99d. + 8d. = 107d. = 8s.$ $11d.;$ write down $11d.;$ then $14s. \times 11 + 8s. = 154s. + 8s. = 162s. = \pounds 8. 2s.;$ write down $2s.;$ then $\pounds 1 \times 11 + \pounds 8 = \pounds 19;$ write down $\pounds 19.$
Ex. 2. Multij	ply \$27.78 by 9.
\$27.78 9 \$250.02	In this example we do the same as in Simple Multiplication, observing to place the point separating the dollars and cents in its proper place.

# Ex. XXIV.

(1)	£ s. d. 12 . 9 . 6 2	(2) <sup>1bs. o</sup>	z. drs. sc. 5.6.2 3	lbs. oz. (3) 18.6	dwt. grs. . 5 . 10 4
(4)	yds. qrs. nls. 27 . 3 . 3 5	(5) <sup>mls. f</sup>	ur. per. yds. 7 . 26 . 4 .	ft. 2 (6) 6	\$237.19 7
(7) <sup>c</sup>	wt. qrs. lbs. oz 16.0.17.0	. drs. mls. . 15 (8) 6 . . 8	fur. per. yds. 4 . 6 . 2 .	ft. in. 1.9 (9) 9	\$609.93 10
(10)	wks. dys. hrs. 7.5.18	min. . 16 	(11) 8c. ro	o. per. yds 3 . 29 . 20	ft. in. 1 108 12
(12)	£ *. 20 . 17 . 7 7	1. lbs. <sup>3</sup> / <sub>4</sub> (13) 74	oz. drs. s 11.5.2	c. bu 2 (14) 7 2	. pk. qt. , 3 . 1 3
(15)	dys. hrs. min. 2.3.59 10	(16) gal. 4554	qt. pt. 3.1 (17)	dys. hrs. 365.5.	min. sec. 48 . 57 12
(18)	£ s. d 73 . 17 . 8 11	2 (19)	ac. ro. per. 14.3.39 9	(20)	297.68 12

## COMPOUND MULTIPLICATION.

(21)	bu. pk. gal. 2782 . 2 . 1 9	(22) 7	8 <b>s</b> . 0 . 0 .	$\begin{array}{c} \overset{d.}{11\frac{1}{2}} \\ 12 \end{array}$ (23)	1bs. oz. 18.3	dwt. grs. . 14 . 5 12
(24)	\$917.75 8	(25)	£ . 17.15	<i>d.</i> • 0 <del>3</del> 9	(26)	\$1875.25 12
		(27) <sup>mls</sup>	s. fur. 4.3.	per. yds. 18.5 7		

If the Multiplier be a composite number, each of whose factors is less than 12, multiply by one of them, and the resulting product by another, and so on. The last product so obtained, is the required product.

Find the product of 2 cwt., 3 qr., 17 lbs. by 63.

cwt. qrs. lbs.

2.3.17The factors of 63 are 9 and 7. First, we<br/>multiply by 9 and the product we get by 7;<br/>which clearly is the same as multiplying 2<br/>cwt., 3 qr., 17 lbs. by 63.

Note. The same result is obtained, by 183.3.21 taking the factor 7 first, and then the 9.

	EX. XXV.
(1)	$ \underbrace{ \begin{array}{c} \text{ac. ro. per} \\ 56 \cdot 2 \cdot 9 \\ \underline{28} \\ \end{array} } \underbrace{ \begin{array}{c} \text{mls. fur. per.} \\ 27 \cdot 6 \cdot 9 \\ \underline{54} \\ 54 \\ \end{array} } \underbrace{ \begin{array}{c} \text{s. d.} \\ 19 \cdot 11 \cdot 4 \\ \underline{144} \\ \underline{144} \\ \end{array} } $
(4)	1bs. dwt. grs.       £       s. d.       yds. qr. nls. in.         21. 13. 17       (5)       17. 11. 84       (6)       27. 1. 3. 2         77       20       54
(7)	$cwt. qrs. lbs. oz. drs. 2.3.23.12.6$ $(8)$ $\begin{array}{c} \pounds & s. d. \\ 72.19.9\frac{3}{4} \\ 81 \end{array}$ $(9)$ $\$209.18$ $\underline{63}$ $\underline{81}$ $\underline{35}$
(10)	$ \begin{array}{c} \text{c.yds. c. ft. c. in.} \\ 17. 21, 57 \\ \underline{- 84} \\ \end{array} \begin{array}{c} \text{lbs. oz. dwt. grs.} \\ 15. 13 \\ \underline{49} \\ \end{array} \begin{array}{c} \text{ft. ft. s. d.} \\ 12 \\ \underline{42} \\ 88 \\ \underline{88} \\ 88 \end{array} $

### Ex. XXV.

(13)	dys, hrs. min. sec. 5.17.39.20 120	(14)	bs. oz. drs. sc. 74.11.5.2 84
(15)	lbs. oz. dwt. grs. 6 . 2 . 3 . 17 5382	(16)	$\begin{array}{c} \pounds & s. & d. \\ 13. & 7. & 4\frac{3}{4} \\ & & 275 \end{array}$
(17)	ac. ro. per. yds. ft. f 20.2.17.15.3.		fur. per. yds. ft. in. . 6 . 2 . 3 . 0 . 5 375
(19)	$ \begin{array}{c} \pounds & s. & d. \\ 2 & . & 6 & . & 8\frac{1}{2} \\ \hline & 900 \end{array} $ (20)	\$237.15 500	(21) bu. pk. gal. 10.2.1 800

When the Multiplier is not a Composite number and larger than 12, the easiest method will be to split the number into factors and parts:

Thus,  $29 = 4 \times 7 + 1$ ;  $19 = 6 \times 3 + 1$ ;  $39 = 12 \times 3 + 3$ . Ex. 1. Multiply £2579. 0s. 03d. by 2331. 2331 = 2000 + 300 + 30 + 1.  $=1000 \times 2 + 100 \times 3 + 10 \times 3 + 1.$  $=10 \times 10 \times 10 \times 2 + 10 \times 10 \times 3 + 10 \times 3 + 1$ d. £ 3579 8. 0.03 for 1 10 71 for 10 25790 . 0. 10 257900 . 6.  $3 \text{ for } 10 \times 10, \text{ or } 100$ 10 2579003 . 2 . 6 for  $100 \times 10$ , or 1000. 2 0 for  $1000 \times 2$ , or 2000. 5158006 . 5. 9 for £257900. 6s.  $3d. \times 3$ , or for 300. add 773700 . 18 .  $10\frac{1}{2}$  for £25790. 0s.  $7\frac{1}{2}d \times 3$ , or for 30. add 77370 . 1. 0% for 1. add 2579 . 0. 81 for 2000 + 300 + 30 + 1, or 2331. 6011656 . 5.

## COMPOUND DIVISION.

## Ex. XXVI.

(1)	cwt. qrs. 3.3.	lbs. oz. 21 . 5 89	(2) <sup>1bs.</sup>	oz. dwt. 2.3.5	grs. 17 463	(3)	£ .	s. d. 6 . 9 <u>1</u> 938
(4)	cwt. grs. 2.3.	1bs. oz. 23.6	drs. 7 527		(5)	£ .	s. 18 56	4. 91 51
		(6	lbs. oz 5) 15.2	drs. sc. . 3 . 2	grs. 7 712			

(7) If a man gets \$2.25 a day, how much will that be in 209 days?

(8) When wheat is selling for \$1.27 a bushel, how many dollars will a farmer get for a load of 52 bushels of wheat?

(9) A butcher had an ox weighing 1625 lbs., live weight, at 6 cents a pound how much will be have to pay altogether?

(10) A boiler-builder bought 29 boiler plates, each weighing 1 qr., 17 lbs., 8 oz., what was the weight of the whole of them?

(11) If the Government of Ontario sells one hundred thousand acres of wild land for forty cents an acre, how many dollars will it obtain for the whole?

## COMPOUND DIVISION.

48. COMPOUND DIVISION is the method of dividing a compound number, that is, a number composed of several denominations, but all of the same kind, into as many equal parts as the divisor contains units; and also of finding how often one compound number is contained in another of the same kind.

When the Divisor is a number either larger, or not larger than 12.

RULE. Place the numbers as in Simple Division; then find how often the divisor is contained in the highest denomination of the dividend; put this number down in the quotient; multiply as in Simple Division and subtract.

If there be a remainder, reduce that remainder to the next

inferior denomination, adding to it the number of that denomination in the dividend, and repeat the division.

Carry on this process through the whole dividend.

When the Divisor is less than 12.

Ex. 1. Divide £676. 19s. 91d. by 11.

When the Divisor is greater than 12 and not a Composite number, the work may stand thus:

Ex. 2. Divide £297. 4s. 8d. by 73.

By the Rule,

 $(73) \frac{\pounds}{297} \cdot 4 \cdot 8 (\pounds 4)$  $\frac{292}{5}$ 20 [add the 4s.]

73) 104 (1s. 73

31

 $\begin{array}{r}
 12 \text{ [add the 8d.]} \\
 73 \text{ )} \overline{380} \text{ (5d.} \\
 \underline{365} \\
 15
 \end{array}$ 

We first subtract £4 taken 73 times, *i.e.* £292 from £297. 4s. 8d., there remains £5. 4s. 8d.

Now £5. 4s. 8d. = 104s. 8d., from this we subtract 1s. taken 73 times, *i.e.* 73s. from 104s., there remains 31s.,  $\therefore$  there is 1s. in quotient.

31s. 8d. = 380d., from this we subtract 5d. taken 73 times, *i.e.* 365d., there remains 15d. over

...£4. 1s. 5d. goes 73 times in £297. 4s. 8d., and 15d. over.

.:. the Quotient is £4. 1s. 5d. and 15d. over.

When the Divisor is a Composite number greater than 12, we may divide as in Ex. 1, successively by each factor, and the last quotient so obtained will be the required quotient.

Ex. 3. Divide 975 mls., 3 fur., 24 per. by 56.

Since  $56 = 8 \times 7$ , the work may stand thus:

8	975 . 3 . 24	Note. The same result would be ob-
7	121 . 7 . 18	tained by dividing first by 7 and then
	17 3 14	0y 0.

## COMPOUND DIVISION.

63

## Ex. XXVII.

- (1)  $\pm 278.15s.8d.\div 5.$
- (2) 237 lbs., 5 oz., 6 dwt. ÷ 8.
- (3) 217 mls., 5 fur., 16 per., 2 yds. ÷ 9.
- (4) 115 yds., 2 qrs., 2 nls. ÷ 5.
- (5) 865 lbs., 9 oz., 2 sc., 10 grs. ÷ 6.
- (6)  $\pm 2078. 17s. 1 \pm d. \div 11.$
- (7) 67 tons, 13 cwt., 1 qr., 17 lbs .:- 27.
- (8) 976 ac., 2 ro., 19 per., 25 yds. ÷ 56.
- (9) 612 cwt., 17 lbs., 2 drs. ÷ 705.
- (10) 8627 mls., 6 fur., 2 yds. ÷ 1247.
- (11) 612 bu., 2 pks., 1 gal. 2 qts. ÷ 96.
- (12) £2851. 16s.  $4\frac{1}{2}d. \div 54$ .
- (13) 247 lbs., 10 oz., 7 drs., 1 sc. ÷ 57.
- (14) 200 mls., 3 fur., 6 per. ÷ 211.
- (15) 416 ac., 3 ro., 19 per., 7 yds. ÷ 318.
- (16) 614 tons, 2 cwt. 3 qrs. ÷ 564.
- (17) 917 c. yds., 9 c. ft., 100 c. in. ÷ 100.
- (18) 926 lbs., 5 oz., 3 drs., 2 sc. ÷ 212.
- (19) 3068 lbs., 8 dwt. ÷ 634.
- (20) £1914. 10s.  $5d. \div 758.$
- (21) £215. 12s.  $6\frac{1}{2}d. \div 317.$
- (22) 125 yrs., 127 dys., 16 hrs., 47 min. ÷ 397.
- (23) \$2267.84  $\div$  267.
- (24)  $$5693.75 \div 425.$

(25) If a person earned \$600 a year, how much is that a day? How much per day, omitting the Sundays?

Note. A year = 365 days.

(26) A farm of 57 acres is let for \$265.05, for a year; how much is that for an acre?

(27) A farmer sold 57 bushels of wheat for \$65.55; how much did he get for one bushel?

(28) The annual rent of a house is \$132; how much must be put aside every week so as to have the whole rent ready at the end of the year?

When the divisor and dividend are both compound numbers of the same kind.

RULE. Reduce both numbers to the same denomination. Divide as in Simple Division. The Quotient will be the answer required. Ex. 1. How often is 3s. 7d. contained in £8. 15s. 7d.?

38.	7d. £8. 1	5s. 7d.
12	20	Reason for the Rule.
43	175	$3s. 7d. = 43d., \pm 8. 15s. 7d. = 2107d.;$
	12	43d. subtracted 49 times from 2107d.
	2107	leaves no remainder.
	43)2107(49	1 ( Martin 1 and 1
	172	
	387	49 times is the answer.
	387	

Ex. 2. I employ twice as many men as women, the wages of the former are 3s. 6d. each, and of the latter 1s. 10d. each per day. The weekly wages amount to £23. 17s. How many men, and how many women do I employ?

 $\pounds 23. 17s. \div 6 = \pounds 3. 19s. 6d. = 954d. = am<sup>4</sup>. of daily wages.$  $Daily wages of 2 men and 1 woman = 3s. 6d. <math>\times 2 + 1s. 10d.$ = 8s. 10d. = 106d.

> 106)954(9 954

.:. there are 18 men and 9 women.

## Ex. XXVIII.

Divide,

- (1) £684. 7s. 6d. by £76. 0s. 10d.
- (2) £171. 1s. 101d. by £57. 0s. 71d.
- (3) 9 lbs., 9 oz., 3 dwt., 12 grs. by 5 dwt. 9 grs.
- (4) 4 mls, 1 fur., 2 yds. by 1 ml., 3 fur., 2 ft.
- (5) 6 cwt. 2 qrs. by 1 qr., 3 oz.
- (6) 12 lbs., 6 oz., 2 sc., by 1 lb., 6 oz., 2 sc., 10 grs.
- (7) 3 yds., 1 qr., 2 nls. by 1 qr., 2 nls.
- (8) 1 dy., 1 hr., 12 min. by 1 hr. 3 min.
- (9) 5 sq. per., 7 yds., 108 in. by 2 yds. 1 ft.
- (10) \$141.05 by \$2.17.
- (11) \$221 by \$2.21.

## 49. To reduce old Canadian to the Decimal Currency.

RULE. Multiply the pounds by 4, the product is dollars. Multiply the shillings by 20, the product is cents. Reduce the pence to farthings and add the given farthings, if any; then multiply by 5 and divide by 12, the quotient is cents.

The sum of these results is the answer required. How many dollars and cents in  $\pounds72$ . 198. 94d.?

 $\begin{array}{c} \pounds 1 = \$4, \dots \pounds 72 = \$72 \times 4 = \$288.00\\ 1s. = 20 \text{ cts.}, \dots 19s. = 19 \times 20 \text{ cts} = 3.80\\ 9\frac{1}{2}d. = 38q., \dots 38q. \times 5 \div 12 = 190 \div 12 = 15\frac{12}{\$291.951\$}\\ \hline\end{array}$ 

Therefore the required answer is \$291.9512.

## Ex. XXIX.

How many dollars and cents in

(1)	£25.	68.	3d.	(2)	£57.	198.	3d.
(3)	£207.	17s.	8d.	(4)	£153.	18s.	5d.
(5)	£217.	178.	0d.	(6)	£319.	15 <i>s</i> .	$7\frac{1}{2}d.$
(7)	£612.	198.	$11\frac{1}{4}d.$	(8)	£63.	98.	$9\frac{3}{4}d$ .
(9)	£912.	128.	6d.	(10)	£711.	58.	$5\frac{1}{2}d.$
(11)	£1117.	0s.	$7\frac{1}{2}d.$	(12)	£47.	78.	9d.
(13)	£2017.	68.	8d.	(14)	£75.	98.	$8\frac{1}{2}d.$
(15)	£37.	188.	$7\frac{1}{2}d.$	(16)	£87.	138.	9d.

50. To reduce dollars and cents to Halifax or old Canadian Currency.

RULE. Divide the dollars by 4, the quotient is pounds.

If there is any remainder bring it to cents and add the given cents if any; then divide by 20, the quotient is shillings.

If any cents are left, multiply them by 3 and divide by 5; the quotient is pence. By arranging these several quotients properly, the required answer is obtained.

How many pounds, shillings and pence in \$1279.122?

 $\begin{array}{c} 4 | \underline{1279.12_{\frac{1}{2}}} \\ \underline{5319} \text{ and } \underline{\$3} \text{ over.} \\ \end{array} \begin{array}{c} \$3 + 12_{\frac{1}{2}} \text{ cts.} = 300 \text{ cts.} + 12_{\frac{1}{2}} \text{ cts.} = 302 \text{ cts.} \\ \underline{312_{\frac{1}{2}}} \text{ cts.}; 312_{\frac{1}{2}} \text{ cts.} \div 20 = 15s. \text{ and} \\ 12_{\frac{1}{2}} \text{ cts.}; 312_{\frac{1}{2}} \text{ cts.} \times 3 \div 5 = 7_{\frac{1}{2}}d. \\ \end{array}$ Therefore the answer is £319. 15s.  $7_{\frac{1}{2}}d.$  The above is evidently correct; because  $\$4 = \pounds1$ , 20 cts. = 12d., 5 cts. = 3d.

## ARITIIMETIC.

### Ex. XXX.

How many pounds, shillings and pence m

(1)	\$217.25	(2)	\$327.55	(3)	\$17.35
(4)	\$84.50	(5)	\$75.95	(v)	\$125.373
(7)	\$867.871	(8)	\$1162.40	(9)	\$1393.621
(10)	\$1937.20	(11)	\$2220.29	(12)	\$3785.48

### Ex. XXXI.

#### MISCELLANEOUS EXAMPLES.

#### PAPER I.

(1) The population of the counties on the river St. Lawrence in 1861 was as follows: Leeds, thirty-five thousand seven hundred; Grenville, twenty-four thousand one hundred and ninety-one; Dundas, eighteen thousand seven hundred and seventy-seven; Stormont, eighteen thousand one hundred and twenty-nine; Glengarry, twenty-one thousand one hundred and eighty-seven. Find the total population of these five counties.

(2) By the census of 1848, the population of Montreal was fifty-five thousand one hundred and forty-six; of Toronto, twenty-three thousand five hundred and three; of Hamilton, nine thousand eight hundred and eighty-nine; of Ottawa, six thousand two hundred and seventy-five; of Kingston, eight thousand three hundred and sixty-nine; of London, four thousand five hundred and eighty-four. Find the whole population of those cities.

(3) Add, one hundred thousand, two hundred and twentynine thousand seven hundred and thirteen, fifty-eight thousand seven hundred and five, six hundred and twelve thousand five hundred and seventeen, nine hundred and ninety-nine thousand nine hundred and ninety-nine, eight hundred and thirty-three thousand seven hundred and nineteen, seven hundred and sixty-eight thousand three hundred and nine, fifty thousand and fifty.

(4) Add, five thousand and five, seven thousand and eighteen, seventeen thousand nine hundred and fifteen, twentyeight thousand seven hundred and nineteen, nine thousand and twelve, eight hundred and seven thousand five hundred and twelve, seven hundred and seventeen thousand and seventeen, ninety-three thousand five hundred and two, two hundred and twelve thousand six hundred and seven.

## (5) How many miles in 178006 inches?

(6) In 1848 the value of the imports into Canada was \$8375180.20; in 1861, the value of the imports was \$43054836; the population at the former date was 1493332, at the latter 2506755. Find lst., the value of the imports for each person in 1848 and in 1861, and 2nd., the difference between these values.

### PAPER II.

(1) What is the price of 818 bushels of wheat at 8s.  $10\frac{1}{2}d$ . per bushel?

(2) A farmer sold 67 bushels of wheat at \$1.62 a bushel; bought a suit of clothes for \$18, 82 yards cotton at  $13\frac{1}{2}$  cents a yard, a stove for \$16. How much was left of the price of the wheat?

(3) If a Government was to divide 72812 acres equally among 397 discharged soldiers, how much would each receive?

(4) A farmer brought 160 bushels of wheat to mill when wheat was worth \$1.60 per bushel, and in exchange got 27 barrels of flour. How much was he charged for the flour per barrel?

(5) A merchant has a piece of cloth containing  $42\frac{1}{2}$  yards, worth 6s.  $6\frac{1}{2}d$ . a yard. How many dresses of  $8\frac{1}{2}$  yards each can be made out of it, and what will each cost?

(6) A farmer sold in the Toronto market 618 barrels of flour for £1. 13s. 9d. per barrel; and bought 84 yards of cotton at 17 cents a yard, 5 lbs. tea at 3s. 9d. a lb., 2 tons of coal at £1. 15s. per ton, 8 sheep at £2. 11s. 9d. each, 15 head of cattle at £12. 19s. 9d. each. How much can he deposit in a bank allowing that he takes \$50 home with him?

#### PAPER III.

(1) In one year there were coined in the British mint 203761 pounds of gold, value £9520732. 14s. 6d. Required the value of each pound?

(2) Three persons bought a ship for \$63000; the first taking one share, the second three, and the third five. How much do they severally pay?

(2) If a contribution of £354. 11s. 6d. is made up in equal shares by 26 men, how much must each give ?

(4) What is the 29th part of 10 ac., 2 ro., 7 per., 2 yds?

(5) Divide 300 tons, 15 cwt., 3 qrs., equally among 347 men. How much will each get?

(6) Soldiers marching in quick time, make 110 steps in a minute, each step 2 ft. 6 in. long. In what time would a company of soldiers march 20 miles in quick time, allowing half an hour for rest?

#### PAPER IV.

(1) Add together £6. 17s. 6d., \$30.27, £3. 12s. 9d. \$75.83; giving your answer in decimal currency.

(2) Three boys went out together to fish, the first caught eight, the second as many and three more, the third as many as his two comrades all but one. How many did each of the last two boys catch?

(3) Three boys, Thomas, William, and Alexander, had between them 6 cents; Thomas had one, William two, and Alexander three; they bought fifty-four marbles with their money. How many ought each boy to get?

(4) Four men went out one night to fish, borrowing both boat and nets. A man was to have 4 shares of the catch as often as the owner of the net was to have one; but, a man was to have only two shares as often as the owner of the boat had one. The catch was four barrels of herrings. What was each party's share in dozens; each barrel containing 38 dozens of herrings?

(5) It is found by observation that in each square inch of the human skin there are about 1000 pores; and the surface of the body of a middle sized man contains about 2304 square inches, or 16 square feet. Required, the number of pores in the surface of such a body, 999 being supposed to be contained in each square inch?

(6) The sum of two numbers is S4S89; the difference between them is S89. What are the numbers?

### PAPER V.

(1) Find the product of 72678397 and 86073?

(2) The quotient is 73697; the remainder 3687; the divisor 11689. Find the dividend?

(3) The minuend is twenty-seven thousand eight hundred and twelve; the difference, fifteen thousand nine hundred and eight. Find the subtrahend?

(4) There are seven addends all equal; their sum is eighty-nine thousand two hundred and sixty-four. Find one of them?

(5) In the census of 1861, Rutland contained twenty-two thousand nine hundred and eighty-three inhabitants; Northamptonshire, ninety-six thousand eight hundred and one; Huntingdonshire, sixty-four thousand one hundred and eighty-three; Leicestershire, ninety-one thousand three hundred and eight; Nottinghamshire, one hundred and ninety thousand and sixty. What was the sum of the population of the above five counties in 1861?

(6) During the Crimean war, out of the French army there were killed in action or missing ten thousand two hundred and forty; drowned in a wreck, seven hundred and four; died of various diseases before the battle of Alma, eight thousand and eighty-four; died of disease before Sebastopol, four thousand three hundred and twelve; died in hospitals, &c., seventy-two thousand two hundred and forty-seven. How many were lost attogether?

### PAPER VI.

(1) In 1861 the population of Edinburgh was 160302; of Glasgow, 168795 more than that of Edinburgh; of Aberdeen 71973; of Inverness, 24527 more than that of Aberdeen. What was the total population of all these places in 1861?

(2) The paid up capital of each of the following Banks doing business in Ontario, is: of the Bank of Montreal, \$6000000; Bank of British North America, \$4866666; of Quebec Bank, \$1467750; of Bank of Toronto, \$800000; of Ontario Bank, \$1909640; of Royal Canadian Bank, \$590382; of Merchants' Bank, \$862033. Find the total amount of the paid up capital of the above named Banks?

(3) The amount of revenue, from the named sources during 1866, was as follows: Customs, \$7328146.68; Excise, \$1888576.76; Postage, \$621936.42; Public-works, \$417474; Education, \$66554; Common School Fund, \$122142.77. Find the whole revenue from these sources?

(4) A person has \$975. He buys a team for \$375, a wagon for \$82, a plough for \$16, a stove \$16, a reaping machine for \$153, 12 sheep for \$8 each, 2 cows \$25 each, 3 pigs \$6 a piece, pays his servantman 3 months' wages at \$20 a month, and the rest he lays out in flour at \$1.75 per 100 pounds. How many pounds of flour will he have?

(5) Among 635 men divide equally 86895 acres.

(6) How many inches in 10 mls., 3 per., 4 yds.?

## SECTION III.

## GREATEST COMMON MEASURE.

51. A MEASURE of any given number is a number which will divide the given number exactly, *i. e.* without a remainder.

Thus, 2 is a measure of 6, because 2 is contained 3 times exactly in 6.

52. A MULTIPLE of any given number is a number which contains it an exact number of times. Thus, 6 is a multiple of 2.

53. A COMMON MEASURE of two or more given numbers is a number which will divide each of the given numbers exactly. Thus, 3 is a common measure of 18, 27, and 36.

The GREATEST COMMON MEASURE (G. C. M.) of two or more given numbers, is the greatest number which will divide each of the given numbers exactly. Thus, 9 is the greatest common measure of 18, 27, and 36.

54. To find the greatest common measure of two numbers.

RULE. Divide the greater number by the less.

If there be a remainder, divide the first divisor by it.

If there be still a remainder, divide the second divisor by this remainder, and so on; always dividing the last preceding divisor by the last remainder, till nothing remains.

The last divisor will be the greatest common measure required.

Ex. Find the G. C. M. of 144 and 240.

By the Rule,

144)240(1

144

96) 144 (1 bringing down last divisor 144 for a dividend. 96

48) 96 (2 ..... 96 96 ... 48 is g. с. м. required.
# LEAST COMMON MULTIPLE.

# Ex. XXXII.

Find the G. C. M. of

(1)	8 ar	nd 18.	(2)	6 an	d 15.	(3)	4 and 22.	
(4)	16 a	and 28.	(5)	20 a	nd 32.	(6)	24 and 39.	
(7)	26 a	nd 44.	(8)	30 a	nd 42.	(9)	36 and 56.	
(10)	46 a	and 116.	(11)	58 a	nd 174.	(12)	315 and 378.	
(13)	366	and 128.	(14)	180	and 210	). (15)	310 and 630.	
(16)	121	6 and 424.	(17)	127	and 445	5. (18)	6408 and 72	64.
	(19)	3042 and	3094.		(20)	7040 a	and 7392.	
	(21)	1441 and	1572.		(22)	46436	and 23025.	
	(23)	21168 and	1 20469	24.	(24)	97482	and 29579.	
	(25)	828597 an	nd 738	140.	(26)	32633	7 and 737800.	

# LEAST COMMON MULTIPLE.

55. A COMMON MULTIPLE of two or more given numbers is a number which will contain each of the given numbers au exact number of times. Thus, 144 is a common multiple of 3, 9, 18, and 24.

The LEAST COMMON MULTIPLE (L. C. M.) of two or more given numbers is the least number which will contain each of the given numbers an exact number of times. Thus, 72 is the least common multiple of 3, 9, 18, and 24.

56. When the least common multiple of several numbers is required, the most convenient practical method is that given by the following Rule.

RULE. Arrange the numbers in a line from left to right, with a comma placed between every two.

Divide those numbers which have a common measure by that common measure, and place the quotients so obtained and the undivided numbers in a line beneath, separated as before.

Proceed in the same way with the second line, and so on with those which follow, until a row of numbers is obtained in which there are no two numbers which have any common measure greater than unity.

Then the continued product of all the divisors and the numbers in the last line will be the least common multiple required.

Note. It will in general be found advantageous to begin

with the lowest prime number 2 as a divisor, and to repeat this as often as can be done; and then to proceed with the prime numbers 3, 5, &c., in the same way.

Ex. 1. Find the L. C. M. of 10, 12, and 16. By the Rule.

2	10,	12,	16	$10=2\times5$ , $12=2\times2\times3$ , $16=2\times2\times2\times2$ .
2	5,	6,	8	$2 \times 5$ for 10.
	5,	3,	4	$2 \times 5 \times 2 \times 3$ for 10 and 12. $2 \times 5 \times 2 \times 3 \times 2 \times 2$ for 10, 12, and 16.

.:. L. C. M. =  $2 \times 2 \times 5 \times 3 \times 4 = 240$ .

Note. The process of finding the L. C. M. may often be shortened by striking out in the same line every number which exactly measures any other number in that line.

Ex. 2. Find the L. C. M. of 9, 14, 16, 18, 24, 36, and 38.

2	\$,14,16,1	8,24,36,38	Every multiple of 36 must be
2	7, 8,	12, 18, 19	a multiple of 9 and of 18;
2	7, 4,	6, 9, 19	same reason strike out 3 in the
	7, 2,	\$, 9, 19	4th line.

 $\therefore$  L. C. M. = 2 × 2 × 2 × 7 × 2 × 9 × 19 = 19152.

# Ex. XXXIII.

Find the L. C. M. of

(2) 8, 9, and 12. (1)2, 4, and 10. (4) 20, 28, and 36. 12, 16, and 18. (3) (5) 16, 24, and 30. (6) 24, 56, and S4. 6, 33, 24, and 32. (7) 15, 25, and 105. (8) 7, 21, 6, 14, and 25. 7, 8, 9, 10, and 12. (10)(9) 24, 28, 36, 22, and 16. 2, 5, 45, 15 and 25. (11)(12)15, 20, 24, 21, and 35. 9, 4, 8, 15, and 27. (14)(13)(15) 4, 5, 7, 8, 15, 21, and 30. 2, 7, 9, 13, 15, 52, and 63. (16)(17) 3, 7, 21, 11, 77, and 198. 100, 56, 35, 125, and 150. (18)(19) 22, 55, 19, 15, 95, and 133. (20) 48, 64, 27, 33, 110 and 165.

#### FRACTIONS.

# SECTION IV.

# FRACTIONS.

57. Let unity be represented by the line AB, which we will consider to be one yard in length.

Suppose AB to be divided into 3 equal parts AD, DE, EB; then one of such parts  $AD \stackrel{A}{\longrightarrow} D \stackrel{E}{\longrightarrow} B \stackrel{F}{\longrightarrow} G \stackrel{C}{\longrightarrow} G$ is a foot or one-third part of the yard, and it is denoted thus  $\frac{1}{3}$  (read *two-third*); two of them AE, or two feet, thus  $\frac{2}{3}$  (read *two-thirds*); three of them AB, or three feet, or the whole yard, thus  $\frac{3}{3}$  or 1.

If another equal portion BF of a second yard BC, divided in the same manner as the first, be added, then AF, or four feet, is denoted thus  $\frac{4}{3}$ ; and so on.

Such expressions, representing any number of the equal parts of a unit, *i. e.* of a quantity which is denoted by 1, are called BROKEN NUMBERS OR FRACTIONS.

5S. A FRACTION denotes one or more of the equal parts of a unit; it is expressed by two numbers placed one above the other with a line between them; the lower number is called the DENOMINATOR (Den<sup>r</sup>.), and shews into how many equal parts the unit is divided; the upper is called the Nu-MERATOR (Num<sup>r</sup>.), and shews how many of such parts are taken to form the fraction.

59. A Fraction also represents the quotient of the num. by the den.

Thus  $\frac{2}{3} = 2 \div 3$ ; for we obtain the same result, whether

we divide one unit, AB or 1 yard, into three equal parts AD, DE, EB, each = 1 ft. or 12 in., and take two of such parts AE(represented by  $\frac{2}{3}$ ),= 12 in.  $\times 2=24$  in., or divide 2 units, ACor 2 yards, into three equal parts, AE, EF, FC, each = 2 ft. or 24 in., and take one of such parts AE; which is equal to  $\frac{1}{3}$  raise part of AC or 2 units, or =  $2 \div 3$ . Hence  $\frac{2}{3}$  and  $2 \div 3$  have the same meaning.

60. When fractions are denoted in the manner above explained, they are called VULGAR FRACTIONS.

61. Fractions, whose den<sup>re</sup>. are composed of 10, or of 10 multiplied by itself any number of times, are called DECI-MAL FRACTIONS, or DECIMALS.

# VULGAR FRACTIONS.

62. In treating of the subject of Vulgar Fractions, it is usual to make the following distinctions :

(1) A PROPER FRACTION is one whose num<sup>7</sup>. is less than the den<sup>7</sup>.; thus  $\frac{3}{4}$ ,  $\frac{4}{5}$ ,  $\frac{6}{7}$ , are proper fractions.

(2) AN IMPROPER FRACTION is one whose num'. is equal to or greater than the den'.: thus,  $\xi$ ,  $\xi$ ,  $\xi$  are improper fractions.

(3) A SIMPLE FRACTION is one whose num'. and den'. are simple integer numbers; thus,  $\frac{1}{2}$ ,  $\frac{4}{3}$  are simple fractions.

(4) A MIXED NUMBER is composed of a whole number and a fraction; thus  $5\frac{1}{4}$ ,  $7\frac{2}{4}$  are mixed numbers, representing respectively 5 units, together with  $\frac{1}{6}$  th of a unit; and 7 units, together with  $\frac{2}{6}$  ths of a unit.

(5) A COMPOUND FRACTION is a fraction of a fraction; thus  $\frac{1}{2}$  of  $\frac{3}{4}$ ,  $\frac{5}{6}$  of  $\frac{7}{10}$  of  $\frac{7}{10}$ , are compound fractions.

(6) A COMPLEX FRACTION is one which is either a fraction of a mixed number in one or both terms of the fraction;

thus,  $\frac{2}{5}$   $\frac{2\frac{1}{2}}{2}$   $\frac{3}{2}$   $\frac{2\frac{1}{7}}{2}$   $\frac{2}{3}$  of  $\frac{1}{2}$  are complex fractions.

5' 3' 42' 51' 21

63. It is clear from what has been said, that every whole number or integer may be considered as a fraction whose den<sup>7</sup>. is 1; thus,  $5 = \frac{2}{3}$ , for the unit is divided into 1 part comprising the whole unit, and 5 of such parts, that is 5 units, are taken.

64. To multiply a fraction by a whole number.

RULE. Multiply the numerator by the whole number.

 $\frac{2}{5} \times 2 = \frac{2 \times 2}{5} = \frac{4}{5}$  For in  $\frac{2}{5}$  and  $\frac{4}{5}$ , the unit is divided into the equal parts, and twice as many parts are taken in  $\frac{4}{5}$  as are taken in  $\frac{2}{5}$ .

#### Ex. XXXIV.

Multiply (1)  $\frac{2}{7}$  and  $\frac{17}{107}$  each separately by 2, 3, 5, 7, 9, and 12; and (2)  $\frac{63}{54}$  and  $\frac{95}{107}$  each separately by 6, 8, 11, 106 and 157.

# VULGAR FRACTIONS.

# 65. To divide a fraction by a whole number.

RULE. Multiply the denominator by the whole number.  $\frac{2}{5} \div 2 = \frac{2}{5 \times 2} = \frac{2}{10}$ . The value of each part in  $\frac{2}{5}$  is twice as large as the value of each part in  $\frac{2}{10}$ ; but the same number of parts are taken in each,  $\therefore \frac{2}{5}$  is twice as large as  $\frac{1}{10}$ , or  $\frac{2}{5} \div 2 = \frac{2}{10}$ .

# Ex. XXXV.

Divide (1)  $\frac{3}{4}$  and  $\frac{7}{4}$  each separately by 2, 3, 5, 6, 9, and 12; and (2)  $\frac{16}{4}$  and  $\frac{77}{4}$  each separately by 3, 5, 11, 56, and 100.

66. If the numerator and denominator of a fraction be both multiplied, or both divided, by the same number, the value of the fraction will not be altered.

 $\frac{3}{4} = \frac{3 \times 2}{4 \times 2} = \frac{6}{3}$ Since  $8 = 4 \times 2$ , two of the parts in  $\frac{6}{3}$  are equivalent to one of the parts in  $\frac{6}{4}$ ; but since  $6 = 3 \times 2$ , there are twice as many parts taken in  $\frac{6}{3}$  as there are in  $\frac{2}{3}$ , therefore  $\frac{3}{4} = \frac{6}{3}$ . In figure, Art. 57, *AE* represents either  $\frac{1}{3}$ rd or  $\frac{2}{3}$ ths of *AC*.

67. Hence it follows that a whole number may be converted into a vulgar fraction with any required den<sup>1</sup>, by multiplying the number by the required den<sup>1</sup> for the num<sup>1</sup>. of the fraction, and placing the required den<sup>1</sup> underneath.

For  $5 = \frac{5}{1}$ , and to convert it into a fraction with a den<sup>r</sup>, 6

or 17, we have  $5 = \frac{5}{1} = \frac{5 \times 6}{1 \times 6} = \frac{30}{6}$ ; also  $5 = \frac{5}{1} = \frac{5 \times 17}{1 \times 17} = \frac{85}{17}$ 

#### Ex. XXXVI.

Reduce (1) 3, 5, 8, 15, to fractions with den<sup>10</sup>. 2, 9, and 13; and (2) 9, 12, 17, 37, to fractions with den<sup>10</sup>. 8, 10, and 57.

68. To represent an improper fraction as a whole or mixed number.

RULE. Divide the numerator by the denominator.

If there be no remainder, the quotient will be a whole number.

If there be a remainder, put down the quotient as the integral part, and the remainder as the num<sup>7</sup>. of the fractional part, and the given den<sup>7</sup>. as the den<sup>7</sup>. of the fractional part.

**Ex.** Reduce  $\frac{24}{4}$  and  $\frac{24}{5}$  to whole or mixed numbers.

By	the	Rule,									
	24	-6	For	24	4 ×	6	6				
	4	-0.	ror	$\frac{-}{4}$	4×	1	- (Art	5. 60)	= 6.		
	24			24	20 -	+ 4	20	4		4	
	5	$=4\frac{4}{5}$ .	For	-==		=	= - +	+ -= =	=4 +	-=	= 47.
	0			0	e	,	9	9		9	

#### Ex. XXXVII.

Express the following improper fractions as mixed or whole numbers:

(1)	82.	(2)	52.	(3)	13.	(4)	16.	(5)	19.
(6)	47.	(7)	69.	(8)	76	(9)	<u>91</u> 13.	(10)	112
(11)	$\frac{231}{27}$ .	(12)	804	(13)	1000.	(14)	$\frac{26540}{260}$ .	(15)	1718

69. To reduce a mixed number to an improper fraction.

RULE. Multiply the whole number or integer by the denominator of the fraction, and to the product add the numerator of the fractional part.

The result will be the required num<sup>1</sup>, and the den<sup>1</sup>. of the fractional part the required den<sup>1</sup>.

Ex. Convert  $3\frac{3}{4}$  into an improper fraction. By the Rule,

# $3\frac{3}{4} = \frac{3 \times 4 + 3}{4} = \frac{12 + 3}{4} = \frac{15}{4}.$ For $3\frac{3}{4} = \frac{3}{1} + \frac{3}{4} = \frac{3 \times 4}{1 \times 4} + \frac{3}{4} = \frac{12}{4} + \frac{3}{4} = \frac{12 + 3}{4} = \frac{15}{4}.$

#### Ex. XXXVIII:

Reduce the following mixed numbers to improper fractions:

(1)	11.	(2) 21	z. (3)	11.	(4)	17흫.	(5) 12	25
(6)	20317.	(7)	$2\frac{11}{65}$ .	(8)	297.	(9)	$704_{126}^{12}$ .	
(10)	900 31	(11)	5-70.	(12)	$53\frac{37}{03}$ .	(13)	$21_{\frac{3}{1250}}$ .	
(14)	$148_{465}^{237}$	(15)	$13\frac{1080}{2160}$ .	(16)	25239	(17)	197 3084	

70. To reduce a compound fraction to its equivalent simple fraction.

RULE. Multiply the several numerators together for the numerator of the simple fraction, and the several denominators together for its denominator. Ex. 1. Convert  $\frac{2}{3}$  of  $\frac{5}{5}$  into a simple fraction. By the Rule,

$$\frac{2}{3} \text{ of } \frac{5}{6} = \frac{2 \times 5}{3 \times 6} = \frac{10}{18}.$$
  
For  $\frac{2}{3} \text{ of } \frac{5}{6} = twice \frac{1}{3} \text{ of } \frac{5}{6} = twice \frac{5}{6} \div 3 = twice \frac{5}{18} \text{ (Art. 65)}$ 
$$= \frac{5 \times 2}{18} \text{ (Art. 64)} = \frac{10}{18}.$$

Note 1. Before applying the above Rule, mixed numbers must be reduced to improper fractions.

Note 2. In reducing compound fractions to simple ones, we may strike out from *any* num<sup>r</sup>. and *any* den<sup>r</sup>. such factors as are common to both; for this is in fact simply dividing the num<sup>r</sup>. and den<sup>r</sup>. of a fraction by the same number. (Art. 66.)

Ex. 2. Reduce  $\frac{3}{5}$  of  $2\frac{1}{17}$  of  $1\frac{1}{15}$  to a simple fraction.  $\frac{3}{5}$  of  $2\frac{1}{12}$  of  $1\frac{1}{15} = \frac{3}{5}$  of  $\frac{25}{12}$  of  $\frac{16}{15} = \frac{3 \times (5 \times 5) \times (4 \times 4)}{5 \times (3 \times 4) \times (3 \times 5)}$ 

 $\frac{3 \times 5 \times 5 \times 4 \times 4}{5 \times 5 \times 4 \times 3 \times 5} = \frac{4}{3}$ , dividing num<sup>r</sup>. and den<sup>r</sup>. by 3, 5, 5, 4, factors common to both.

Ex. XXXIX.

Reduce the following compound fractions to simple ones :

(1)	울 of \$.	(2)	ŧ of 1₽.		(3)	3 of 21.
(4)	3 of 3.	(5)	§ of 2§.		(6)	3 of 11.
(7)	182 of 57	of 10.	(8)	112 of	83.	

(9)	5 of 2	<sup>1</sup> / <sub>3</sub> of 9.	(10) $\frac{4}{7}$ of $3\frac{3}{4}$ of $3\frac{1}{2}$ .	•
111	K . C 2		2. 892. 83. 312. 8 (01)	÷.

(11)  $g \text{ of } \frac{1}{21} \text{ of } \frac{23}{5} \text{ of } \frac{1}{45}$ . (12).  $\frac{1}{24} \text{ of } \frac{45}{5} \text{ of } \frac{6}{57} \text{ of } \frac{6}{11} \text{ of } \frac{7}{53}$ . (13)  $\frac{1}{21} \text{ of } \frac{2}{2} \text{ of } \frac{5}{7} \text{ of } 10\frac{1}{2}$ . (14)  $\frac{7}{4} \text{ of } 12\frac{1}{2} \text{ of } \frac{4}{5} \text{ of } \frac{3}{5} \text{ of } \frac{3}{5} \text{ of } 9$ .

(15)  $\pi_{1}^{5}$  of  $\frac{7}{4}$  of  $\frac{3}{6}$  of  $\frac{9}{6}$  of  $\frac{9}{3}$  of  $\frac{3}{3}$  of 2 of  $\frac{9}{3}$ .

(10) 18 01 3 01 10 01 4 01 10 01 2 01 27.

(16)  $\frac{5}{7}$  of  $\frac{3}{7}$  of  $\frac{6}{7}$  of  $70\frac{2}{9}$  of  $\frac{3}{40}$  of  $1\frac{7}{11}$  of 147.

71. A fraction is in its LOWEST TERMS, when its numerator and denominator are FRIME to each other.

72. To reduce a fraction to its lowest terms.

RULE. Divide the numerator and denominator by their greatest common measure.

Ex. Reduce  $\frac{176}{484}$  to its lowest terms.

By the Rule, find the G. C. M. of 176 and 484. 176 ) 484 ( 2 352

132)176 132	2 (1	For $\frac{176}{484}$ =	$=\frac{44\times4}{44\times11}=$	$=\frac{4}{11}$ (Art. 60	ö.)
44 4) 176 ( 4 176	$ \begin{array}{r}132(3)\\132\\\overline{44})484(1)\\44\end{array} $	n			•
	44 44 44	fractio	n in its lo	west terms :	$=\frac{4}{11}$ .

# Ex. XL.

Reduce each of the following fractions to its lowest terms:

(1)	24.	(2)	10.	(3)	$\frac{14}{21}$ .	(4)	30 48.
(5)	28	(6)	<u>64</u> 84.	(7)	$\frac{77}{121}$ .	(8)	48 272.
(9)	1428 2652.	(10)	1408	(11)	875	(12)	1690 2600·
(13)	837 2268.	(14)	6006 8008	(15)	805	(16)	<u>9504</u> 10692.
(17)	23111 33769.	(18)	30599 271469.	(19)	5170 8734.	(20)	1236
(21)	285714	(22)	10395 16819	(23)	7040 7392	(24)	11385 16335.

To reduce fractions to equivalent ones with a common 73. denominator.

RULE. Find the least common multiple of the denominators; this will be the common denominator.

Then divide the common multiple so found by the denominator of each fraction, and multiply each quotient so found into the numerator of the fraction which belongs to it for the new numerator of that fraction.

Note. If the given fractions be in their lowest terms, the above rules will reduce them to others having the least common den<sup>r</sup>. : if the *least* common den<sup>r</sup>. be required, the given fractions should be reduced to their lowest terms before the rule is applied.

Ex. 1. Reduce 11, 17, and 11 to equivalent fractions with a common denominator.

# VULGAR FRACTIONS.

By the Rule, 12  $|\frac{42}{2}, \frac{24}{3}, \frac{36}{3}, \dots$  L. C. M. =12 × 2 × 3=72. ... the fractions become =  $\frac{11 \times 6}{12 \times 6} = \frac{66}{72}$  (since 72 ÷ 12=6), and  $\frac{17 \times 3}{24 \times 3} = \frac{51}{72}$  (since 72 ÷ 24=3), and  $\frac{31 \times 2}{36 \times 2} = \frac{62}{72}$  (since 72 ÷ 36=2),

. the required fractions are  $\frac{66}{72}$ ,  $\frac{51}{72}$ , and  $\frac{62}{72}$ .

Note. If the den<sup>m</sup>, have no common measure, the work will be more quickly done, by multiplying each num<sup>r</sup>. into all the den<sup>m</sup>, except its own, for a new num<sup>r</sup>. for each fraction, and all the den<sup>m</sup>. together for the common den<sup>r</sup>.

Ex. 2. Reduce  $\frac{2}{3}$ ,  $\frac{3}{7}$ , and  $\frac{5}{7}$  to equivalent fractions with a common den<sup>r</sup>.

L. C. M. Of	f the denra.	$=3 \times 5 \times$	7 = 105.			
· fronts -	$2 \times 5 \times 7$	$3 \times 3 \times 7$	5×3×5	70	63	75
Iract, -	$\overline{3 \times 5 \times 7}$	$\overline{5 \times 3 \times 7}'$	$7 \times 3 \times 5$	105'	105	105

# Ex. XLI.

Reduce the fractions in each of the following sets to equivalent fractions, having the least common den<sup>r</sup>.

(1) <sup>8</sup> / <sub>4</sub> and <sup>8</sup> / <sub>6</sub> .	(2) \$	and <del>3</del> .	(3) <sup>3</sup> / <sub>4</sub> a	nd <del>7</del> .
(4) 3 and 5.	(5) $\frac{11}{16}$	and 21.	(6) $\frac{11}{12}$ a	and 27.
(7) $\frac{7}{10}$ and $\frac{183}{200}$ .	$(8) \frac{11}{28}$	$\frac{3}{6}$ and $\frac{527}{960}$ .	(9) $\frac{4}{5}, \frac{1}{1}$	1/2, and 3/0.
(10) $\frac{3}{16}, \frac{8}{21}$ , ar	1d 5.	(11)	7, 11, an	d 33.
$(12) \frac{7}{9}, \frac{8}{11}, \frac{18}{15},$	and 17.	(13)	$\frac{13}{14}, \frac{35}{36}, \frac{14}{15}$	, and 48.
$(14)$ $\frac{7}{12}, \frac{17}{30}, \frac{17}{13}$	, 15, and	75. (15)	$\frac{13}{25}, \frac{27}{32}, \frac{7}{12}$	, and 15.
(16)	9 13 18, 3	7 18 23	and 53.	
(17) 3, 4, 3,	and 14.	(18)	) 3, 5, 7,	and 9.
$(19) \frac{2}{3}, \frac{5}{6}, \frac{7}{8}, .$	, and 3.	(20)	$) \frac{2}{3}, \frac{4}{5}, \frac{1}{2},$	and 3.
74 Whonever		on has to 1	he made h	atmaan for

74. Whenever a comparison has to be made between fractions, in respect of their magnitudes, they must be reduced to equivalent ones with a common den<sup>\*</sup>.; because then we shall have the unit divided, in the case of each fraction so obtained, into the same number of equal parts; and the respective num<sup>\*\*</sup>. will shew us how many of such parts are

taken in each case, or which is the greatest fraction, which the next, and so on. Ex. Which is the greatest, and which the least of the  $11 \times 4$   $12 \times 3$   $10 \times 5$  11 + 4, fractions  $5 \times 9$   $4 \times 10$   $6 \times 8$  5 + 944 9 25 15 The fract<sup>ns</sup>. in their lowest terms are  $\frac{1}{45}$ 10 24' and 14. L. C. M. of the den".==2520. 2464  $9 \times 252$  $44 \times 56$ 2268... the fractions become  $\overline{45 \times 56}$  or  $\overline{2520}$   $\overline{10 \times 252}$  or  $\overline{2520}$  $25 \times 105$ 2625  $15 \times 180$ 2700 $\overline{24 \times 105}$  or  $\overline{2520}$ ,  $\overline{14 \times 180}$  or  $\overline{2520}$  $12 \times 3$ 11 + 4 $\therefore \frac{5}{5+9}$  is the greatest, and  $\frac{1}{4 \times 10}$  the least.

#### Ex. XLII.

Compare the values of

- (1)  $\frac{2}{3}$  and  $\frac{4}{5}$ . (2)  $\frac{7}{9}$  and  $\frac{9}{12}$ . (3)  $\frac{17}{24}$  and  $\frac{19}{26}$ .
- (4)  $\frac{7}{5}$ ,  $\frac{5}{8}$ , and  $\frac{11}{14}$ . (5)  $\frac{15}{42}$ ,  $\frac{22}{49}$ , and  $\frac{43}{83}$ . (6)  $\frac{53}{80}$ ,  $\frac{63}{90}$ , and  $\frac{57}{84}$ .
- (7)  $\frac{2}{7}$  of  $\frac{5}{7}$ ,  $\frac{1}{2}$  of  $\frac{2}{7}$ , and  $7\frac{8}{7}$ . (8)  $\frac{11}{16}$ ,  $\frac{17}{20}$ ,  $\frac{21}{26}$ , and  $\frac{29}{36}$ .
- (9)  $\int_{1}^{6} \text{rof} \frac{1}{18} \text{of} 7\frac{1}{4}, 4\frac{1}{2} \text{of} \frac{2}{5}, \frac{1}{5} \text{of} 7\frac{1}{2} \text{of} 11, \text{ and } \frac{3}{5} \text{of} 4\frac{1}{5} \text{of} \frac{1}{2} \text{of} 14, \frac{7}{17}.$
- (10)  $\frac{\$\$}{12} \frac{\$}{61} \circ f_{1\frac{2}{28}}^{\$.5}$ ,  $\frac{15}{12} \circ f_{\frac{2}{8}}^{\$.5} \circ f_{\frac{1}{8}\frac{1}{6}}^{\$.5} \circ f_{\frac{1}{8}\frac{1}{6}}^{\$.5} \circ f_{\frac{1}{8}\frac{1}{6}}^{\$.5} \circ f_{\frac{1}{28}}^{\$.5}$ .

Which is the greater.

- (11) § of a yd. or § of a yd.
- (12)  $\frac{1}{2}$  of a yd. or  $\frac{2}{3}$  of a yd.
- (13)  $l_{\overline{4}}^7$  of  $l_{\overline{11}}^3$  of  $l_{\overline{3}}^2$  of  $l_{\overline{45}}^2$  of a loaf, or  $\frac{6}{7}$  of  $\frac{1}{10}$  of  $\frac{51}{2}$  loaves?

#### ADDITION OF VULGAR FRACTIONS.

75. RULE. reduce the fractions to equivalent ones with the least common denominator.

Add all the new numerators together, and under their sum write the common denominator.

Ex. 1. Find the sum of  $\frac{1}{2}$ ,  $\frac{1}{3}$ , and  $\frac{5}{2}$ . By the Rule, The L. C. M. of the den<sup>rs</sup>. is 24.

 $\therefore \text{ fract}^{n_{5}} \text{ become} \frac{1 \times 12}{2 \times 12} \text{ or } \frac{12}{24} \frac{1 \times 8}{3 \times 8} \text{ or } \frac{8}{24} \frac{5 \times 3}{8 \times 3} \text{ or } \frac{15}{24}.$  $\therefore \text{ Their sum} = \frac{12 + 8 + 15}{24} = \frac{35}{24} = 1\frac{11}{24}.$ 

*Reason for the Rule.* In each of the equivalent fractions unity is divided into 24 equal parts, and 12, 8, and 15, of such parts are taken, therefore their sum must be 12 + 8 + 15, or 35 of such parts, and will be represented by the fraction  $\frac{4}{24}$ , or by  $1\frac{1}{24}$ .

Note 1. If the sum of the fractions be a fraction which is not in its lowest terms, reduce it to its lowest terms; and if the result be an improper fraction, then reduce it to a whole or mixed number: thus  $\frac{147}{105} = \frac{49}{35} = 1\frac{14}{35}$ : the same remark applies to all results in Vulgar Fractions.

Note 2. Before applying the Rule, reduce all fractions to their lowest terms, improper fractions to whole or mixed numbers, and compound fractions to simple ones.

Note 3. If any of the given numbers be whole or mixed numbers; the whole numbers may be added together as in simple addition, and the fractional parts by the Rule given above.

Ex. 2. Find the sum of  $3_{152}^{*}$ ,  $3_{13}^{*}$ ,  $2_{16}^{*}$ , and  $\frac{3}{4}$  of  $3_{13}^{*}$ .  $\frac{3}{4}$  of  $3_{13}^{*} = \frac{3}{4}$  of  $\frac{1}{3}^{*} = \frac{1}{4} = 2\frac{3}{4}$ ;  $\therefore$  sum of fractions  $= 3 + 3 + 2 + 2 + \frac{1}{52} + \frac{3}{4} + \frac{7}{15} + \frac{3}{4}$ ,  $= 10 + \frac{5 \times 4}{12 \times 4} + \frac{1 \times 8}{6 \times 8} + \frac{7 \times 3}{16 \times 3} + \frac{3 \times 12}{4 \times 12}$  (since L. C. M of den<sup>16</sup>. =48)  $= 10 + \frac{20 + 8 + 21 + 36}{48} = 10 + \frac{85}{48} = 10 + 1\frac{37}{4\frac{3}{4}} = 11\frac{47}{4\frac{5}{8}}$ .

76. The sign () or  $\{\}$ , called BRACKET, enclosing numbers within it, and the sign called a VINCULUM, placed over two or more numbers, denotes that all the numbers within the bracket or under the vinculum are equally affected by anything outside the bracket or vinculum, thus (2 + 3) apples or 2 + 3 apples would mean 2 apples + 3 apples, or 5 apples; whereas 2 + 3 apples would mean 2 units + 3 apples.

6

Again  $\frac{1}{2} + \frac{1}{3}$  of  $(2 + \frac{1}{2}) = \frac{1}{2} + \frac{1}{3}$  of  $\frac{5}{2} = \frac{1}{2} + \frac{5}{2} = \frac{5}{4} = \frac{1}{4} = \frac{1}{4}$ .  $(\frac{1}{2} + \frac{1}{3})$  of  $(2 + \frac{1}{2}) = (\frac{3}{2} + \frac{2}{3})$  of  $(\frac{4}{2} + \frac{1}{3}) = (\frac{5}{2} \text{ of } \frac{5}{2} - \frac{25}{2} - 2\frac{1}{2})$  $(\frac{1}{2}+\frac{1}{3})$  of  $2+\frac{1}{2}=(\frac{3}{2}+\frac{2}{3})$  of  $2+\frac{1}{2}=\frac{5}{2}$  of  $2+\frac{1}{2}=\frac{1}{2}+\frac{3}{2}=\frac{1}{2}=\frac{1}{2}=\frac{1}{2}$ Ex. 3. Find the value of  $\frac{4}{5} + \frac{1}{3}$  of  $(2 + \frac{1}{3}) + \frac{1}{6}$  of  $2\frac{1}{3} + \frac{1}{4}$  of  $(\frac{5}{5} + \frac{1}{2})$ value= $\frac{4}{5} + \frac{1}{5}$  of  $\frac{7}{5} + \frac{1}{5}$  of  $\frac{5}{5} + \frac{1}{4}$  of  $(\frac{5}{6} + \frac{3}{6}) = \frac{4}{5} + \frac{5}{12} + \frac{5}{24}$ .  $=\frac{11}{9} + \frac{5}{12} + \frac{1}{3} = \frac{44 + 15 + 12}{36}$  $=\frac{135}{36}=1\frac{35}{36}$ Ex. XLIII. Find the sum of, 1 and 2. and a. (1) (2) (3) 3 and  $\frac{1}{3}$ . (4) and a. (5) 15 and 7. (6)  $\frac{3}{4}$  and  $\sqrt{7}_{5}$ . (7) \$ and 5. (8) 3 and 1. (9) 11 and 2. (10) 11 and 11. (11) 73 and 8. (12) 11 of 21 and 61. 3. 4, and 72. 23, 15, and 31. (13) (14) (15) 63, 1 of 13, and 27. (16) 91 of 21, 13, and 17. (17)  $\frac{2}{3}$ ,  $\frac{5}{6}$ , and  $\frac{1}{3}$  of  $(1 + 1\frac{1}{3})$ . Find the value of, (18)  $\frac{1}{3} + \frac{2}{3} + \frac{2}{3} + \frac{1}{3}$  $(19) \quad 2\frac{1}{2} + 3\frac{1}{3} + 4\frac{1}{2} + 5\frac{1}{3}.$ (20)  $5\frac{7}{54} + 13\frac{5}{32} + \frac{49}{52} + 2\frac{23}{60}$ . (21)  $4\frac{5}{5} + \frac{7}{15} + 16\frac{9}{20} + 25\frac{13}{25}$ . (22)  $3\frac{8}{5} + 16\frac{7}{5} + 7\frac{5}{5} + \frac{2}{5}$  of  $3\frac{8}{5}$ . (23)  $(2\frac{3}{4} + 3\frac{3}{4})$  of  $2\frac{5}{11} + 3\frac{1}{4}$  of  $(16\frac{5}{4} + 3\frac{1}{4}) + 1\frac{3}{4}$  of 11 of  $2\frac{1}{22}$ . (24) A gentleman gave  $\pounds 2\frac{1}{18}$  to A,  $\pounds \frac{1}{2}$  to B,  $\pounds 3\frac{1}{12}$  to C, £413 to D, and £39 to E. How much did he give away? (25) A man ate  $\frac{3}{10}$  of a 4 lb. loaf on Mon.,  $\frac{5}{12}$  of a similar loaf on Tues., <sup>7</sup>/<sub>15</sub> on Wed., <sup>9</sup>/<sub>20</sub> on Thurs., <sup>1</sup>/<sub>2</sub> on Frid., and on Sat. and Sun. as much as on Mon., Tues., and Wed. How many lbs. of bread did he eat during the week? SUBTRACTION. 77. RULE. Reduce the fractions to equivalent ones having the least common denominator. Take the difference of the new numerators, and place the common denominator underneath. Ex. 1. Subtract & from §. By the Rule,  $1 \times 4$ The fract<sup>ns</sup>. become  $\frac{1}{2 \times 4}$  or  $\frac{1}{8}$ , and  $\frac{1}{8}$ , 5-4

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$$\therefore$$
 their difference  $=\frac{1}{9}$ 

Reason for the Rule. In each of the equivalent fractions, unity is divided into 8 equal parts, and there are 5 and  $\cdots$ parts respectively taken, ... the difference must be 5-4, or 1 of such parts, which is represented by  $\frac{1}{3}$ .

Note 1. Before applying the Rule, reduce fractions is their lowest terms, improper fractions to whole or mixed numbers, and compound fractions to simple ones.

Note 2. If either of the given fractions be a whole or mixed number, it is most convenient to take separately the difference of the integral parts and that of the fractions is parts, and then add the two results together, as in the foilowing examples.

Ex. 2. From 
$$4\frac{3}{5}$$
 take  $2\frac{1}{4}$ , or from  $(4 + \frac{3}{5})$  take  $(2 + \frac{1}{4})$ .  
Diff.= $(4 + \frac{3}{5}) - (2 + \frac{1}{4}) = 4 + \frac{3}{5} - 2 - \frac{1}{4}$  (Art. 76.)  
 $= (4 - 2) + (\frac{3}{5} - \frac{1}{4}) = 2 + (\frac{3}{5} - \frac{3}{5}) = 2 + \frac{1}{5} = 2\frac{1}{5}$ .

Ex. 3. Find the difference between 28 and 44.

is greater than 1, and ... cannot be taken from it,

... we write  $4\frac{1}{4}$  thus  $(3 + 1 + \frac{1}{4})$ , or  $(3 + \frac{5}{4})$ 

then diff•: = $(3\frac{5}{4}) - (2 + \frac{3}{8}) = (3 - 2) + (\frac{5}{4} - \frac{3}{8}) = 1 + \frac{19}{8} - \frac{5}{4} + \frac{19}{8} - \frac{5}{8} + \frac{19}{8} - \frac{19}{8} + \frac{19}{8} + \frac{19}{8} - \frac{19}{8} + \frac{19}{8}$ 

# Ex. XLIV.

Find the diff. between

(1)	1 and 1.	(2)	1/2 and 1/8.	(3)	\$ and 5.
(4) .	13 and 19.	(5)	$3\frac{2}{3}$ and $2\frac{1}{6}$ .	(6)	7 and 21%.
(7)	1012 and 83.	(8)	$17\frac{3}{4}$ and $13\frac{5}{6}$ .	(9)	$1\frac{4}{25}$ and $\frac{3}{4}$ .

(10)  $4\frac{3}{7}$  and  $2\frac{17}{20}$ . (11)  $15\frac{3}{7}$  and  $7\frac{2}{3}$ . (12)  $20\frac{5}{13}$  and  $8\frac{3}{56}$ .

(13) A boy ate  $\frac{3}{6}$  of a cake, how much less did he leave than he ate?

(14) What number added (1) to  $\frac{7}{36}$  will make  $\frac{13}{12}$ ? and (2) to  $2\frac{4}{5}$  will make  $8\frac{1}{2}$ ?

(15) I copied down by mistake §d. instead of §d., what amount of error did I make?

78. Examples involving both Addition and Subtraction of Vulgar Fractions.

F

Ex. 1. Find the value of 
$$5\frac{1}{4} - 2\frac{1}{2} + \frac{1}{8} + 2\frac{1}{4} - \frac{1}{16}$$
.  
Value =  $(5-2+2) + (\frac{1}{4} - \frac{1}{2} + \frac{1}{8} + \frac{1}{4} - \frac{1}{16})$ .  
=  $5 + \frac{4-8+2+4-1}{16} = 5 + \frac{1}{16} = 5\frac{1}{16}$ .

Ex. 2. Find the value of  $\frac{4}{5} + \frac{1}{3}$  of  $(2 - \frac{1}{3}) - \frac{1}{6}$  of  $2\frac{1}{2} + \frac{1}{3}$  $-\frac{1}{2}$  of  $(\frac{5}{6} - \frac{1}{2})$ . Value= $\frac{4}{9} + \frac{1}{3}$  of  $(\frac{6-1}{3}) - \frac{1}{6}$  of  $\frac{5}{2} + \frac{1}{2} - \frac{1}{4}$  of  $(\frac{5}{6} - \frac{3}{6})$  $=\frac{4}{5}+\frac{1}{3}$  of  $\frac{5}{3}-\frac{1}{6}$  of  $\frac{5}{2}+\frac{1}{2}-\frac{1}{4}$  of  $\frac{2}{6}=\frac{4}{5}+\frac{5}{3}-\frac{5}{12}+\frac{1}{2}+\frac{1}{3}$  $= 1 - \frac{5}{12} + \frac{1}{2} - \frac{1}{12} = 1 + \frac{1}{2} - \frac{5}{12} - \frac{1}{12} = 1 + \frac{6}{12} - \frac{1}{12} - \frac{1}{12} = 1 + \frac{6}{12} - \frac{1}{12} - \frac{1}{12} = 1 + \frac{6}{12} - \frac{1}{12} = 1 + \frac{6}{12} - \frac{1}{12} = 1.$ 

#### Ex. XLV.

Find the value of

- $\frac{1}{4} + 2\frac{1}{7} + 13\frac{3}{10} 3\frac{3}{70}$  (2)  $\frac{1}{4} \frac{3}{8} + \frac{5}{6} \frac{18}{24}$ (1)
- $12\frac{11}{17} \frac{21}{34} + 7\frac{16}{51} \frac{1}{3}$  of  $\frac{16}{17} + \frac{2}{5}$  of  $3\frac{3}{4}$ . (3)
- $(16\frac{5}{2} 3\frac{1}{4})$  of  $3\frac{1}{5} 16\frac{5}{5} + 3\frac{1}{4}$  of  $3\frac{1}{5}$ (4)
- (5)  $6\frac{1}{4} + \frac{7}{12}$  of  $\frac{9}{14}$  of  $3\frac{1}{3} \frac{45}{45} 5\frac{3}{4}$ .
- (6)  $6\frac{1}{4} + \frac{7}{12}$  of  $\frac{9}{14}$  of  $(3\frac{1}{3} \frac{45}{60}) 5\frac{3}{4}$ .

(7) What number must be added to the sum of  $\frac{4}{5}$ ,  $\frac{7}{5}$ , and 11, to make 5,89?

(8) A bought  $\frac{3}{4}$  of a cheese, and sold  $\frac{1}{3}$  of his purchase to B.  $\frac{1}{2}$  of what then remained to C,  $\frac{1}{2}$  of what then remained to D; what part of the cheese had B, C, and D, and what part had A, after the sales ?

#### MULTIPLICATION.

79. RULE. Multiply all the numerators together for a new numerator, and all the denominators together for a new denominator.

Ex. 1. Multiply  $\frac{2}{3}$  by  $\frac{5}{7}$ . By the Rule,  $\frac{2}{3}$  multiplied by  $\frac{5}{7} = \frac{2 \times 6}{3 \times 7} = \frac{10}{12}$ . Reason for the Rule.  $\frac{2}{3}$  multiplied by 5, gives  $\frac{1}{3}^{6}$  (Art 64.) But  $\frac{1}{3}^{6}$  must be 7 times too large, since 5 is one-seventh part of 5. Therefore 10 must be divided by 7, and  $\frac{19}{2} \div 7 = \frac{19}{19}$  (Art. 65.)

Note 1. The same reasoning will apply, whatever be the number of fractions which have to be multiplied together. .

Note 2. Before applying the Rule, mixed numbers must be reduced to improper fractions.

Note 3. It has been shewn that a fraction is reduced to its

nowest terms by dividing its num<sup>7</sup>. and den<sup>7</sup>. by their G. C. M., or in other words, by the product of those factors which are common to both; hence, in all cases of multiplication of fractions, it will be well to split up the num<sup>7</sup>. and den<sup>76</sup>. as much as possible into the factors which compose them; and then, after putting the several fractions under the form, of one fraction, the sign of X being placed between each of the factors in the num<sup>7</sup>. and den<sup>7</sup>. to cancel those factors which are common to both, before carrying: into effect the final multiplication. Thus, in the following examples:

Ex. 1. Multiply 
$$\frac{3}{4}$$
 and  $\frac{4}{5}$  together.  
Prod<sup>4</sup>.  $=\frac{3\times4}{4\times5} = \frac{3}{5}$ , dividing num<sup>7</sup>. and den<sup>7</sup>. by 4.  
Ex. 2. Multiply  $\frac{8}{9}, \frac{16}{24}, \frac{27}{30}, \text{ and } \frac{45}{60}$  together.  
Prod<sup>4</sup>.  $=\frac{8\times16\times27\times45}{9\times24\times30\times60}$   
 $=\frac{(2\times2\times2)\times(2\times2\times2\times2)\times(3\times3\times3)\times(3\times3\times5)}{(3\times3)\times(2\times2\times2\times2)\times(2\times2\times2\times2)\times(3\times3\times3)\times3\times5)}$   
Ex. 3. Multiplying  $2\frac{1}{2}, 3\frac{1}{3}, 10\frac{1}{2}, 20\frac{1}{5}, \text{ and } 5\frac{9}{73}$  together  
Prod<sup>4</sup>.  $=\frac{5}{2}\times\frac{27}{8}\times\frac{81}{8}\times\frac{184}{9}\times\frac{124}{23}$   
 $=\frac{5\times(9\times3)\times(9\times9)\times(3\times23)\times(4\times31)}{2\times(2\times4)\times3\times9\times23}$   
 $=\frac{5\times3\times9\times9\times31}{2\times2}=\frac{37665}{4}=9416\frac{1}{4}$ .  
Ex. 4. Simplify ( $\frac{1}{7}$  of  $1\frac{1}{4}$  of  $\frac{1}{15}+\frac{3}{2}$  of  $2\frac{1}{2}, \frac{27}{7}$   
 $=\left(\frac{3\times2\times5\times2\times7}{7\times2\times2\times3\times5}+\frac{7\times2\times26}{2\times3\times7}-\frac{8}{3}\right)\times\frac{27}{7}$   
 $=\left(1+\frac{26}{3}, \frac{8}{3}\right)\times\frac{27}{7}=\frac{21}{3}\times\frac{27}{7}=27$ 

# Ex. XLVI.

Find the value of

 $\frac{1}{5} \times \frac{3}{4}$ . (2)  $\frac{7}{5} \times \frac{5}{5}$ . (3)  $\frac{4}{13} \times \frac{5}{8}$ . (4)  $\frac{2}{21} \times \frac{7}{8}$ . (1)

(5)  $7\frac{1}{2} \times 3\frac{1}{3}$ . (6)  $\frac{3}{4}$  of  $\frac{1}{5} \times 17\frac{1}{2}$ . (7)  $\frac{7}{12}$  of  $1\frac{1}{7} \times 3\frac{3}{20} \times \frac{13}{34}$ .

(8)  $\frac{5}{6} \times 3\frac{2}{11} \times 19\frac{1}{5} \times \frac{11}{56}$ . (9)  $\frac{7}{18}$  of  $1\frac{1}{15}$  of  $1\frac{13}{12} \times 2\frac{1}{5} \times 2\frac{2}{7}$ .

(10)  $\frac{11}{14}$  of  $3\frac{3}{4} \times 4\frac{4}{5}$  of  $2\frac{1}{22} \times 13$ .

(11)  $2\frac{11}{23}$  of  $(4\frac{1}{5} + 3\frac{5}{14}) \times \frac{1}{5}$  of  $2\frac{1}{10} \times 1\frac{1}{10}$ .

(12)  $(3\frac{5}{8} - 1\frac{7}{12} + 1\frac{4}{8} - 2\frac{11}{12}) \times 38\frac{1}{4}$  of  $\frac{7}{77}$ .

(13) $\frac{3}{4}$  of  $(\frac{1}{3} + \frac{1}{4} - \frac{4}{15} + \frac{1}{9}) \times \frac{3}{3}$  of  $(2\frac{3}{16} + \frac{5}{9})$ .

- (14)  $\{(\frac{1}{2} + \frac{1}{3}) \text{ of } (1\frac{1}{3} + 2\frac{3}{4})\} \times \{(2\frac{1}{14} 1\frac{1}{3}) \text{ of } (3\frac{1}{10} \frac{3}{7})\}.$
- $\{1\frac{3}{7} \text{ of } 26\frac{1}{2} \text{ of } (1-\frac{3}{3})\} \times \{2\frac{5}{8} \text{ of } (4\frac{1}{5}-3\frac{3}{8}) \text{ of } \frac{45}{106}\}.$ (15)

#### DIVISION.

80. RULE. Invert the divisor, i. e. take its numerator as a denominator and its denominator as a numerator, and proceed as in Multiplication.

Ex. 1. Divide ? by 3.

By the Rule,  $\frac{3}{7} \div \frac{3}{4} = \frac{3}{7} \times \frac{3}{7} = \frac{3}{74}$ .

Reason for the Rule. If \$ be divided by 2, the result is 3 (Art. 65).

This quotient is only one-third part of the required quotient, since the divisor is one-third part of 2; hence 3 must be multiplied by 3, in order to give the true quotient, and  $^{13}_{14} \times 3 = ^{9}_{14}$ . (Art. 64.)

Before applying this Rule, mixed numbers must Note. be reduced to improper fractions, and compound fractions to simple ones.

Ex. 2. Find the quotient of 335 by 42.

$$\mathbf{3}_{\frac{3}{25}}^{\frac{3}{25}} \div \mathbf{4}_{5}^{\frac{3}{2}} = \frac{78}{25} \div \frac{22}{5} = \frac{78}{25} \times \frac{5}{22} = \frac{2 \times 39 \times 5}{5 \times 2 \times 11} = \frac{39}{55}.$$

#### Ex. XLVII.

(2) 2 by 3. (3) fr by 8. (1) 18 by 4 (4) 45 by 67. (5) 56 by 5<sup>4</sup>/<sub>7</sub>. (7) 1 of 203 by 103. (6) 75 by 42. (8)  $\frac{2}{5}$  of  $5\frac{1}{2}$  by  $\frac{5}{22}$  of 9. (9)  $(\frac{3}{5} \text{ of } 7\frac{1}{2} - \frac{3}{17})$  by  $1\frac{2}{5}$ .

(10) Divide  $\frac{1}{4} + \frac{3}{4} - \frac{1}{4}$  by the sum of  $\frac{4}{4}$  and  $\frac{3}{4}$ .

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Divide

# VULGAR FRACTIONS.

(11) What number multiplied by 216 will produce 62?

(12) What must <sup>3</sup>/<sub>4</sub> be divided by in order to produce 2?

(13) What is the least fraction which must be added to the sum of 4 and '4 divided by their difference to make the result a whole number ?

Note. COMPLEX FRACTIONS may by this Rule be reduced to simple ones.

- (1)  $\frac{1_4^3}{2_2^1} = \frac{7}{4} = \frac{7}{4} \div \frac{5}{2}$  (Art. 59)  $= \frac{7}{4} \times \frac{5}{6} = \frac{7}{10}$ .
- $\begin{array}{c} (2) & \frac{4\frac{1}{2}}{30} = \frac{\frac{9}{2}}{\frac{3}{10}} = \frac{9}{2} \div \frac{3}{10} = \frac{9}{2} \times \frac{1}{30} = \frac{3}{20}. \end{array}$

 $\begin{array}{c} \text{Simplify,} \\ \text{(1)} \quad \frac{6\frac{1}{3}}{9\frac{1}{3}}, \\ \begin{array}{c} (2) \quad \frac{6}{2\frac{1}{4}}, \\ \hline \\ \frac{7}{3\frac{1}{3}}, \\ \end{array} \\ \begin{array}{c} (2) \quad \frac{6}{2\frac{1}{4}}, \\ \hline \\ \frac{7}{3\frac{1}{3}}, \\ \hline \\ \frac{7}{3\frac{1}{3}}, \\ \end{array} \\ \begin{array}{c} (3) \quad \frac{24}{6}, \\ \hline \\ \frac{7}{3\frac{1}{3}}, \\ \hline \\ \\ \frac{7}{3\frac{1}{3}}, \\ \\ \\ \\ \frac{7}{3\frac{1}{3}}, \\ \hline \\ \\ \frac{7}{$ 

81. To find the value of a fraction in terms of the same or lower denomination.

RULE. Divide (if possible) the numerator by the denominator; if there be a remainder, reduce it to the next lower name, and divide the product by the denominator; repeat the latter operation as often as necessary.

Find the value of <sup>2</sup>/<sub>4</sub> of £15.

By the Rule,

$$\frac{1}{7}$$
 of £15 =  $\pounds \frac{2 \times 15}{7} = \pounds \frac{30}{7} = \pounds 4\frac{2}{7}; \pounds \frac{2}{7} = \frac{2 \times 20}{7}s. = \frac{40}{7}s. = 5\frac{5}{7}s.;$ 

 $\frac{\sqrt[5]{7}s.=5\times12}{7}d.=\frac{60}{7}d.=8\,\frac{1}{7}d.=\frac{4\times4}{7}q.=\frac{16}{7}q.=2\frac{2}{7}q.$  $\therefore \frac{2}{7} \text{ of } \pounds 15=\pounds 4.5s.8\frac{1}{7}d.\frac{2}{7}q.$ 

# Ex. XLIX.

Find the respective values of,

(1)	<sup>2</sup> / <sub>5</sub> of \$1. (2) <sup>3</sup> / <sub>5</sub> of	a ml.	(3) <sup>3</sup> / <sub>7</sub> of a cwt.
(4)	<sup>9</sup> / <sub>20</sub> of 2 tons. 3 cwt.	(5)	<sup>3</sup> / <sub>16</sub> of 3 mls., 2 fur.
(6)	4 of 3 ac., 2 per., 3 yds.	(7)	5 of 5 lbs., 13 dwts.
(8)	7 of 68 yds. 2 nls.	(9)	<sup>3</sup> <sub>11</sub> of £26. 8s. 11d.
10)	<sup>§</sup> / <sub>7</sub> of 128 lbs., 2 sc.	(11)	₹ of § of 103 hrs.
12)	75 of a lb. Avoird.	(13)	<sup>6</sup> / <sub>7</sub> of <sup>2</sup> / <sub>3</sub> of \$42.
14)	To of a day.	(15)	$\frac{9}{16}$ of 24 cords of wood.
00	177 A 7		

82. To reduce a given quantity to the fraction of another quantity of the same kind.

RULE. Reduce both to the same name; and take the result of the former for the numerator, and of the latter for the denominator, of the required fraction.

Reduce 7s. 5d. to the fraction of £1.

Method of working,

 $\therefore$  the fraction is  $\frac{89}{240}$ .

7s. 5d. = 89d.

 $\pounds 1. = 240d.$ 

Reason for the Rule. For  $1d. = \frac{1}{24\pi}$  of £1;  $\therefore$  7s. 5d. which = 89d. is  $\frac{89}{240}$  of £1.

#### Ex. L.

Reduce,

(1) 3s. 4d. to the fr. of £1.

(2) 2 ro. 13 per. to the fr. of 3 acres.

(3) 3 wks., 16 min. to the fr. of half-an-hour

(4) 1 lb., 1 oz., 3 dwt., to the fr. of 2 lbs.

(5) 1 lb., 5 oz. to the fr. of 2 lbs. 1 sc.

(6) 8 ac., 3 ro. to the fr. of 2 ac., 32 per.

(7) 2 sq. yds., 2 ft., 120 in., to fr. of 3 per. 131 yds., 1 ft., 72 in.

(8) £1. 18s. to the fr. of £7.

(9) 2 bu., 1 pk., to the fr. of 4 bu. 1 gal.

(10) \$2.09 to the fr. of \$56.43.

(11) 2 yds., 2 ft. to the fr. of 13 per., 3 yds., 6 in.

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# VULGAR FRACTIONS.

(12) 1 lb. Troy to the fr. of 1 lb. Avoirdupois.

(13) What fraction of 7 bu. is 3 qts.?

(14) What fraction of 4 mls., 2 fur. is 11 yds.?

(15) What fraction of 5 ac., 1 per. is 1 yd., 4 in.?

83. To reduce a fraction of one given quantity to a fraction of another.

RULE. Express by (82) the first quantity as a fraction of the second; and the fraction required will then be found by reducing the resulting compound fraction to a simple one.

Ex. 1. Reduce 2 lb. to the fraction of a cwt.

Method of working,

1 lb.  $=\frac{1}{100}$  of cwt.;  $\therefore \frac{2}{7}$  lb.  $=\frac{2}{7} \times \frac{1}{100}$  of a cwt.  $=\frac{3}{300}$  of cwt. Ex. 2.  $2\frac{1}{2}$  of \$5.25 to the fraction of 15 cents.

\$5.25 is \$\$ of 15 cts.; ... 21 of \$\$ of 15 cts. = \$15 of 15 cts.

Ex. LI.

Reduce,

(1)  $\frac{2}{9}$  of \$14 to the fr. of  $\frac{1}{2}$  of \$16.

(2) \$ of 2 ac., 2 ro. to the fr. of \$ of 3 ac., 2 per.

(3) 21 of 3 lbs., 6 dwt. to the fr. of 11 of 6 lbs., 12 grs.

(4) 122 of 3s. 6d. to the fr. of £1.

(5) 31 of 10 cwt., 2 qrs., to the fr. of 1 ton.

(6)  $3\frac{1}{2}$  of 2 ac., 3 ro. to the fr. of 2 ro.,  $2\frac{1}{2}$  per.

(7) § lb. Troy to the fr. of a lb. Av.

(8)  $1_{17}^{3}$  of £2. 4s.  $7\frac{1}{2}d$ . to the fr. of 5s.

(9)  $\frac{3}{11}$  of  $2\frac{3}{4}$  mls. to the fr. of  $\frac{1}{2}$  of  $\frac{7}{5}$  mls.

(10)  $6\frac{1}{2}$  of 3 cords to the fr. of 5 cord ft.

(11) 81 of 6 lbs., 2 sc. to the fr. of a lb.

(12) \$ of \$ of \$21 to the fr. of \$7.

(13)  $\frac{9}{16}$  of 8 yds., 2 nls. to the fr. of  $2\frac{1}{3}$  ells (English).

(14) 27 of 10 hrs. to the fr. of 1 day.

84. Miscellaneous Examples in Vulgar Fractions worked out.

Ex. .1. At the 'call over' at a certain school, § of the children on the register answered to their names; the rest, 18 in number, were absent. How many children were there on the register?

a of the no. were present, . . . tof no. were absent.

By the question,  $\frac{1}{6}$  of no. = 18.

... no. = 18 × 6 = 108.

Ex. 2. A poor woman lost through a hole in her pocket  $*_{T}$  of her money; only 3s.  $0_{4}^{2}d$ . was left. How much money had she at first, and how much did she lose?

After losing  $\frac{4}{11}$  of her money,  $\frac{7}{11}$  of it was left,

 $\begin{array}{c} \ddots \ _{1}^{\tau_{1}} \text{ of her money} = 3s. \ 0_{4}^{3}d. \\ \ddots \ _{1}^{\tau} \text{ of her money} = 3s. \ 0_{4}^{3}d. \\ \ddots \ _{1}^{\tau} \text{ of her money} = 3s. \ 0_{4}^{3}d. \\ \ddots \ _{1}^{\tau} \text{ of her money} = 5_{\frac{1}{2}}d. \\ \times 11 = 4s. \ 9_{4}^{3}d. \\ \end{array}$ She lost  $_{11}^{\tau_{1}} \text{ of } 4s. \ 9_{4}^{3}d. = \frac{19s. \ 3d.}{11} = 1s. \ 9d. \end{array}$ 

Ex. 3. A, B, C. D run a race over 1 mile. First A and B race, when A wins by 20 yds.; then C and D race, when i wins by 60 yds.; then A and C race, which will win, and by how much, supposing that if B and D had run against ach other, B would have won by 40 yds.?

While A runs 1760 yds., B runs 1740 yds.; while C runs 1760 yds., D runs 1700 yds., or while D runs 1 yd., C runs 4768 yds.; while B runs 1760 yds, D would have run 1720 yds., or while B runs 1 yd., D would have run  $\frac{17768}{1768}$  yds. While A runs 1760 yds., B runs 1740 yds.

" D runs  $(1740 \times \frac{172}{176})$  yds.

"
"
C runs  $(1740 \times \frac{178}{176} \times \frac{178}{176})$ , or 1760  $\frac{8}{17}$  yds. ... C will win by  $\frac{8}{17}$  yds.

Ex. 4. Divide 15s. 6d. between A and B, so that B's share may be less than A's share by  $\frac{2}{5}$  of A's share.

To represent A's share fix on some number which is exexcitly divisible by 5; let 5 represent A's share.

Then B's share  $= 5 - \frac{2}{5}$  of 5, or 5 - 2, or 3.

, . 15s. 6d. has to be divided into 5 + 3, or 8 shares, of which A is to have 5, and B 3;

... value of each share  $=\frac{15s. \ 6d.}{8}=1s. \ 11\frac{1}{4}d.$ 

... A's share = 1s.  $11\frac{1}{4}d$ .  $\times 5 = 9s$ .  $8\frac{1}{4}d$ ., B's = 1s.  $11\frac{1}{4}d$ .  $\times 3 = 5s$ .  $9\frac{3}{4}d$ .

Ex. 5. If 7 men or 11 boys can dig a field in 10 days, in what time will 11 men and 7 boys dig a field of half the size?  $7 \text{ men} = 11 \text{ boys}, \therefore 1 \text{ man} = \frac{1}{7} \text{ boy};$ 

... 11 men and 7 boys= $(11 \times \frac{1}{7} + 7)$ , or  $\frac{121 + 49}{7}$ , or  $\frac{170}{7}$  boys.

66

# VULGAR FRACTIONS.

By the question,
11 boys can dig the greater field in 10 days,
1 boy(10 × 11) days;
$170 \qquad 10 \times 11 \times 7$
the lass field in $10 \times 11 \times 7$ down = 0.2 down
$170 \times 2$ days $z_{s_{\overline{s}}}$ days.
Ex. 6. Divide 1860 cords of wood between A, B, and C, so that for every 5 cords given to A, B may receive 4 cords, and for every 3 cords given to B, C may receive 1 cord. The L. C. M. of 5, 4, and 3 is 60; $\therefore$ if 60 shares be given to A, B will have $\frac{1}{5}$ of 60 shares, or 48 shares, and C will have $\frac{1}{5}$ of 48 shares, or 16 shares; $\therefore A$ , B, and C together have (60 + 48 + 16), or 124 shares; $\therefore A$ has $\frac{60}{124}$ of 1860 cords = (15 × 60), or 900 cords. B has $\frac{48}{124}$ of 1860 cords = (12 × 60), or 720 cords. 16
C has $\frac{10}{124}$ of 1860 cords = (4 × 60), or 240 cords.
Ex. 7. $A$ can do a piece of work in 5 days, $B$ can do it in 6 days, and $C$ can do it in 7 days; in what time will $A$ , $B$ , and $C$ , all working at it, finish the work? Find also in what time $A$ and $B$ working together, $A$ and $C$ together, and $B$ and $C$ together, could respectively finish it. In one day $A$ does $\frac{1}{2}$ part of the work, $\frac{B}{2}$ $\frac{1}{2}$
(1, 2) = (1, 1) + (
$A + B + C do \left(\frac{1}{5} + \frac{1}{6} + \frac{1}{7}\right) or \frac{1}{210};$
, no. of days in which $A + B + C$ would finish the work $= \frac{\text{whole work}}{\text{part done in one day}} = \frac{1}{107} = \frac{210}{107} = 1\frac{193}{107}.$
210
Again, in one day $A + B \operatorname{do}\left(\frac{1}{5} + \frac{1}{6}\right)$ , or $\frac{11}{30}$ of the work,
$\therefore A + B$ would finish the work in $\frac{1}{11}$ , or $\frac{30}{11}$ , or $23$ days.
30

A

.

In like manner, it may be shewn that A and C would finish the work in  $2\frac{1}{12}$  days; and B and C in  $3\frac{3}{13}$  days.

#### Ex. LII.

(1)  $\frac{1}{2}$  ths of a farm belongs to A, the rest to B; A sells  $\frac{1}{2}$  ths of his share to C, and  $\frac{1}{2}$  th of it to B; what portions of the farm do A, B, and C, respectively hold after the sales?

(2) (1) Among how many boys can 9 oranges be divided, so that each boy may have  $\frac{3}{5}$  of an orange? (2) From the sum of  $4\frac{1}{2}$  and  $3\frac{1}{10}$  take their difference.

(3) Divide  $\frac{2}{5}$  into two parts, so that one of them is greater than the other by  $\frac{3}{5}$ .

(4) (1) What number must be multiplied by  $1\frac{1}{6}$  of  $2\frac{2}{3}$  to give  $3\frac{3}{7}$ ? (2) What number must be added to  $\frac{1}{3}$  of  $2\frac{1}{7}$  to give  $3\frac{3}{7}$ ?

(5) A gives to  $B \frac{1}{5}$  of his money, to  $C \frac{1}{2}$  of what remains, and to  $D \frac{1}{5}$  of what then remains; compare the sums which A and D will now have.

(6) Miss Taylor, after spending  $\frac{1}{3}$ rd of the money in her purse, and then  $\frac{3}{2}$ ths of the remainder, has still left \$4.20; how much had she in her purse at first?

(7)  $\frac{1}{3^{T}}$  of a fishing smack being worth \$90, find the value of  $\frac{1}{3}$ rd of it.

(8) A person after paying an income-tax of 5 cents in the dollar, has a net income of \$855; find his gross income?

(9) If, when the income-tax was 6 cents in the dollar, a person paid \$54; how much less will he now pay, the tax being reduced 4 cents in the \$?

(10) If  $\frac{4}{20}$  of a rabbit be worth  $\frac{3}{20}$  of a pig; what is the value of 100 pigs?

(11) If, in practising, 7 riflemen shoot 26 rounds in 1 hr., 31 min.; how many rounds will 37 riflemen shoot in 4½ hrs. at the same rate ?

(12) A sum of money is divided into 4 parts, which are to each other as the numbers 1, 2, 3, 4; and a person, who receives § of each share, obtains altogether \$12.60; find the sum of the several shares?

(13) If 15 cows or 28 sheep can graze a field of 5 ac. in 11 days, how many days ought a similar field of 18 ac. to serve 33 cows and 20 sheep? (14) Divide \$94.50 between A and B; (1) giving A half as much again as B; (2) giving A's share less half A's share to B.

(15) A bankrupt owes to one creditor 500 dollars, to each of two others \$250, to each of three others \$75: his property is worth \$625. How much can he pay in the dollar, and how much will the first creditor receive?

(16) A mine is worth \$10000; a person for  $\frac{3}{16}$  of his share receives \$750. What part of the mine did he possess?

(17) A school is composed of three divisions; there are \$2\$ths of the whole number of boys in the first, \$th in the second, and the rest, 80 in number, in the third; how many boys are there altogether?

(18) A can do a piece of work in 10 days, which B could do in 12; in what time would they do it together?

(19) A father left to the elder of his two sons  $\frac{13}{25}$  of his estate, and  $\frac{13}{25}$  of the remainder to the younger, and the residue to the widow; find their respective shares, it being found that the elder son received \$1690 more than the younger.

(20) Divide 85 ac. 2 ro. of land between A, B, and C, so that B's share  $= \stackrel{\alpha}{_{11}}$  of A's share, and that C's share shall be 9 ac. more than the united shares of A and B.

(21) A fine of \$14.40 had to be raised among a number of boys; one-third paid 18 cents each, as many more 30 cents each, and the remainder 42 cents each. How many boys were there?

(22) A cistern has 3 pipes in it, by one of which it could be filled in 3 minutes, and by the other two it could be emptied in 6 and 7 minutes respectively; in what time will it be filled, if they are all opened together?

(23) A and B together can do a piece of work in 30 days, B by himself can do it in 70 days; (1) in what time could A do it by himself? (2) how much more of the work does A do than B, when they work together?

(24) A and B can do a piece of work in  $6\frac{2}{3}$  days, A and C in  $5\frac{1}{2}$  days, and A, B, and C in  $3\frac{3}{4}$  days. In how many days can A do it alone?

(25) There are 4 casks of different sizes. The 1st is filled with liquid the rest are empty. The 2nd cask is filled from the 1st, and ≱ths of the original liquid in the 1st remains. The 3rd is then filled from the 2nd, and ‡th of the liquid in the 2nd remains. The liquid in the third is then poured into the 4th, and fills  $q_{\rm x}^{\rm o}$  ths of it. Had the 3rd and 4th casks been filled from the contents of the 1st, 15 gallons would still have remained in the 1st. Find the size of each oask?

(26) A in 2 days can do as much work as B can do in 3 days; together they take 12 days to do a certain work. In what time would A alone have done it?

#### DECIMALS.

85. Figures in the units' place of any number express their simple values, while those to the left of the units' place increase in value tenfold at each step from the units' place; therefore, according to the same notation, as we proceed' from the units' place to the right every successive figure would decrease in value tenfold. We can thus represent whole numbers or integers and certain fractions under a uniform notation by means of figures in the units' place and on each side of it; for instance, in the number 5673.241, the figures on the left of the dot denote fractions. The number written at length would stand thus:

 $5 \times 1000 + 6 \times 100 + 7 \times 10 + 3 + \frac{2}{10} + \frac{4}{100} + \frac{1}{1000}$ 

The dot is termed the decimal point, and all figures to the right of it are called DECIMALS, or DECIMAL FRACTIONS, because they are fractions with either 10, 100 or  $10 \times 10$ , 100, and 10  $\times 10$ , 20, and 20  $\times 10 \times 10$ , 20, and 20  $\times 10 \times 10$ , 20, and 20  $\times 10 \times 10$ , 2

The extended Numeration Table will be represented thus:

&c.	7 Mil	6 Hui	5 Ten	4 Tho	⇔ Hui	2 Ten	1.2 Uni	3	4	5	6	7	
	lions,	ndreds of	s of Thou	usands.	ndreds.	ţe	ts.			ths.	usandths.		
		Thousand	isands.				chs.	dredths.	usandths.	Thousand	dred Tho	ionths.	
		ls.					Tent	Hun	Thot	Ten	Hun	Mill	kc.

86. 10, called the first Power of 10, is written thus,  $10^1$ .  $10 \times 10$ , or 100, called the second Power of 10, is written thus,  $10^2$ .

 $10 \times 10 \times 10$ , or 1000, called the *third* POWER of 10, is written thus,  $10^{\circ}$ , and so on; similarly of other numbers: thus the fifth power of 4 is  $4 \times 4 \times 4 \times 4 \times 4$ , and is written thus,  $4^{\circ}$ .

The small figures 1, 2, 3, &c., at the right of the number, a little above the line, are called INDICES.

97 .206 -	3 0	6	$3 \times 100$	$0 \times 10$	6
07. 000 -	$-10^{-100}$	1000	$10 \times 100$	$100 \times 10$	1000
	300	0 6	306		
	= 1000 $+$ 1	000 + 100	$1600^{-1}$		
A roin .030	0	3 (	0 6	0×10	00
ngain, 000	$-\frac{10}{10}$	100 10	00 10000	$\overline{10 \times 10}$	00
3×100	0×10	. 6	0+300-	+0+6	306
$+\frac{100\times100}{100\times100}$	1000×10	+ 10000	100	$\overline{00} = \overline{1}$	0000
A main 2019	06 - 00 1	306	80000 + 306	80306	
Again, 80'5	00=00+	1000	1000	1000	

Hence to convert decimals to vulgar fractions: from the above examples we deduce the following:

SS. RULE. Write the figures which compose the decimal as numerator, and for denominator 1, followed by as many cyphers as there are figures after the decimal point.

#### Ex. LIII.

Express as vulgar fractions, ·

- (1) '3; '13; '19; '301; '270; '5653.
- (2) .504; .73201; .791003; .03; .0045.
- (3) '300; 18.741; 2.1; '000001; 5.0007.
- (4) 347.02007; 500.005; 5.60746805; 0000500.
- (5) 29.0050; 20.607; 5.00038.

89. Any fraction, having 10, or any power of 10, for its denominator,  $as_{100000}^{s_{10000}}$ , may be expressed thus, 80 0036.

90.  $241 = \frac{241}{1000}$ ,  $0241 = \frac{241}{10000}$ ,  $2410 = \frac{2410}{10000} = \frac{241}{10000}$ .

We see that '241, '0241, and '2410 are respectively equivalent to fractions which have the same numerator, and the

first and third of which have also the same denominator, while the denominator of the second is greater. Hence 241 is equal to 2410, but 0241 is less than either.

The value of a decimal is therefore not affected by affixing cyphers to the right of it; but its value is decreased by prefixing cyphers : which effect is exactly opposite to that which is produced by affixing and prefixing cyphers to integers.

91. A decimal is multiplied by 10, if the decimal point be removed one place towards the right hand; by 100, if two places ; by 1000, if three places ; and so on : and conversely, a decimal is divided by 10, if the point be removed one place to the left hand; by 100, if two places; by 1000, if three places; and so on.

Thus,  $5.6 \times 10 = \frac{56}{10} \times 10 = 56$ ;  $5.6 \times 1000 = \frac{56}{10} \times 1000 = 5600$ .  $5 \cdot 6 \div 10 = \frac{56}{10} \times \frac{1}{10} = \frac{56}{100} = \cdot 56; 5 \cdot 6 \div 1000 = \frac{56}{10} \times \frac{1}{1000} = \frac{56}{1000}$ = .0056.

# Ex. LIV.

- (1)10; 10; 10; 10; 100; 1000; 1000.
- (2)5001; 961; 951; 502; 502 10; 100; 100000; 100; 100; 100000.
- 35600 1700701; 50005; 1000000; 2078854; 1000 100000; 1000000; 1000000; 100000; 100000; (3)10000000000000
- Seven-tenths; thirty thousandths. (4)
- Three hundred and three thousandths; one ten thou-(5) sandth.
- Four, and five hundred and four millionths : seventy (6) ten millionths.

Express in words the meaning of,

- ·6; ·17; ·07. (8) '007; '700; 6'3004. (7)
- (9) 35.00205:400.34000.

(10) Multiply 3, 13, 013, 54 0003, 7420 1, each separately by 10, 100, 10000, and by ten millions.

(11) Divide 5:362, .3, 70:0107, and 5000, each separately by 10, 100, and by 1000000.

(12) What is the quotient of 2.03 by a million?

# ADDITION OF DECIMALS.

92. RULE. Place the numbers under each other, units under units, tens under tens, &c., tenths under tenths. &c. : so that the decimals be all under each other. Add as in

#### DECIMALS.

whole numbers, and place the decimal point in the sum under the decimal point above.

Ex. Add together 2.3, .056, 37, and 3.60015.

By the Rule.

1 1

·056	By fractions.
37.	$2 \cdot 3 + \cdot 056 + 37 + 3 \cdot 60015 = \frac{23}{10} + \frac{56}{1000} + \frac{37}{1} + \frac{360015}{10000}$
3.60015	$= \frac{230000}{100000} + \frac{5600}{100000} + \frac{3700000}{100000} + \frac{360015}{100000}$
42.95615	$=$ $\frac{4295615}{100000} = 42.95615$ (Art. 89).

## Ex. LV.

Add			
(1) 1.035 $(2)$	24.	(3) 186.8	(4) 94.25
.00643	185.3009	35.2779	•008
27.	·98795	9000	187.96009
2.2146	3.098	9.201	57:3916
530.09	•70006	830.05764	5.998347
		1	

Add together, and verify each result by fractions :

(5) 12.5, 20.043, 7.63201, add .0561.

(6) .0573, 15, 2.04, and 567.98075.

(7) 505.0003, 13.98, 5853.097, and 960.

(8) 6.00734, 54, 15.70087012, 8.00003, and 9.987789.

(9) Find the sum of thirteen hundredths, seven and three ten-thousandths, four hundred and eight and five tenths, nine hundred and seventy-eight, and eight hundred and eight ten-thousandths.

# SUBTRACTION OF DECIMALS.

93. RULE. Place the less number under the greater, units under units, tens under tens, &c., tenths under tenths, &c.; suppose cyphers to be supplied if necessary in the upper line to the right of the decimal.

Then subtract as in whole numbers, and place the decimal point in the remainder under the decimal point above.

Ex. Subtract 3.084 from 5.7.

By the Rule,

3.084		By fractions, 5.7 2:084 - 57 3084 - 5704 - 3084
-		01-001-10-1000-1000-1000
2.616		$=\frac{2519}{10}=2.616$
	-	1000 - 0100

#### Ex. LVI.

(1)	From 5.345	(2) 26.002	(3) 15.67	(4) 21
	Take 3.087	18.9564	9.7003	19.9009

(5) Find the difference between, verifying each result by fractions, (1) ·13 and 1·3; 2·07 and 207. (2) 76·3 and 7.63;
67·3 and 67:5803. (3) 501 and 428.90456; 53·24 and 5324.
(4) 4·42 and ·00042; ·0000007 and ·007.

(6) By how much does 23 exceed the difference between 2.3 and .23?

(7) Find the difference (1) between one-tenth and five thousandths; (2) between twenty and nine thousandths and twenty-nine thousandths.

(8) A person who has seven-tenths of a ship, sells eightyseven thousandths of it, how much has he left?

(9) Find the least fraction, which added to the sum of 1.2, .12, .012, and 210, will make the result a whole number.

(10) Find the value of (1)  $31\cdot25 - 3\cdot059 + 235\cdot6758 - 184\cdot0003$ ; (2)  $215\cdot263 - (7\cdot0004 - \cdot05) - (45\cdot08 + 80\cdot5007)$ .

# MULTIPLICATION OF DECIMALS.

94. RULE. Multiply the numbers together as if they were whole numbers, and point off in the product as many decimal places as there are decimal places in both the multiplicand and the multiplier; if there are not figures enough, supply the deficiency by prefixing cyphers.

Ex. Find the product of (1) 7.35 by 23, (2) of 8.27 by 0002.

By the Rule,

(1) 7.35

 $\frac{\cdot 23}{2205}
 1470$ 

By fractions,

 $5 \quad 7.35 \times .23 = \frac{7.55}{100} \times \frac{23}{100} = \frac{16905}{1000} = 1.6905.$ 

1.6902

(2) 8.27

 $0002 \quad 8.27 \times 0002 = \frac{127}{100} \times \frac{2}{100000} = \frac{1654}{1000000} = 001654.$ 

·001654

#### Ex. LVII.

Multiply $(1)$ 3.25 $(2)$	6.035	(3)	40.004	(4)	680.35	(5)	20607
By .35	2.7		2.03		·0049		·20607
	and the second division of the second divisio		Concession of the local division of the loca		COLUMN TWO IS NOT THE OWNER.		and the owner where the owner

# DECIMALS.

Multiply, and verify each result by fractions:

(6) 60.71 by 11; 57.068 by 2.004; 5.36 by 700; 7.01509 by 50.805.

(7) 48.067 by .00037; 54.3047 by 9.00005; 2.568 by .00025.

(8) Find the continued product (1) of 5.5, 055, 550, and 0055; (2) of 1.75, 6.2, 85, and 0004.

(9) How many yds. of cloth are there in 7.35 pieces of cloth, each of which contains 37.85 yds.?

(10) A man eats 95 of a loaf daily; how many loaves will he eat in the year 1866?

## DIVISION OF DECIMALS.

95. First. When the number of decimal places in the dividend exceeds the number of decimal places in the divisor.

RULE. Divide as in whole numbers, and mark off in the quotient a number of decimal places equal to the excess of the number of decimal places in the dividend over the number of decimal places in the divisor; if there are not figures sufficient, prefix cyphers as in Multiplication.

Ex. 1. Divide (1) 2.1125 by 8.45, (2) .0021125 by 84.5. By the Rule,

(1) 8.45)2.1125(25 By fractions,

1690	$2 \cdot 1125 \div 8 \cdot 45 = \frac{2}{1000} \div \frac{8}{100} \div \frac{8}{100} = \frac{2}{1000} \times \frac{8}{1000} $
4225	$\frac{1}{848} = \frac{21125}{846} \times \frac{1}{1600} = \frac{25}{1} \times \frac{1}{100} = \frac{25}{100}$
4225	= .25.

No. of dec<sup>1</sup>, places in quotient = 4 - 2 = 2,  $\therefore$  quotient = 25. (2) 84.5) .0021125 (25 By fractions.

390	$0021125 \div 84.5 = \frac{21125}{10000000} \div \frac{845}{10}$
1225	$= \frac{21125}{10000000} \times \frac{10}{845} = \frac{21125}{845} \times \frac{100000000}{100000000000000000000000000$
1225	$=\frac{25}{1} \times \frac{1000000}{10000000000000000000000000000$

a

No. of decl. places in quotient = 7-1=6,  $\therefore$  quotient = 000025. <sup>9</sup>96. Secondly. When the number of decimal places in the dividend is less than the number of decimal places in the divisor.

RULE. Affix cyphers to the dividend until the number of decimal places in the dividend equals the number of decimal places in the divisor; the quotient up to this point of the division will be a whole number.

It there be a remainder, and the division be carried on

further, the figures in the quotient after this point will be decimals.

Ex. 2. Divide 2112.5 by .845. By the Rule,

·845)2112·500(2500

1690	By fractions,
4225	$2112.5 \div .845 = {}^{2112.5}_{-10.4} \div {}^{845}_{-1000} = {}^{2112.1}_{-10.4}$
4225	$\times \frac{1000}{845} = \frac{21125}{845} \times \frac{1900}{845} = 25 \times 100 = 2500.$
00	

#### Ex. LVIII.

Divide and verify each result by fractions.

- (1) 33·372 by 2·7. (2) ·33372 by ·27. (3) ·33372 by 27.
- (4) 33372 by 27. (5) 33372 by 00027.
  - 561.0833 by .323. (7) 5610833 by .323.
- (8) 56108.33 by 3.23. (9) 5610.833 by .0000323.

(10) 552.5325 by 3.25, and also by .00325.

(11) 2.419003 by 464.3, and also by .004643.

(12) '000081 by 2.7, by '0027, and also by 27000.

(13) 218051.081884 by 2.00099, and by 200099.

(14) '121 by 11, by 1100, and also by '0011.

(15) 393.72 by 000193, by 1.93, and also by 193000.

(16) 590.4825 by .03275, and also by 327500.

(17) 213.419596 by 1.00103, and also by 100103.

(18) Divide the sum of twenty-four ten thousandths and twenty-four hundreths by twenty-four.

(19) Two ten thousandths by twenty-five hundreths.

(20) If a man mow 1.75 ac. of grass in one day, how long will it take him to mow 21.875 ac.?

(21) How often is '75 min. contained in 64.125 min.?

(22) The product of two numbers is seventy thousand two hundred and forty two hundred millionths; one of the numbers is twenty-three thousandths; find the other num ber.

Ex. 3. Divide 240.13 by 73.4 to three places of decimals.

Before dividing, affix two cyphers to the dividend, so as to make the number of decimal places in the dividend exceed

#### 100

(6)

#### DECIMALS.

the number of decimal places in the divisor by 3; if we divide up to this point, the quotient will contain 3 decimal places by Rule 1.

73.4 ) 240.1300 ( 3.271

220	By fractions,
1993	$240.13 \div 73.4 = 24813 \div 73.4$
1468	$= \frac{24013}{100} \times \frac{10}{734} = \frac{24013}{734} \times \frac{10}{100}$
5250	$= \frac{24013}{734} \times \frac{100}{1000}.$
5138	(we multiply num <sup>r</sup> . and den <sup>r</sup> . by 10, to
1120	make den <sup>r</sup> . 1000, since the quotient is
734	to contain three decimal places)
386	$= \frac{2401300}{734} \times \frac{1}{1000} = \frac{3271}{1000} = 3.271.$

# Ex. LIX.

Divide to three places of decimals, and verify each result by fractions,

(1) 1.9 by 3, by 03, and by 300.

(2) 4.937 by 159, by 1.59, and by 1590.

(3) 329744 by 53, by 0053, and by 5300.

97. Certain Vulgar Fractions can be expressed accurately as Decimals.

RULE. Reduce the fraction to its lowest terms; then place a dot after the numerator and affix cyphers for decimals; divide by the denominator, as in division of decimals, and the quotient will be the decimal required.

Ex. 1. Convert 3, 3, 30, 400, each into a decimal.

4) 3.00 No. of dec'. places in quotient = no. of dec'. places  $\overline{\phantom{0}}_{75}$  in dividend – no. of dec'. places in divisor = 2 - 0 = 2.

 $_{40}^{3} = \frac{3}{4} \div 10 = .75 \div 10 = .075; _{40}^{3} = \frac{3}{4} \div 100 = .75 \div 100 = .0075.$ 

Ex. 2.	Reduce	$\frac{1}{16}$ to a	a decimal.	
16)	5.0000 ( .	3125		

 $\begin{array}{r}
 20 \\
 16 \\
 \overline{40} \\
 32 \\
 \overline{80} \\
 80 \\
 80 \\
 80 \\
 \end{array}$ 

	10	(4	5.00
or thus,	10	4	1.2500
			·3125

	5		
•*•	16	=	•3125

Ex. 3. Convert  $5_{\overline{640}} + .75$  of  $\frac{6}{5}$  of  $7\frac{1}{2}$  into a decimal.

	( 8	5.000	$.75 \text{ of } \frac{6}{-} \text{ of } 7\frac{1}{2} = .75 \text{ of } \frac{6}{5} \text{ of } \frac{1}{5}$
640 -	10	078125	$5 = .75 \times 9 = 6.75.$
		·0078125	

 $\therefore 5^{-5}\pi + .75 \text{ of } \frac{6}{5} \text{ of } 7\frac{1}{2} = 5.0078125 + 6.75 = 11.7578125.$ 

#### Ex. LX.

Reduce to decimals,

(1)  $\frac{1}{4}$ ;  $\frac{3}{5}$ ;  $\frac{6}{4}$ ;  $\frac{6}{5}$ ;  $\frac{39}{5}$ ;  $\frac{5}{8}$ ;  $5\frac{3}{10}$ . (2)  $\frac{3}{16}$ ;  $\frac{815}{16}$ ;  $\frac{19}{26}$ ;  $\frac{31}{32}$ ;  $7\frac{37}{46}$ 

 $(3) \quad \tfrac{47}{50}; \, 4_{1\frac{7}{25}}; \, \tfrac{3}{500}; \, \tfrac{99}{625}; \, 84_{10\frac{3}{24}}.$ 

(4) § of 18; 31 of 24; 31 of 41 of 51.

(5)  $1\frac{3}{5} - \frac{13}{5} + 3\frac{5}{40}$ ;  $11\frac{1}{2} + .75$  of  $\frac{24}{5}$  of  $6\frac{3}{2}$ .

98. To convert a vulgar fraction into a decimal, we have in fact, after reducing the fraction to its lowest terms, and affixing cyphers to the num<sup>r</sup>., to divide 10, or some multiple of 10 or of its powers, by the denr.; now  $10=2 \times 5$ , and these are the only factors into which 10 can be broken up; therefore, when the fraction is in its lowest terms, if the den'. be not composed solely of the factors 2 and 5, or one of them, or of powers of 2 and 5, or one of them, then the division of the num'. by the den'. will never terminate. Decimals of this kind are called indeterminate decimals, and they are also called CIRCULATING, REPEATING, or RE-CURRING DECIMALS, from the fact that when a decimal does not terminate, the same figures must come round again, or recur, or be repeated : for since we always affix a cypher to the dividend, whenever any former remainder recurs, the quotient will also recur.

99. PURE CIRCULATING DECIMALS are those which recur from the beginning: thus, '333.., '2727.., are pure circulat<sup>g</sup>. dec<sup>la</sup>.

MIXED CIRCULATING DECIMALS are those which do not begin to recur, till after a certain number of figures : thus, '128888..., '0113636..., are mixed circulats. dec<sup>19</sup>.

The circulating part is called the PERIOD or REPETEND.

Pure and mixed circulating decimals are generally written

down only to the end of the first period, a dot being placed over the first and last figures of that period.

Thus 3	represents the pure circulats. decl.	•333
.36		•3636
·639		·639639
·138	mixed	·1388.
·01136		.0113636

100. Pure Circulating Decimals may be converted into their equivalent Vulgar Fractions by the following Rule.

RULE. Make the period or repetend the numerator of the fraction, and for the denominator put down as many *nines* as there are figures in the period or repetend.

This fraction, reduced to its lowest terms, will be the fraction required in its simplest form.

Ex<sup>\*</sup>. Reduce the following pure circulat<sup>\*</sup>. dec<sup>ia</sup>., 3, 27, 857142, to their respective equivalent vulgar fractions.

 $\frac{\cdot 357142}{3}, \text{ to their respective equivalent vulgar fractions.} \\ \text{By the Rule, } \cdot 3 = \frac{3}{9} = \frac{1}{3}; \quad \cdot 27 = \frac{27}{99} = \frac{3}{11}. \\ \cdot 357142 = \frac{857142}{999999} = \frac{142857 \times 6}{142857 \times 7} = \frac{6}{7}.$ 

101. Mixed Circulating Decimals may be converted into their equivalent Vulgar Fractions by the following Rule.

RULE. Subtract the figures which do not circulate from the figures taken to the end of the first period, as if both were whole numbers.

Make the result the num<sup>r</sup>.; and write down as many *nines* as there are figures in the circulating part, followed by as many zeros as there are figures in the non-circulating part, for the denominator.

Ex. Reduce the following mixed circulat<sub>g</sub>. dec<sup>1</sup><sub>s</sub>. <sup>1</sup>4, <sup>0</sup>133, <sup>2</sup>213, to their respective equivalent vulgar fractions.

By the Rule,  $\cdot_{1\dot{4}} = \frac{14-1}{90} = \frac{13}{90}; \cdot_{013\dot{8}} = \frac{138-13}{9000} = \frac{125}{9000}$ =  $\frac{1}{72}; \cdot_{2\dot{4}1\dot{8}} = \frac{2418-2}{9990} = \frac{2416}{9990} = \frac{1208}{4995}.$ 

102. In the Addition and Subtraction of circulating decimals, where the result is only required to be true to a certain number of decimal places, it will be sufficient to carry on the circulating part to two or three decimal places more than the number required; taking care that the last figure

retained be increased by 1, if the succeeding figure be 5, or greater than 5. In the Multiplication and Division, however, of circulating decimals, it is always preferable to reduce the circulating decimals to Vulgar Fractions, and having found the product or quotient as a Vulgar Fraction, then,  $\Re$  necessary, to reduce the result to a decimal.

#### Ex. LXL

Reduce to circulating decimals: (1)  $\frac{2}{3}$ ;  $\frac{1}{9}$ ;  $\frac{6}{7}$ ;  $\frac{7}{12}$ ;  $\frac{11}{15}$ (2)  $6\frac{3}{81}$ ;  $7\frac{5}{87}$ ;  $100\frac{7}{44}$ ;  $2\frac{15}{17}$ . (3)  $11\frac{67}{495}$ ;  $23\frac{15}{1875}$ .

Reduce to their equivalent vulgar fractions: (4) 2; 05; 18; 156; 027027; 285714. (5) 566; 743; 20235; 19:305; 20:02916. (6) 6:18153153; 15:692307692307.

Find the value correct to six places of dec<sup>1</sup>. of (7)  $4\dot{3}$ + 16 $\dot{4}\dot{5}$ +75 $\dot{7}35\dot{2}$ . (8)  $3\dot{2}\dot{3}$ +26 $\dot{7}9\dot{6}$ +7 $\dot{4}1\dot{3}$ . (9)  $3\dot{8}5\dot{6}\dot{4}$ -2 $\dot{8}0387$ . (10)  $52\dot{8}\dot{6}$ -8 $\dot{8}37235$ .

Find the value of (11)  $7 \cdot 6 \times 5 \cdot 3$ ;  $\cdot 3 \cdot 5 \cdot 1 \times 7 \cdot 3 \cdot 6$ ;  $\cdot 13 \times 2 \times 4$ . (12)  $6 \cdot 7 \div 2 \cdot 6$ ;  $\cdot 26 \cdot 7 \div 1 \cdot 92 \cdot 6$ ;  $\cdot 37 \cdot 1 \div 5$ ;  $42 \cdot 0463 \div 1 \cdot 3 \cdot 6$ .

# **REDUCTION OF DECIMALS.**

103. To reduce a decimal of any denomination to its proper value.

RULE. Multiply the given decimal by the number of units of the next lower denomination which make one of the given denomination, and point off for decimals as many figures in the product, beginning from the right hand, as there are figures in the given decimal.

The figures on the left of the decimal point will represent the whole numbers in the next denomination.

Proceed in the same way with the decimal part for that denomination, and so on.

Ex. 1. Find the value of '4625 of £1. By the Rule,

#### DECIMALS.

Note. If the quantity, the value of whose decimal part is to be found, be a compound quantity, it must be reduced to one denomination before the rule is applied.

Ex. 2. Find the value of 7.405 of 15 mi., 5 fur., 31 po.

15 mi., 5 fur., 31 po. = 5031 7.405 25155 20124 35217 37254 555 DO 51 2.775 ·2775 3.0525 vda po. yds. in. 3150 . val. =37254 3 1.89 1575 mi, fur. po. yds. in. 1.8900 in. or=116 3 14 3 1.89 Find the value of .5416 of 41 cwt. Ex. 3. 1st method. cwt. lbs. 41=450 .541666 2d. method. 450  $5416 \text{ of } 4\frac{1}{2} = \left(\frac{5416 - 541}{9000} \text{ of } \frac{9}{2}\right) \text{ cwt.}$ 27083300 2166664  $2\overline{43749700}$  lbs. =  $\left(\frac{4875}{9000} \times \frac{9}{2}\right)$  ewt. =  $\left(\frac{13}{24} \times \frac{9}{2} \times 100\right)$  lbs. 11.995200 oz. =243 lbs., 12 oz. ...value=243 lbs., 12 oz. nearly. The 2nd method is the better one in most cases. Ex. LXII. Find the value of. .75 of \$1. ·875 of \$5. (3) ·625 of \$1. (1) (2)(4) ·375 of a mi. (6) 175 of a ton. ·625 of 1 cwt. (5) (7) ·46875 of £2. 10s. (8) .0625 of 7s. 6d. 3.175 of 1 lb. Troy. (10) 4.65 of 44 ac. (9) (11) 10.04 of 21 ro. (12) 2.56 of 10s. 111d. (13) 5.00875 of 3 wks. 4 dys. (14) 16.504 days.

- (15) 3.05 of 5 lbs. 29. (16) 3.0085 of £4. 1s.
- (17) 7.034 of 1 ac., 3 ro., 5 po.
- (18) 5.005 of 16 lbs., 1 oz., 6 grs. Troy.
- (19) 3 of \$2. (20) 54 of 16s. 6d. (21) 243 of a ton
- (22) 6.83 of £5. (23) 2.383 of 21 lbs. T'y. (24) 6.2 of ac. yd.
- (25) 18 72 of an ac. (26) 2.063 of 1000 guineas.

(27)  $\pounds \cdot 634375 + \cdot 025$  of 25s.  $+ 3 \cdot 16$  of 30s.

(28) 6 of an ac. + 625 of a ro. - 4 po.

(29) 6.714285 of 1s. 9d. - 0833 of £7. 4s. + 251190476 of 6s. 8d.

104. To reduce a number or fraction of one or more denominations to the decimal of another denomination of the same kind.

RULE. Reduce the given number or fraction to a fraction of the proposed denomination; and then reduce this fraction to its equivalent decimal.

Ex. 1. Reduce  $\frac{2}{5}$  of £1 to the decimal of a guinea.

 $\frac{2}{3}$  of  $\pounds 1 = \frac{4}{9}s. = 8s. 1$  guin<sup>a</sup>. = 21s.,  $\therefore$  fraction req<sup>d</sup>. =  $\frac{8}{21}$ . Now  $8 \div 21 = \frac{3}{2}8095238..., \therefore$  dec<sup>l</sup>. req<sub>d</sub>. =  $\frac{3}{2}80952$ .

Ex. 2. What decimal of £2 is 11s. 9<sup>§</sup><sub>4</sub>d. ?

11s.  $9\frac{3}{4}d = 567q$ ;  $\pounds 2 = 1920q$ .

... fract<sup>a</sup>, req<sup>d</sup>. =  $\frac{667}{1620}$  =  $\frac{189}{640}$ , ... dec<sup>l</sup>, req<sup>d</sup>. = 189  $\div$  640 = 2953152; or thus,

 $\begin{array}{c|c} 4\\ 12\\ \hline 9.75\\ 4,0\\ \hline 11.8125\\ \hline \hline 2253125\\ \hline \end{array} \begin{array}{c} We first reduce \frac{3}{2}d. to the decl. of 1d., by divs. \\ 3d. by 4, which = .75d., next 9.75d. to the decl. \\ of 1s., by divs. by 12, which = .8125s., then \\ 11.8125s. to the decl. of £2, by divs. by 40 \\ \hline which = \pounds.2953125.\\ \hline \end{array}$ 

# Ex. LXIII.

Reduce.

(1) 1 qr., 5 lbs. to the decl. of a cwt.

- (2) \$2.50 to the decl. of \$10.
- (3) 3 hrs., 30' to the dec<sup>1</sup>. of a day.
- (4) 3 ro., 11 per. to the decl. of an acre.
- (5)  $6\frac{1}{2}d$ . to the dec<sup>1</sup>. of a shilling.
- (6) 31 in. to the decl. of 2 furlongs.
- (7) 2 oz., 13 dwt. to the dec<sup>1</sup>. of a lb.
- (8) 4 lbs., 2 sc. to the decl. of an oz.

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#### MISCELLANEOUS EXAMPLES.

- (9) 2 sq. ft. 73 in. to the dec<sup>1</sup> of a sq. yd.
- (10) 1 lb. Troy to the dec<sup>1</sup>. of a lb. Avoir.
- (11) 10s. 9d. to the dec<sup>1</sup>. of a  $\pounds$ .
- (12) 17s. 7d. to the dec<sup>1</sup>. of a  $\pounds$ .
- (13) 2 wks., 6<sup>1</sup>/<sub>2</sub> dys. to the dec<sup>1</sup>. of 4 dys. 3 hrs.
- (14) 2 lbs., 14 oz. to the dec<sup>1</sup>. of 18 lbs.

#### Ex. LXIV.

#### MISCELLANEOUS EXAMPLES.

#### PAPER I.

(1) Define a unit; a number. Into what classes are numbers divided? Explain the difference between them. Define Notation and Numeration.

(2) Write down in words the following numbers :

70340; 125004321; 5607605213403; and express by numbers eight hundred and ten thousand four hundred and one; sixty-four billions two millions six hundred and forty-six thousand and two.

(3) (1) Add together one million eighteen thousand two hundred and sixty-nine; twenty thousand nine hundred and seventy-nine; one hundred millions one thousand and fifty; fifty-four billions three thousand; four hundred millions and six; nine hundred and ninety-nine thousand nine hundred and ninety. (2) Subtract 300725 from 400001.

Explain clearly why you carry 1 when you borrow ten.

(4) (1) Multiply 268936785 by 5689, and verify by division.
(2) Divide 27027027027 by 6974, and verify by multiplication.

(5) The product is 99626417315464, the multiplier 72568; what is the multiplicand ?

(6) In 12 mi., 2 fur., 6 per., how many inches? Shew that your result is correct.

#### PAPER IL.

(1) When is a number said to be a multiple of another number? What is a common multiple? What is the least common multiple of two or more numbers? Find L. C. M. of 27, 36, 42, 48.

(2) Explain the meaning of the signs, +, -, =. When can questions in Addition be performed by Multiplication.

(3) A cask is required to be exactly filled by any one of the following measures: 1 pint, 2 pints, 3 pints, 5 pints, 6 pints, or 9 pints; find the smallest cask for the purpose.

(4) The forewheel of a waggon is 8 feet round, and the hind-wheel fourteen; how many feet will the waggon travel over before each wheel shall have made a number of complete turns? How often will this happen in 1000 feet?

(5) The length and cost of building the undernamed Canadian Canals, were as follows: The Rideau Canal, 1264 miles, \$4380000; the St. Lawrence Canal, 404 miles, \$8550-000; the Ottawa Canal, 104 miles, \$1500000; the Chambly and St. Ours Lock, 114 miles, \$550000; the Welland Canal and feeder, 504 miles, \$7000000; the Burlington and Desjardins Bridge cost \$560000. Find (1) the total length of the above canals, (2) their total cost, and (3) the average cost per mile, excluding the Burlington and Designations Bridge.

(6) Define a vulgar fraction? Distinguish between a vulgar and decimal fraction? Give an example of the different kinds of vulgar fractions?

#### PAPER III.

(1) Simplify (1)  $2\frac{1}{4}(\frac{1}{6}+\frac{2}{3}) + \frac{4}{5}(\frac{2}{3}-\frac{1}{7})$ .

 $(2) 2\frac{1}{4} \left\{ \left(\frac{1}{6} + \frac{2}{3}\right) + \frac{4}{9} \left(\frac{2}{3} - \frac{1}{7}\right) \right\}.$ 

(2) A person who owns  $\frac{1}{2}$  of a steam-vessel, sells  $\frac{3}{4}$  of his share for \$15000; what is the remaining part of his share worth?

(3) Simplify (1)  $\frac{7}{12} (8\frac{1}{4} - 2\frac{1}{2}) - \frac{1}{2} (\frac{3}{2} - \frac{1}{4})$ (2)  $\frac{7}{12} \left\{ (8\frac{1}{4} - 2\frac{1}{2}) - \frac{1}{2} (\frac{3}{2} - \frac{1}{4}) \right\}$ 

(4) A clerk copied  $\cdot 55$  of £5 instead of  $5 \cdot 5$  of £5, what was the amount of the error?

(5) It takes 87 yds. of carpet, 1.25 yd. wide, to cover a room, how many more yds. will it take, if the width be 75 yd?

(6) A gave 5 of an orange to B; 3 of what remained to C; how much of the orange had A left for himself?

#### PAPER IV.

(1) A drover sold  $\frac{1}{3}$  of his flock to A,  $\frac{1}{4}$  of the remainder to B, and the rest to C. How many had he at first, supposing C got 32?

(2) Add together 13 $\frac{1}{2}$ , 56 $\frac{3}{4}$ , and 14 $\frac{6}{5}$  by vulgar and decimal fractions, and shew that the results coincide.

(3) The product of two decimals is 033372; one of them is 2.7; find the other.

(4) Add together £27. 6s. 9½d., \$17.22, £19. 5s. 8d., \$198.05, £3. 12s. 7d. The answer to be in decl. currency.

(5) At a football match there were 875 as many on one side as on the other, and the players on both sides were equal in number to 625 of the lookers on; if there were 21 on the smaller side, how many were playing on the other side, and how many were looking on?

(6) If in a cricket match one side scores '014 of  $1\frac{2}{5}$  of  $\frac{1\frac{1}{5}}{52}$ 

of  $\frac{5}{7}$  of 4.5 of  $\frac{3}{2} + \frac{1}{2}$  of 713 of the score made by the other side; which side wins?

#### PAPER V.

(1) C owes B 6 of what B owes A, B gives C 5s to put the accounts between them all straight. What is B's debt to A?

(2) Out of a bag of silver, I take 50s. more than '5 of the whole sum which it contained; then 30s. more than '2 of what then remained; and then 20s. more than '25 of what then remained; after this 10s. remained. What did the bag contain at first?

(3) A bath, containing 286 cub. yds. has two inlets A and B, which respectively supply 26 cub. yds. in  $3\frac{1}{2}$  hrs., and  $12\frac{1}{2}$  cub. yds. in  $2\frac{1}{2}$  hrs.; and also an outlet C, which discharges 11.375 cub. yds. in  $1\frac{3}{4}$  hrs., if the bath be empty, and A and C open for 12 hrs., and then B also open, in what time will 75 of it be filled?

Make out the following bills :

(4) 500 envelopes at 44 cents per 100, 3 boxes of elastic bands at 33 cents per box,  $\frac{1}{2}$  a gross of penholders at 19 cents per doz.  $\frac{1}{2}$  reams of foolscap at 21 cents per quire, 4 dozen quill pens at 9 cents per doz., 13 note books at 27 cents each, and 250 official envelopes at 48 cents per 100.

(5) A loin of lamb  $(7\frac{1}{2}$  lbs.) at 10 cents per lb., a haunch of mutton  $(19\frac{1}{2}$  lbs.) at 8 cents per lb., a pork ham (18 lbs.) at 15 cents per lb.,  $5\frac{1}{2}$  lbs. of suet at 10 cents per lb., and 9 chops at 4 cents each.

( $\hat{6}$ ) 17 yds. calico at 19 cents per yd.,  $25\frac{1}{2}$  yds. at 55 cents per yd.,  $34\frac{1}{2}$  yards of flannel at 60 cents per yd., 14 pairs of stockings at 38 cents a pair, and 5 pairs of gloves at \$12 per doz.

# SECTION V.

#### RATIO AND PROPORTION.

105. Numbers are divided into two classes, ABSTRACT and CONCRETE. One, or the number one, when the unit does not refer to any particular object, is an *abstract* number. One, in the expression one pound, when the unit refers to a particular object, viz. "a pound," is a *concrete* number.

106. We may ascertain the relation which one abstract number bears to another abstract number or one concrete number to another concrete number of the same kind, by expressing the first number as a fraction of the second; thus the relations which 12 bears to 3, and 3 to 12 are expressed by the fractions  $\frac{12}{3}$  or  $\frac{1}{1}$ , and  $\frac{3}{12}$  or  $\frac{1}{4}$ ; also the relations which 12s. bears to 3d., or 144d. to 3d., and 3d. to 12s., or 3d. to 144 48 3 1

144*d*. are expressed by the fractions  $\frac{144}{3}$  or  $\frac{48}{1}$ , and  $\frac{3}{144}$   $\frac{1}{48}$ 

107. The relation of one number to another in respect of magnitude is called RATIO. The Ratio of one number to another may be expressed by the fraction which the first is of the second.

108. The Ratio of one number to another is often denoted by placing a colon between them. Thus the ratios of 12 to 3 and 3 to 12 are denoted by 12:3 and 3:12. Hence it follows that  $12:3=\frac{12}{3}$ , and  $3:12=\frac{3}{12}$ .

109. The two numbers which form a Ratio are called its *terms*; the former term is called the ANTECEDENT, the latter the CONSEQUENT. Since 3d. reduced to the fraction of 12s.

 $=\frac{1}{144}$ , it is clear that when we have two concrete numbers

of the same kind, but of different denominations, we must, in order to find their ratio, reduce them to one and the same denomination, and may then treat them as abstract numbers 110. When two Ratios are equal, in other words, when they can be expressed by the same fraction, they are said to form a PROFORTION, and the four numbers are called PROFORTIONALS. Thus the ratio of 8 to 9 is equal to that of 24 to 27, for  $8:9=\frac{8}{9}$ , and  $24:27=\frac{24}{27}=\frac{8}{9}$ . The Ratios being equal, Proportion exists among the numbers 8, 9, 24, 27; and those numbers are Proportionals.

111. The existence of Proportion between the numbers 8, 9, 24, 27 is denoted thus, 8:9 = 24:27, or 8:9:24:27, which is usually read thus, 8 is to 9 as 24 is to 27.

112. In any Proportion, as 8:9::24:27, the product of the 1st and 4th, i.e. the extreme terms = the product of the 2nd and 3rd, i.e. the mean terms;

 $\frac{8}{9} = \frac{24}{27}; \therefore \frac{8}{9} \times 9 \times 27 = \frac{24}{27} \times 9 \times 27, \text{ or } 8 \times 27 = 24 \times 9.$ 

113. If four numbers be proportionals when taken in a certain order, they will also be proportionals when taken in the contrary order. For instance, 8, 9, 24, 27 are proportionals;

 $\therefore \frac{8}{9} = \frac{24}{27}; \therefore 1 \div \frac{8}{9} = 1 \div \frac{24}{27}; \text{ or } \frac{9}{8} = \frac{27}{24}, \text{ or } \frac{27}{24} = \frac{9}{8};$  $\therefore 27: 24:: 9: 8.$ 

114. If any three terms of a proportion be given, the remaining term may always be found.

For since in any Proportion

1st term × 4th term = 2nd term × 3rd term;  $\therefore$  1st term =  $\frac{2nd \times 3rd}{4th}$ , 2nd term =  $\frac{1st \times 4th}{3rd}$ , 3rd term =  $\frac{1st \times 4th}{2nd}$ , 4th term =  $\frac{2nd \times 3rd}{1st}$ .

Ex. 1. Find the 4th term in the proportion 2, 3, 18.

2:3::18:4th term; ... 4th term = 
$$\frac{3 \times 18}{2} = 27$$
.

Ex. 2. Find the 2nd term in the proportion 8, 32, and 24.

8 : 2nd term :: 32 : 24;  $\therefore$  2nd term =  $\frac{8 \times 24}{22} = 6$ .

#### Ex. LXV.

Find the 4th term in each of the following proportions :

(1)	4:9:12:	(2) 32:9::24:
(3)	4:6::10:	$(4). \frac{1}{2}: \frac{1}{3}:: \frac{1}{4}:$
(5)	•05 • •8 • •79 •	(6) $3 \cdot 10 \cdot 4 \cdot 5$

Find the 2nd term in each of the proportions :

(7)  $\frac{5}{7}$ : ::  $\frac{10}{21}$ :  $\frac{16}{27}$ . (8) 1.2: :: 1.3: .39.

Find the 1st term in each of the proportions :

# (9) $: \frac{9}{14} : \frac{7}{13} : \frac{1}{3}$ . (10) $: 4 \cdot 22 : 17 \cdot 6 : 23\frac{2}{5}$ .

#### RULE OF THREE.

115. The RULE OF THREE is a method by which we are enabled, from three numbers which are given, to find a fourth which shall bear the same ratio to the third as the second to the first; in other words, it is a Rule by which, when three terms of a proportion are given, we can determine the fourth.

116. RULE. Find out of the three quantities which are given, that which is of the same kind as the fourth or required quantity; or that which is distinguished from the other terms by the nature of the question: place this quantity as the third term of the proportion.

Now consider whether, from the nature of the question, the fourth term will be greater or less than the third; if greater, then put the larger of the other two quantities in the second term, and the smaller in the first term; but if less, put the larger in the first term and the smaller in the second term.

Take care to reduce the first and second terms to one and the same denomination, and also to reduce the third so that it may be wholly in one denomination; remembering, however, that if the quantities involved be all of the same kind, it is unnecessary to reduce all the three terms to the same denomination, but only the first and second terms to one and the same denomination, and the third to a single denomination, which will not necessarily be the same as the former. When the terms have been properly reduced, multiply the second and third together, and divide by the first, treating all three as abstract numbers. The quotient will be the answer to the question, in the denomination to which the third term was reduced.

#### RULE OF THREE.

If 19 bushels of potatoes cost \$15.20, how many bushels can be bought for \$83.20? Since 19 bush. is of the same kind as the reqd. term, viz., bus., we make 19 bus. the 3rd. term ; since \$83.20 can buy more bus. than \$15.20, we make \$83.20 the 2nd. term, and \$15.20 the 1st. term :

> \$ c. \$ c. bus.

15.20 : 83.20 :: 19 : no. of bus. req<sup>4</sup>.

or 1520 cts. : 8320 cts. :: 19 bus. : of bus. reqa.

... no. of bus. req<sup>4</sup>. 
$$=\frac{8320 \times 19}{1520} = 104.$$

Ex. 2. A gentleman hired a servant for the year 1865 for £32. 13s. 111d., the man left his service on the evening of the last day of June: what amount of wages ought to be paid to him?

From Jan. 1 to June 30, both included, there are (31 + 28 + 31 + 30 + 31 + 30) days = 181 days;

We place £32. 13s. 111d., the given quantity of the reqd. kind, in the 3rd. term ; wages for 181 days will be less than wages for 365 days, ... place 181 days in the 2nd. term, and 365 days in the 1st. term.

days. days. s. d. £

or 365 days : 181 days :: 31390q......in q.

 $31390 \times 181$  $\therefore$  req<sup>d</sup>. am<sup>t</sup>. of wages =  $-q. = \pounds 16. 4s. 3\frac{1}{2}d.$ 365

Ex. 3. A bankrupt can pay 9s.  $0\frac{1}{2}d$ . in the £, and his assets amount to £1069. 3s. 61d.; find the amount of his debts.

For every asset of 9s.  $0\frac{1}{2}d$ . he owes £1,  $\therefore$  place £1 in the 3rd term.

9s. 0<sup>1</sup>/<sub>2</sub>d. : £1069. 3s. 6<sup>1</sup>/<sub>2</sub>d. :: £1 : am<sup>t</sup>. of debts in £'s, or 217 half-pence : 513205 half-pence :: £1 : amt. of debts in £'s;

> $\therefore$  am<sup>t</sup>. of debts in £'s =  $-\frac{1}{217}$ -=2365.

Ex. 4. If '0625 of 1 lb. cost '458s.; what will '075 of a ton cost ?

> 1b. ton

'0625 : '075 :: '458 : req<sup>d</sup>. price in shillings, lb.

lbs. or '0625 : '075 × 20 × 112 :: '458 : req<sup>d</sup>. price in shillings •458 × •075 × 20 × 112 . price =

 $-s. = \pm 61, 11s. 1.248d.$ .0625

Ex. 5. A owned  $\frac{1}{17}$  ths of a ship, and sold  $\frac{1}{17}$  of  $\frac{2}{5}$  of his share for  $\pm 12\frac{4}{35}$ ; what was the value of  $\frac{1\frac{1}{4}}{4\frac{1}{4}}$  of  $\frac{2}{5}$  ths of the vessel?

 $\begin{array}{l} \overset{a}{_{11}} \text{ of } \overset{s}{_{5}} \text{ of } \overset{1}{_{17}} : \frac{14}{4\frac{1}{4}} \text{ of } \overset{2}{_{5}} :: \pounds 12_{\mathfrak{I}} \overset{4}{_{3}} : \text{ req}^{4} \text{ value in } \pounds \overset{*}{_{5}} \text{ ,} \\ \\ \text{ or } \frac{2 \times 4}{11 \times 3 \times 17} : \overset{\sharp}{_{\mathcal{A}}} \times \frac{\mathcal{A}}{17} \times \frac{2}{_{\mathcal{B}}} :: \pounds \frac{400}{33} : \text{ req}^{4} \text{ value in } \pounds \overset{*}{_{5}} \text{ ;} \\ \\ \therefore \text{ req}^{4} \text{ value in } \pounds \overset{*}{_{5}} s = \frac{400 \times 2}{33 \times 17} \times \frac{11 \times 3 \times 17}{2 \times 4} = 100. \end{array}$ 

Note 1. There are certain examples in which, at first sight, more than three terms appear to be given, but they, in certain cases, come under this Rule, as in the following instances:

Ex. 6. If the carriage of 5 cwt., 7 lbs., for 84 miles cost £3. 18s. 4d., what will it cost to have 21 cwt., 1 qr., 14 lbs. carried the same distance?

84 miles may be left out of consideration, the distance in both cases being the same.

...5 cwt.,7 lbs.: 21 cwt., 1 qr., 14 lbs.:: £3.18s.4d.: req<sup>4</sup>.cost. whence, req<sup>4</sup>. cost=£16. 10s. S<sup>\*</sup><sub>4</sub>d. <sup>5</sup><sub>8</sub>q.

Ex. 7. If 12 men can reap a field in 4 days, in what time can the same work be performed by 32 men?

32 men require less than 4 days to perform the work .

 $\therefore$  req<sup>d</sup>. time =  $\frac{12 \times 4}{32}$  days =  $1\frac{1}{2}$  days.

Note 2. Examples such as the following are easily worked by Rule of Three.

Ex. 8. A gentleman after paying an income-tax of 7d. in the £, has £248. 10s. 8d.; what was his gross annual income? After paying inc<sup>e</sup>. tax on £1, he had £1 less 7d., or 19s. 5d.

:. 19s. 5d. : £248. 10s. 8d. :: £1. : req<sup>d</sup>. income ;

whence, req<sup>d</sup>. income =  $\pounds 256$ .

Ex. 9. A hare, pursued by a greyhound, was 130 yards before him at starting; whilst the hare ran 5 yards the dog ran 7 yards; how far had the hare gone when she was caught by the greyhound?

Since the dog gains 2 yds. on every 5 yds. which the hare

#### RULE OF THREE.

runs, we require to find how many yards the hare must run for the dog to gain 130 yds.

... 2 yds. : 130 yds. :: 5 yds. : no. of yds. the hare must run;  $130 \times 5$ 

... no. of yds. req<sup>d</sup>. =  $\frac{100 \times 0}{2}$  = 325.

#### Ex. LXVI.

(1) If 8 bushels of wheat cost \$16, what will 24 bushels cost at the same rate?

(2) If 2 bushels of cats cost \$1.10, how much will 33 bushels cost?

(3) If 9 bushels clover seed cost \$36, how much will 4 bus. 20 lbs. cost?

(4) When oats are selling at 55 cents a bushel; how many bushels can be bought for \$21.25?

(5) The price of a bushel of pease being 84 cents; how many bushels can be bought for \$17.20?

(6) Find the value of a silver salver, weighing 21 lbs., 4 oz. at 6s. 5d. an oz.

(7) How much cheese at 16 cts. per lb. can be bought for \$462.36?

(8) A bankrupt, who owes \$23856, can pay \$10496.64; what will be the dividend in the \$?

(9) A pensioner received \$106.14 for the year 1864; find the amount of his daily pension.

(10) I mile of road cost \$393.75; what will 20 mi., 5 fur., 22 yds. of the same kind of road cost?

(11) What weight of sugar may be bought for \$449.28, when the cost of 6 cwt., 2 qrs. is \$133.12.

(12) The taxes on a house rated at 183.75 amount to 332.15; the taxes on another house in the same village amount to  $236.66\frac{1}{2}$ ; find the rateable value of the 2nd house.

(13) A bankrupt's debts amount to \$10000, and his property to \$3875, what will each of his creditors lose in the \$?

(14) A ship was provisioned for a crew of 84 men for 5 months; how much longer would the provisions last, if a a crew of only 60 men were taken on board?

(15) A merchant exchanged 1134 yds. of velvet for 5313

115

H

yds. of silk at 3s. 4½d. a yd.; find the value of the velvet a yd.?

(16) What are the effects of a bankrupt worth, whose debts amount to  $\pm 3057$ . 12s., and who can pay 17s. 6d. in the  $\pm$ ?

(17) A man on the average walks over 10 ft., 8 in. in 4 steps, what number of steps will be take between two places, a distance of 1 mi., 1280 yds. apart?

(18) If 31 ac., 3 ro., 9 po., 21 yds. of ground cost £3025 12s.  $4\frac{1}{2}d$ ., what will be the price of 49 ac., 3 ro., 38 po.,  $2\frac{3}{4}$ yds. of ground of the same quality?

(19) A bankrupt pays 59 cts. in the \$; what will be lost on a debt of \$13675?

(20) How many minutes must a boy, who runs 6 mi. an hour, start before another boy, who runs 7<sup>1</sup>/<sub>4</sub> mi. an hour in order that they may be together at the end of 10 mi.?

(21) Two boats start in a race, and one of them gains 5 ft. upon the other in every 55 yds.; how much will it have gained at the end of half a mile?

(22) How many pairs of mits at 45 cts. a pair should be exchanged for 36 dozen pairs of stockings at 55 cts. a pair?

(23) How many men would perform in 168 days a piece of work, which 108 men can do in 266 days?

(24) If an incorporated village be rated at \$12571.87½ and a rate be granted of \$419.06½; how much is the rate in the \$? How much will be paid by a house rated at \$1734.37½.

(25) A gentleman's income in 1863 was \$2500, out of which he saved \$994.37<sup>1</sup>/<sub>2</sub>; find his average daily expenditure.

(26) If 100 men can finish a piece of work in 27 days, how many men will finish it in 20 days?

(27) A special train on the Grand Trunk Railway, which travels at the uniform rate of 44 ft. in a second, leaves Belleville for Toronto, a distance of 109 miles, at 8 o'clock A. M.; at what time will the train reach Toronto.

(28) A bankrupt owes to one creditor a certain sum, to each of two others \$1250, to each of three others \$816; his property is worth \$1718.75, and he can pay 22 cts. in the \$. How much will the first creditor lose?

(29) If, when wheat is 42s. a qr. (8 bus.), the 4 lb. los.

costs  $4\frac{1}{2}d$ , what ought the 4 lb. loaf to cost when wheat is 70s. a qr.?

(30) In what time ought 10 men to perform the same work, which 5 men and 5 boys can perform in 15 days, it being given that 3 men can perform the same amount of work as 5 boys?

(31) Find a 4th proportional to 1 lb., 10 oz., 10 dwts.; 1 oz.; and £6. 3s. 9d.

(32) How much might a person have spent in Jan., 1864, who wished to save in that year \$250 out of an income of \$2034.50?

(33) A person, after paying an income-tax of 6d. in the £, has £877. 10s. left, find his original income.

(34) Find (1) the income which pays £29. 3s. 4d. tax at the rate of 7d. in the  $\pounds$ ; (2) the income from which, after paying tax at the same rate, the remainder is £932.

(35) A piece of gold at £3. 17s.  $10\frac{1}{2}d$ . per oz. is worth £150; what will be the worth of a piece of silver of equal weight at 54s. 6d. per lb.?

(36) A certain piece of work was to be done by 25 men in 16 days; after 4 days 15 men go away; how long will it take the rest of the men to finish the work?

(37) A person after paying for the 1st half of a year an income-tax of 1 ct. in the , and for the 2nd half one of 1 $\frac{1}{2}$  cts. in the on his income, has \$1855 left; what was the income on which he paid?

(38) If  $\frac{2}{3}$  of a qr. of wheat cost 54s., what will be the price of  $\frac{4}{3}$  of a bus.?

(39) If  $\frac{12}{15}$  of a cwt. cost £7 3s., what will  $\frac{6}{11}$  of a ton cost?

(40) If  $\frac{1}{120}$  of  $\frac{2}{3}$  of  $2\frac{1}{2}$  of 40 lbs. of beef cost  $1\frac{3}{50}d$ , how many lbs. can be bought for £1. 6s. 6d. ?

(41) A clock marks the true time on Sunday morning at 6 o'clock, and on Tuesday at noon it has gained 24 minutes, what will be the true time when it shews 1 o'clock on Saturday afternoon?

(42) The hour and minute hands of a watch are together at 12 o'clock, when will they next be together?

(43) If 5 lbs. of sugar cost '0703125 of \$4, what will '0625 cwt. of the same sugar cost ?

(44) A certain piece of work can be done in 18 days by

4 men, 7 women, or 9 boys; how long will the same work occupy 5 men, 4 women, and 2 boys?

(45) If after selling  $\frac{3}{5}$  ths of an estate, I sell  $\frac{1}{5}$  of  $\frac{7}{5}$  of the remainder for  $1\frac{1}{5}$  of  $\frac{4}{5}$  of  $\pounds 600\frac{6}{5}$ , what is the value of  $\frac{2}{5}$  rds of it?

(46) What will be the value of a gold cup weighing 2.683 lbs.; when 1 oz. of it is worth £4.09?

(47) 4 men and 5 boys earn \$22.12 in 7 days, and 3 men and 8 boys earn \$28.98 in 9 days; in what time will 12 men and 12 boys earn \$186.48?

(48) A can do a piece of work in 5 hours, B in 9 hours, and C in 15 hours. How long will it take C to finish the work, after A has worked at it for 40 minutes, and B for  $1\frac{1}{2}$ hours?

(49) If a garrison of 1500 men have provisions for 13 mo., how long will their provisions last, if at the end of 2 mo. they be reinforced by 700 men?

(50) Two men start at S.30 A.M., one from Toronto and the other from Whitby, a distance of 30 miles, and they approach each other at the rates of  $4\frac{1}{2}$  and 3 miles an hour; at what time will they meet, and at what distance from a place, which is 2 miles nearer to Toronto than Whitby?

(51) Two trains respectively 210 feet and 180 feet in length are going in opposite directions, the first at the rate of 24 miles per hour, and the other at the rate of 27 miles per hour; find how long they will take to pass each other  $^{\circ}$ 

#### DOUBLE RULE OF THREE.

117. The DOUBLE RULE OF THREE is a shorter method of working out such questions as would require two or more applications of the Rule of Three.

118. For the sake of convenience, we may divide each question in the Double Rule of Three into two parts, the supposition and the demand; the supposition being the part which expresses the conditions of the question, and the demand the part which mentions the thing demanded or sought. In the question, "If the carriage of 15 cwt. for 17 miles cost \$21, what would the carriage of 21 cwt. for 16 miles cost?" the words "if the carriage of 15 cwt. for 17 miles cost \$21, what would the carriage of 15 cwt. for 17 miles cost \$21, what would the carriage of 15 cwt. for 16 miles cost?" form the supposition; and the words "what would the carriage of 21 cwt. for 17 miles cost \$21," form the supposition; and the words "what would the carriage of 21 cwt. for 16 miles cost?" form the demand.

Adopting this distinction, we may give the following Rule for working out examples in the Double Rule of Three.

119. RULE. Take from the supposition that quantity which corresponds to the quantity sought in the demand; and write it down as a third term. Then take one of the other quantities in the supposition and the corresponding quantity in the demand, and consider them with reference to the third term only (regarding each other quantity in the supposition and its corresponding quantity in the demand as being equal to each other); when the two quantities are so considered, if from the nature of the case, the fourth term would be greater than the third, then, as in the Rule of Three, put the larger of the two quantities in the second term, and the smaller in the first term; but if less, put the smaller in the second term, and the larger in the first term.

Again, take another of the quantities given in the supposition, and the corresponding quantity in the demand; and retaining the same third term, proceed in the same way to make one of those quantities a first term and the other a second term.

If there be other quantities in the supposition and demand, proceed in like manner with them.

In each of these statings reduce the first and second terms to the same denomination. Let the common third term be also reduced to a single denomination if it be not already in that state. The terms may then be treated as abstract numbers.

Multiply all the first terms together for a final first term, and all the second terms together for a final second term, and retain the former third term. In this final stating multiply the second and third terms together and divide the product by the first. The quotient will be the answer to the question in the denomination to which the third term was reduced.

Ex. 1. If 5 men earn £18, 15s. in 12 weeks, how much will 16 men earn in 20 weeks?

By the Rule,

5 men : 16 men 12 wks. : 20 wks. } :::£18 15s.

16 men will earn more money than 5 men in a given time; in 20 wks. more money will be earned than in 12 wks. by a given no. of men.

... 5 × 12 : 16 × 20 :: 375s. : no. of shillings req<sup>d</sup>.;

"." no. of shillings requ. =  $\frac{16 \times 2\emptyset \times 3\pi \beta}{\cancel{5} \times \cancel{12}}$ = 2000s. = £100.

Ex. 2. If 16 horses eat 56 bus. of corn in 32 days, in how many days will 8 horses eat 84 bus.?

8 horses : 16 horses  $\}$  :: 32 days  $\stackrel{A}{}$  given no. of bus. will last 56 bus. : 84 bus.  $\}$  :: 32 days  $\stackrel{A}{}$  given no. of bus. will last a $\therefore$  no. days req<sup>4</sup>. =  $\frac{16 \times 84 \times 32}{8 \times 56}$ = 96. given no. of horses more days than 56 bus.

Ex. 3. If 15 pumps, working 8 hours a day, can raise 1260 tons of water in 7 days; how many pumps, working 12 hours a day, will be required to raise 7560 tons of water in 14 days?

12 hrs. : 8 hrs. 1260 tons : 7560 tons 14 days: 7 days	:: 15 pumps
$  \frac{1}{8 \times 7560 \times 7 \times 7560} $	15 _ 20
$=$ $12 \times 1260 \times 1260 \times 1200 \times 12000 \times 12000 \times 12000 \times 12000 \times 12000 \times 12000 \times 120000 \times 1200$	$\frac{1}{14} = 30.$

Fewer pumps works. 12 hrs. a day are req<sup>4</sup> to raise a given weight of water in a given no. of days than if they worked 8 hrs a day; more pumps are req<sup>4</sup>. to raise 7560 tons than to raise 1260 tons in a given no. of

days, work<sup>g</sup>. a given no. of hrs. each day; fewer pumps are req<sup>d</sup>., work<sup>g</sup>. for 14 days a given no. of hrs. each day, to raise a given weight of water, than if they worked only for 7 days.

Ex. 4. If 25 men can perform a piece of work in 16 days working 12 hours a day, in what time will 20 men perform a similar piece of work 4 times as large, when they work only 8 hours a day?

Call the 1st piece of work 1, then the 2nd piece will = 4.

20 men : 25 men 1 : 4	:: 16 days.	$\begin{array}{r} \therefore \text{ no. of days req}^{d}.\\ \underline{25 \times 4 \times 12 \times 16}_{-120} \end{array}$
8 hrs. : 12 hrs.	)	$-\frac{20 \times 8}{20 \times 8}$

Ex. 5. A contractor engages to make a road  $5\frac{1}{2}$  mi. long in 160 days; but after employing 135 men upon it for 100 days, he finds that only 3 mi., 700 yards are completed; how many extra men must he employ in order to complete his contract?

 $\begin{array}{c} \mathbf{3}_{2} \text{ mi.} -3 \text{ mi.}, 700 \text{ yds.} = 9680 \text{ yds.} -5980 \text{ yds.} = 3700 \text{ yds.} \\ 5980 \text{ yds.} : 3700 \text{ yds.} \\ 60 \text{ days} : 100 \text{ days.} \end{array} \right) :: 135 \text{ mon} = \frac{3700 \times 100 \times 135}{5980 \times 60} = 139 \frac{44}{199} \frac{4$ 

... 140 men must be employed, or 6 additional men.

#### Ex. LXVII.

(1) If 10 sacks of oats supply 12 horses for 4 weeks, how long will 15 sacks supply 9 horses?

(2) If 42 men finish a work in 36 days, how many will finish twice as great a work in 27 days?

(3) If 60 men in 36 days finish a work, in how many days will 135 men finish four times as great a work?

(4) If 104 tons carried 34 miles cost \$87.36, what will 102 tons carried 122 miles cost?

(5) If a man with a capital of \$100000 gain \$2500 in 3 months, what sum will he gain with a capital of \$1500000 in 7 months?

(6) If 21 cwt. be carried 40 miles for \$2.80, how far ought 7 cwt. to be carried for \$4.06?

(7) If 7 horses be kept 20 days for \$70, what will it cost to keep 45 horses for 9 days?

(8) If 140 horses eat 560 bus. of oats in 16 days, how many horses may be kept for 24 days on 1200 bus. of oats?

(9) If with a capital of \$5000 a person gains by trade \$250 in 16 months, in how many months will he gain \$625 with a capital of \$2000?

(10) If a regiment of 1878 soldiers consume 702 qrs. of wheat in 336 days, how many qrs. will an army of 22536 men consume in 112 days?

(11) If 6 horses can plough  $17\frac{1}{2}$  acres in 4 days, how much land can 24 horses plough in  $2\frac{1}{2}$  days?

(12) If £240 be paid for bread for 49 persons for 20 mo., when wheat is 48s. a qr.; how long will £234 find bread for 91 persons, when wheat is £2. 16s. a qr.?

(13) If 100.8 lbs. of flour support 20 men for 3 days, how many men will 46.305 cwt. support for 7.35 weeks?

(14) If 26 men can reap a field of 85 ac. in 12 days, how many men will reap another similar field one-half the size of the 1st field in one-seventh part of the time?

(15) 3 men can do a piece of work in 6 days, if they work 10 hours a day; how long will it take 16 men to do twice the amount of work, when they are working at it 9 hours a day?

(16) If the wages of 25 men amount to £76. 13s. 4d. in 16 days, how many men must work 24 days to receive

£103. 10s., the daily wages of each of the latter being onehalf that of each of those of the former?

(17) If 6664 men, on half rations, consume 357 qrs. of wheat in 57 days, how many qrs. of wheat will 798 men, on full rations, consume in 119 days?

(18) If the 16 cts. loaf weighs 3:35 lbs., when wheat is \$1.14 a bus., what ought to be the price of wheat per bus., when 47:5 lbs. of bread cost \$3.20.?

(19) If when wheat is \$14.40 a qr., the 12 cts. loaf weighs 41bs., what should be the price of wheat per. qr., when 25 lbs. of bread cost  $37\frac{1}{2}$  cts.?

(20) If 4 men, each working 8 hrs. a day, take 11 days to pave a road 220 yds. long, and 35 ft. broad; how many days will 6 men, each working 12 hrs. a day, take to pave a road 175 yds. long, and 36 ft. broad?

(21) If 100 horses consume a stack of hay 20 ft. long, 11 ft., 3 in. broad, and 31 ft., 6 in. high, in 9 days, how long will a stack 18 ft. long, 5 ft. broad, and 14 ft. high supply 80 horses?

(22) If 3 men can dig a ditch 105 yds. long, 4 ft. deep, and 5 ft. wide in 10 days, how long will it take 5 men to dig a ditch 175 yds. long, 4½ ft. deep, and 6 ft. wide?

(23) If the 8 cts. loaf weighs 1 lb. 11 oz. 12 drs. when wheat is \$1.80 per bu., what ought the 12 cts. loaf to weigh when wheat is \$1.26 per bus.?

(24) If 5 horses require as much corn as 8 ponies, and 15 qrs. last 12 ponies for 64 days, how many horses may be kept 48 days for £41. 5s. when corn is 22s. a qr.?

(25) A contractor agrees to execute a certain piece of work in a certain time. He employs 55 men, who work 9 hrs. daily. When <sup>§</sup><sub>4</sub>ths of the time is expired, he finds that only <sup>§</sup><sub>7</sub>ths of the work is done. How many men must he employ during the remaining part of the time, working 11 hrs. daily, in order that he may fulfil his contract?

(26) If 5 pumps, each having a length of stroke of 3 feet, working 15 hours a day for 5 days, empty the water out of a mine; what must be the length of stroke of each of 15 pumps which, working 10 hours a day for 12 days, would empty the same mine, the strokes of the former set of pumps being performed 4 times as fast as those of the latter?

## PRACTICE.

# PRACTICE.

120. An Aliquot part of a number is such a part as, when taken a certain number of times, will exactly make up that number.

Thus, 4 is an aliquot part of 12; 6s. of 18s.

TABLES OF ALIQUOT PARTS.

Parts of a cust. (100 lbs.)

8:

Parts of a cut. (112 lbs.)

50 lbs. or 2 qrs. = $\frac{1}{2}$ cwt.	56 lbs. or 2 qrs. = $\frac{1}{2}$ cwt.
25 lbs. or 1 qr. = $\frac{1}{4}$ "	28 lbs. or 1 qr. = $\frac{1}{4}$
20 lbs. $=\frac{1}{5}$ "	$16 \text{ lbs.} = \frac{1}{7}$
10 lbs. $=\frac{1}{10}$ "	14 lbs. $=\frac{1}{8}$ "
5 lbs. $=\frac{1}{20}$ "	7 lbs. $=\frac{1}{16}$ "
Note The narts of a \$ the	4 lbs. $=\frac{1}{28}$ "
me as of the cwt (100 lbs)	2 lbs. $=\frac{1}{56}$
inc as of the cwt. (100 105).	
Parts of a £1.	Parts of a shilling.
$10s. = \frac{1}{2} \pounds 1.$	$6d. = \frac{1}{2}$ of 1s.
$6s. 8d. = \frac{1}{4}$	$4d. = \frac{1}{4}$
58. = 1 "	$3d_{2} = \frac{3}{4}$ "
48. = 1 "	$2d_{1} = \frac{1}{2}$
38 4d = 1 66	$11d = \frac{1}{4}$ "
2º 6d - 1 "	10 - 2 "
20.00 1	$\frac{100}{8d} - \frac{12}{-11}$ 66
10.9d - 1.46	$\frac{4}{1d} - \frac{16}{16}$
13.00 12	$\frac{1}{1}$ $-\frac{1}{24}$
18. 40. = 15	In. = 18
$13. 3a. = \frac{1}{16}$	Constraint and the second s
$18. = \frac{1}{25}$	

Note. In working examples in Practice, the above tables will often have to be varied; the knowledge, which the scholar now has, will render him expert in taking such aliquot parts as he may require in any particular example.

121. Practice is a short method of finding the value of any number of articles by means of *Aliquot Parts*, when the value of a unit of any denomination is given. Practice may be divided into Simple and Compound.

#### SIMPLE PRACTICE.

122. In this case the given number is expressed in the same denomination as the unit whose value is given; as, for instance, 27 bushels at \$1.30 per bushel.

The Rule for Simple Practice will be easily shewn by the following examples.

Ex. 1. Find the value of 1296 things at  $16s.10\frac{1}{2}d$ . each. The method of working such an example is the following : If the cost of the things be £1 each ;

then the total  $cost = \pm 1296$ .

·. cost at

10s. 0d.	each $= \frac{1}{2}$ of the above sum	=	648	•	0	•	0
1s. 3d.	$each = \frac{1}{2}$ the cost at 10s. each $each = \frac{1}{4}$ the cost at 5s. each	=	324 81	•	0	•	0
$0s. 7\frac{1}{2}d.$	each = $\frac{T}{2}$ the cost at 1s. 3d. each	=	40	•	10		0

 $\therefore$  by adding up the vertical columns, cost at 16s. 10<sup>1</sup>/<sub>4</sub>d. each =£1093.10.0

The operation is usually written thus :

	J.,	5.	a.	
$10s. = \frac{1}{2}$ of £1.	1296 .	0.	$0 = \cot at d$	El each.
$5s. = \frac{1}{2}$ of 10s.	648 .	0.	$0 = \cos t$ at :	10s. each.
$1s. 3d. = \frac{1}{2} \text{ of } 5s.$	324 .	0.	$0 = \cot at a$	5s. each.
$7\frac{1}{2}d. = \frac{1}{2}$ of 1s. 3d.	81.	0.	$0 = \cot at 1$	s. 3d. each.
	40.	10.	$0 = \cot at$	$l \frac{1}{2}d$ . each.
	£1002	10	$\overline{0}$ - and at 1	6. 101d anal

Note. The student must use his own judgment in selecting the most convenient 'aliquot' parts; taking care that the sum of those taken make up the given price of the unit.

Ex. 2. Find the value of 825 bushels of wheat at \$1.30 per bus.

If 1 bus. cost \$1, cost of 825 bus. = \$825 at \$1 each.

	\$825.00 = value at \$1 each.
20 cts. = $\frac{1}{2}$ of \$1.	165.00 = value at 20 cts. each.
$10 \text{ cts.} = \frac{1}{2} \text{ of } 20 \text{ cts.}$	82.50 = value at 10 cts. each.
	\$1072.50 = value at $$1.30 $ each.

#### Ex. LXVIII.

Find the value of,

- (1) 75 at \$2.25.
- (3) 910 at \$1.75.
- (5) 1075 at \$3.25.
- (7) 397 at £1. 1s.
- (9) 1324 at \$3.75.
- (11) 973 at 16s.  $8\frac{1}{2}d$ .

- (2) 105 at \$1.50.
- (4) 876 at \$2.20.
- (6) 1278 at \$1.871.
- (8) 250 at £2. 8s.
- (10) 2678 at £2. 7s. 6d.
- (12) 236 at £7. 58. 111

(13) 9978 at £8. 13s.  $8\frac{1}{2}d$ . (14) 15739 at £9. 17s.  $9\frac{3}{2}d$ . (15) 27835 at  $\$9.62\frac{1}{2}$ . (16) 37832 at \$18.90.

(17) A bankrupt whose debts amount to \$250215 pays 29 cts. in the dollar; what are his effects worth?

(18) A gentleman's gross income is \$12815, his rates and taxes amount to 25 cts. in the \$, find his net income.

(19) What will be the loss on a debt of £4970, if a dividend of 8s.  $10\frac{1}{2}d$ . in the £ be paid?

(20) What will be the total cost of  $83\frac{1}{2}$  yds. of calico @  $11\frac{1}{2}d$ . per yd., of  $57\frac{2}{3}$  yds. of flannel @ 1s. 10d. a yd., and of 118 yds. of ribbon @  $9\frac{2}{3}d$ . a yd.?

## COMPOUND PRACTICE.

123. In this case the given number is not wholly expressed in the same denomination as the unit whose value is given; as for instance, 1 cwt. 2 qrs., 14 lbs. at \$10.24 per cwt.

The Rule for *Compound Practice* will be easily shewn from the following examples.

Ex. 1. Find the value of 60 cwt., 3 qrs., 5 lbs. of sugar @ \$8.50 per cwt.

The method of working such an example is the following : The value of 1 cwt. of sugar being \$8.50;

value of 60 cwt. = $(\$8.50 \times 60)$	-	\$510.00
$2 \text{ qrs.} = \frac{1}{2} \text{ (value of 1 cwt.)}$	)	
$=\frac{1}{2}(\$8.50)$	=	\$4.25
$1 \text{ qr.} = \frac{1}{2} \text{ (value of 2 qrs.)}$		
$=\frac{1}{2}(\$4.25)$	=	$$2.12\frac{1}{2}$
5 lbs. = $\frac{1}{5}$ (value of 1 qr.)		1.1
$=\frac{1}{6}(\$2.12\frac{1}{2})$	-	\$0.421

Therefore adding up the vertical columns, value of 60 cwt. 3 qrs., 5 lbs.

= \$516.80

The operation is usually written thus :

$2 \text{ qrs.} = \frac{1}{2} \text{ cwt.}$	\$8.50 10	=	value of 1 cwt.	
	85.00	=	value of 10 cwt.	
	<u>6</u> 510.00	-	value of 60 cwt.	
	4.25	=	value of 2 qrs.	
$1 \text{ qr.} = \frac{1}{2} \text{ of } 2 \text{ qrs.}$ 5 lbs. = $\frac{1}{2} \text{ of } 1 \text{ qr.}$	2.12	=	value of 1 qr. value of 5 lbs.	
	\$516.80	=	value of 60 cwt., 3 grs., 5 lbs.	

Ex. 2. Find the value of 319 cwt., 3 qrs., 16 lbs., at £2. 12s. 6d. per cwt.

	£	8.	d.					
$2 \text{ qrs.} = \frac{1}{2} \text{ cwt.}$	2.	12	6	11	value	of 1	cwt.	
			10					
the second s	26 .	. 5	0	=	value	of 10	) cwt.	
			4					
	105 .	0	0	=	value	of 40	) cwt.	
			8					
	840.	0	0	=	value	of 32	0 cwt	
subtracting	2.	12	6	=	value	of 1	cwt.	
	837 .	7	6	=	value	of 31	9 cwt	
	1.	6	3	=	value	of 2	grs.	
$1 \text{ qr.} = \frac{1}{2} \text{ of } 2 \text{ qrs.}$	0.	13	11	==	value	of 1	qr.	
$14 \text{ lbs.} = \frac{1}{2} \text{ of } 1 \text{ qr.}$	0.	6	$6\frac{3}{4}$	=	value	of 14	lbs.	
$2 \text{ lbs.} = \frac{1}{7} \text{ of } 14 \text{ lbs.}$	0.	0	114	=	value	of 2	lbs.	
1	£839 .	14	41	:=	value	of 31	9 cwt	
			-	3 q	rs., 16	blbs.		Í

#### Ex. LXIX.

Find the value of

(1) 55 bus., 25 lbs. wheat @ \$1.20 per bushel.

(2) 16 cwt., 2 qrs., 20 lbs. of sugar @ 10 cts. per lb.

(3) 96 ac., 2 ro., 10 per. at \$15.50 per ac.

(4) 2 lbs., 8 oz., 13 dwt. at 7s. 1d. per oz.

(5) 15 yds., 2 ft., 7 in. at 12s. 6d. per yd.

(6) 28 sq. yds., 7 ft., 110 in. at £1. 7s. per sq. ft.

(7) 11 mls., 3 fur., 55 yds., at \$11000 per mile.

(8) What is the value of 5 tubs of butter, each of 2 of them containing  $57\frac{1}{2}$  lbs., and each of the rest  $73\frac{3}{4}$  lbs., at \$25 per cwt.?

(9) What will 3460 ft. of timber cost at \$5 per 100 ft.?

(10) What will 24650 bricks cost at \$4 per 1000?

(11) What will 46590 ft. lumber cost at \$10.25 per 1000 ft.? Find the amount of each of the following bills :

(12) 175 yds. calico at  $19\frac{1}{2}$  cts. a yd.,  $35\frac{1}{16}$  yds. flannel at  $55\frac{1}{2}$  cts. a yd.,  $96\frac{1}{17}$  yds. sheeting at  $70\frac{1}{2}$  cts. a yd.,  $104\frac{5}{9}$  yds. of Holland at  $32\frac{1}{2}$  cts. a yd.,  $12\frac{3}{9}$  yds. of ribbon at  $17\frac{1}{2}$  cts. a yd.

(13) 2513 lbs. of beef at 121 cts. a lb., 1911 veal at 11 cts.

#### SIMPLE INTEREST.

a lb.,  $35\frac{7}{2}$  lbs. of pork at  $8\frac{1}{2}$  cts. a lb.,  $17\frac{1}{2}$  lbs. lamb at  $6\frac{1}{2}$  cts. a lb.

(14)  $17\frac{5}{9}$  lbs. crushed sugar at  $12\frac{1}{2}$  cts. a lb.,  $18\frac{3}{4}$  lbs. cheese at  $17\frac{1}{2}$  cts. a lb.,  $5\frac{5}{15}$  lbs. of tea at 75 cts. a lb.,  $10\frac{5}{7}$  lbs. coffee at 40 cts. a lb.,  $7\frac{3}{4}$  lbs. honey at 25 cts. a lb.

Note 1. The scholar should bring the last three questions in the form of a bill, to the master.

#### INTEREST.

124. INTEREST (Int.) is the sum of money paid for the loan or use of some other sum of money, lent for a certain time at a fixed rate; generally at so much for each \$100 for one year.

The money lent is called THE PRINCIPAL.

The int. of \$100 for a year is called THE RATE PER CENT.

The principal + the interest is called the AMOUNT.

Interest is divided into Simple and Compound When interest is reckoned only on the principal or sum lent, it is SIMPLE INTEREST.

When the interest at the end of the first period, instead of being paid by the borrower, is retained by him and added as principal to the former principal, interest being calculated on the new principal for the next period, and this interest again, instead of being paid, is retained and added on to the last principal for a new principal, and so on ; it is COMPOUND INTEREST.

#### SIMPLE INTEREST.

125. To find the interest of a given sum of money at a given rate per cent. for a year.

RULE. Multiply the principal by the rate per cent., and divide the product by 100.

Note 2. The int. for any given number of years will be found by multiplying the int. for 1 year, by the number of years; and the int. for any part of a year may be found from the int. for 1 year, by Practice, or by the Rule of Three.

Note 3. If the interest has to be calculated from one given day to another, as for instance from the 30th of Jan. to the 7th of Feb., the 30th of Jan. must be left out in the calculation, and the 7th of Feb. must be taken into account, for the borrower will not have had the use of the money for one day till the 31st of Jan.

Note 4. If the amount be required, the int. has first to be

found for the given	a time, and the principal has then to be
Er 1 Find the	simple int of \$250 for one man at 0
cent. per appum.	simple int. of \$250 for one year, at 9 per
By the Rule,	or by the Rule of Three.
\$250	\$100 : \$250 :: \$9 : Int. req <sup>d</sup> .
9	
\$22.50	1 Int mod _ 250 × 9 _ 200 50
$\therefore$ Int.=\$22.50	100 = \$22.50.
Ex. 2. Find the	amount of £1376. 11s. 3d. at 43 per cent.
from Apr. 6 to Aug	. 30.
£. s. d. 1376 11 3	£. s. <b>d.</b> *1276 11 3
48	3
5506.5.0	4) 4129 . 13 . 9
1032 8 . 54*	£1032 . 8 . 5t
£65.38 . 13 . 5‡	
- 20	
8. 7·73 12	.•. Int for 1 yr. = $\pounds 65.7s.8.8125d$ .
d. 8.8125 since 51d	d = 5.25d.
No. of days from $= 146$ ;	Apr. 6 to Aug. 30=24 + 31 + 30 + 31 + 30
365 days : 14	46 days :: £65. 7s. 8.8125d. : int. reqd.
or 5 : 2 :	: £65. 7s. 8.8125d. : int. req <sup>d</sup> .
$$ int. req <sup>a</sup> .= $\frac{1}{276}$	$5 \text{ of } \pm 65. 78. 8.8125d = \pm 26. 38. 1.125d.;$
Note. Since £13	376. 118. 3d = £1376.5625. and 49 = 4.75.
	$(1376.5625 \times 4.75)$
we might have found	d the int. thus : int. $=$ $t \left( \frac{100}{100} \right)$
= £65·38671875.	
	Ex. LXX.
Find the Simple In	t. and also the Amt. of
(1) \$217.25 for 1	year at 8 per cent. per ann <sup>m</sup> .
(2) \$217.25 for 2	yrs. at 8 per cent
(3) \$527.37 <sup>1</sup> / <sub>2</sub> for	3 yrs. at 7
(4) \$93.50 for 2	yrs. at 6

(5) \$75.75 for 2½ yrs at 7.....
(6) £62. 18s. 9½d. for 3½ yrs. at 8.....

#### COMPOUND INTEREST.

(7) \$1075.75 for 41 yrs. at 8 per cent. per ann.

(8) \$684 for 5 yrs. 8 mo., at 8 .....

(9) £7500 from May 5 to Oct. 26, at 3<sup>1</sup>/<sub>5</sub>.....

(10) £4865. 11s. 5d. from Jan. 1 to Aug. 28, 1868, at 38.,

(11) In what time will \$672 at 8 per cent. simp. int. amount to \$994.56?

(12) At what rate per cent., simp. int., will the int. on \$816 amount to \$346.80 in 5 yrs. ?

(13) What sum of money will amount to £138. 2s. 6d. in 15 mo. at 5 per cent. per ann<sup>m</sup>., simp. int.?

(14) If  $\pm 1 = 10$  forms = 100 cents = 1000 mills, find the simp. int. on  $\pm 578$ . 3 fl. 1 c.  $2\frac{1}{2}$  m. for  $2\frac{1}{2}$  yrs. at  $2\frac{1}{2}$  per cent.

(15) At what rate per cent., simp. int., will \$2293.75 double itself in 25 yrs.?

## COMPOUND INTEREST.

126. To find the Compound Interest of a given sum of money at a given rate per cent. for any number of years.

RULE. At the end of each year add the interest of that year, found by (Art. 116), to the principal at the beginning of it; this will be the principal for the next year; proceed in the same way as far as may be required by the question. Add together the interests so arising in the several years, and the result will be the compound interest for the given period.

Ex. 1. Find the Comp. Int. and Am<sup>t</sup>. of \$600 for 3 yrs. at 8 per cent. per ann.

Int. for 1st yr. Prin <sup>1</sup> . for 2nd y <b>r.</b>
Int. for 2nd yr. Prin <sup>1</sup> . for 3rd yr.

\$55.9872 Int. for 3rd yr.

.:.Comp<sup>4</sup> int. =55.9872 + 51.84 + 48 = 155.8272. Am<sup>4</sup>. 600 + 155.8272 = 755.8272.

Ex. 2. Find, working with decimals, the comp. int. and am<sup>4</sup>. of £690 for 2 yrs. at 4<sup>1</sup>/<sub>2</sub> per cent. per ann.

£
41 - 4.5
3450
2760
$\pounds 31.050 = $ Int. for 1st yr.
£690
$\pounds 721.050 = Prin^{1}$ for 2nd yr.
4.5
360525
288420
£32.44725 = Int. for 2nd yr.
£721.05
£753:49725 - Print for 3rd vr or amount read
20
9.94500.
12
11,2402
11.9400.

1.36q. ...  $am^{t} = \pounds753.$  9s. 114d. nearly, and Int. = \pounds753. 9s. 114d., nearly - \pounds690 = \pounds63. 9s. 114d. nearly.

Note 1. It is customary, if the comp<sup>4</sup> int. be required for any number of entire yrs. and a part of a yr. (for instance for  $5\frac{2}{3}$  yrs.) to find the comp<sup>4</sup> int. for the 6th yr., and then take  $\frac{2}{3}$ ths of the last int. for the  $\frac{2}{3}$ ths of the 6th yr.

Note 2. If the int. be payable half-yearly or quarterly, it is clear that the comp<sup>4</sup>, int. of a given sum for a given time will be greater as the length of each given period is less; the simp. int. will not be affected by the length of each period.

#### Ex. LXXI.

Find the Compound Int. and Arnt. of

- (1) \$800 for 2 yrs. at 7 per cent. per annum.
- (6) \$1000 for 3 yrs. at 7.....paid half-yearly.

(7) Find the difference between the Amounts at simp. and comp. int. of (1)  $\pounds$ 880 for 2 ys. at  $3\frac{1}{2}$  per cent. (2)  $\pounds$ 1431. 5s. for three yrs. at 4 per cent.

## PRESENT WORTH AND DISCOUNT.

127. A owes B \$500, which is to be paid at the end of 9 months from the present time; it is clear that, if the debt be paid at once (int. being reckoned, we will suppose, at 8 per cent. per annum), B ought to receive a less sum of money than \$500; in fact such a sum of money as will, being now put out at 8 per cent. int., amounts to \$500 at the end of 9 months. The sum which B ought to receive now is called the Present Worth of the \$500, due 9 months hence, and the sum to be deducted from the \$500, in consequence of immediate payment, which is in fact the int. of the Present Worth, is called the Discount of the \$500 paid 9 months before it is due; hence,

PRESENT WORTH is the actual worth at the present time of a sum of money due some time hence, at a given rate of interest.

DISCOUNT of a sum of money is the interest of the Present Worth of that sum, calculated from the present time to the time when the sum would be properly payable.

... Disc<sup>t</sup>. = given sum less its P. Worth, and P. Worth = given sum less its Disc<sup>t</sup>.

#### PRESENT WORTH.

128. RULE. Find the interest of \$100 for the given time at the given rate per cent., and state thus :

\$100 + its interest for the given time at the given rate per cent. : given sum :: \$100 : present worth required.

Ex. 1. Find the present worth of \$676, due 6 months hence, at 8 per cent. per annum.

By the Rule,

Int. on \$100 for 6 mo. at 8 per cent.=\$4. ∴\$104 : \$676 :: \$100 : P. Worth req<sup>d</sup>.

hence P. Worth req<sup>d</sup>. =  $\frac{670 \times 100}{104} =$ \$650.

Reason. \$100 is the P. Worth of \$104, due 6 mo. hence, ... we have the above statement by the Rule of Three.

Ex. 2. Find the present worth of £275. 6s. 8d. due 15 months hence at 4 per cent per annum.

Int. of £100 for 15 mo. at 4 per cent.  $=\frac{15}{12}$  of £4 = £5.  $\therefore$  £105 : £275 $\frac{1}{3}$  :: £100 : P. Worth req<sup>4</sup>.  $\therefore$  P. Worth req<sup>4</sup>. = £ $\frac{275\frac{1}{3} \times 100}{105}$  = £262. 4s. 5 $\frac{1}{4}d$ . nearly.

#### DISCOUNT.

129. RULE. Find the interest of \$100 for the given time at the given rate per cent., and state thus :

\* \$100. + its interest for the given time at the given rate per cent. : given sum :: interest of \$100 for the given time at the given rate per cent. : discount required.

Ex. 1. Find the discount of \$250.75 due 17 months hence at 8 per cent per annum, simple interest.

By the Rule,

Int. of \$100 for 17 mo. at 8 per cent.  $=\frac{17}{12}$  of \$8 = \$11 $\frac{1}{3}$ .  $\therefore$  \$111 $\frac{1}{3}$  : \$250 $\frac{3}{4}$  :: \$11 $\frac{1}{3}$  : disc<sup>t</sup>. req<sup>d</sup>.  $\therefore$  disc<sup>t</sup>. req<sup>d</sup>. = \$ $\frac{250\frac{3}{4} \times 11\frac{1}{3}}{111\frac{1}{3}}$  = \$25.40 $\frac{29}{27}$ .

*Reason.*  $11\frac{1}{3}$  is the interest on 100 or the discount on  $111\frac{1}{3}$  for 17 mo. at 8 per cent., ... we have the above statement by the Rule of Three.

130. In the discharge of a tradesman's bill before it has become due, it is usual to deduct interest instead of discount; thus, if B contracts with A a debt of \$100, A giving 12 months' credit, it is usual, if the interest of money be reckoned at 8 per cent. per annum, and the bill be discharged at once, for A to throw off \$8, or for A to receive \$92 instead of \$100; but if A were to put out the \$92 at 8 per cent. interest for 12 months it will not amount to \$100; therefore such a proceeding is to the advantage of B: the sum of money which in strictness ought to have been deducted, was not \$8, the interest on the whole debt, but \$7.36, the interest on the present worth of the debt, i. e. the discount.

131. Bankers and Merchants in discounting bills calculate interest, instead of discount, on the sum drawn for in the bill, from the time of their discounting it to the time when it becomes due, adding THREE DAYS OF GRACE, which days are usually allowed after the time a bill is NOMINALLY due, before it is LEGALLY due. When a bill is payable on demand, the days of grace are not allowed.

If a bill, without the days of grace, should appear to be due on the 31st of any month which contains less than 31 days, the last day of that month, and not the first day of the next, is considered as the day on which the bill is due. Thus a bill drawn on the 31st of Oct. at 4 months, would be really due, adding in the days of grace, on the 3rd of March. Bills which fall due on a Sunday, are paid on the previous Saturday.

Ex. A bill of  $\pounds 1000$  is drawn on Feb. 16th, 1864, at 7 months' date : it is discounted on the 8th day of July at 5 per cent. What does the banker gain by the transaction?

The bill is *legally* due on Sept. 19; from July 8 to Sept. 19 are 73 days.

Int. of £1000 for 73 days = £10. Disc<sup>t</sup> = £9.  $18_{161}^{2}$ s., .: banker's gain = £10 - £9.  $18_{161}^{2}$ s. =  $19_{101}^{9}$ s.

## Ex. LXXII.

Find the present worth of

(1) \$216 due 1 yr. hence at 8 per ct. per ann. simp. in	at.
(2) \$9683 yr	• •
(3) \$12366 mo 6	
(4) \$225.259 mo 10	•••
(5) \$1057.50 $2\frac{1}{2}$ yrs 7	
(6) £161. 138. $5\frac{1}{4}d$ . $7\frac{1}{7}$ yrs $3\frac{1}{2}$	• •
(7) £193. 17s. $4\frac{1}{4}d$ . 19 mo 5	• •
(8) £458. 8s. 9 <sup>1</sup> <sub>4</sub> d. 31 days 5	• •
Find the Discount on	
(9) \$217 due 3 yrs. hence at 8 per ct. per ann. simp. in	at.
(10) \$22100 $1\frac{1}{2}$ yrs 7	• •
(11) \$2000 6 mo 10	
(12) \$1750 9 mo 8	• •
(13) £345. 16s. 3d. 86 days 4	

(14) What is the difference between the true and mercantile discount on £549 for 32 days at 5 per cent. per annum?

(15) A bill for £450 drawn March 3, at 9 mo. date, is discounted by a banker on Oct. 22 at 5 per cent. Find his profit.

(16) From a bill of £3. 11s. 8d. due 18 mo. hence, a tradesman deducts 5s.; which is the rate per cent. at which the true discount is calculated?

#### STOCKS.

132. If the 6 per cent. "Dominion of Canada" stock be quoted in the money market at 105<sup>5</sup><sub>2</sub>, the meaning is, that for  $$105\frac{1}{2}$  of money a man can purchase \$100 of such stock, for which he will receive, a document which will entitle him to half-yearly payments of Interest or Dividends, as they are called, from the Government of the country, at the rate of 6 per cent. per annum on the stock held by him, until the Government choose to pay off the debt.

Similarly, if shares in any trading company, which were originally fixed at any given amount, say \$100 each, be advertised in the share-market at 86, the meaning is, that for \$86 of money one share can be obtained, and the holder of such share will receive a dividend at the end of each halfyear upon the \$100 share according to the state of the finances of the company.

STOCK may therefore be defined to be the capital of trading companies; or to be the money borrowed by our or any other Government, at so much per cent., to defray the expenses of the nation.

The amount of debt owing by the Government is called the NATIONAL DEET, or the FUNDS. The Government reserves to itself the option of paying off the principal or debt at any future time, pledging itself however to pay the interest on it regularly at fixed periods in the mean time.

From a variety of causes the price of stock is continually varying. A fundholder can at any time sell his stock, and so convert it into money, and it will depend upon the price at which he disposes of it as compared with the price at which he bought it, whether he will gain or lose by the transaction.

Note 1. Purchases or sales of stock are made through Brokers, who generally charge \$, or  $12\frac{1}{2}$  cts. per cent. upon the stock bought or sold : so that, when stock is bought by any party, every \$100 stock costs that party \$ more than the market-price of the stock : and when stock is sold, the seller gets \$ less for every \$100 stock sold than the marketprice.

Thus, the actual cost of \$100 stock in the 3 per cents at

#### STOCKS.

94<sup>1</sup>/<sub>5</sub>, is  $\$(94\frac{1}{3} + \frac{1}{6})$ , or  $\$94\frac{2}{3}$ . The actual sum received for \$100 stock in the 3 per cents. at  $94\frac{1}{3}$ , is  $\$(94\frac{1}{3} - \frac{1}{6})$ , or \$94.

Unless the brokerage is mentioned, it need not be noticed in working examples in stocks.

Note. When \$100 stock costs \$100 in money, the stock is said to be at *par*; when \$100 stock cost more than \$100 in money, the stock is said to be at a *premium*; when \$100 stock costs less than \$100 money, the stock is said to be at a *discount*.

All Examples in Stocks depend on the principles of Proportion, and may therefore be worked by the Rule of Three.

Ex. 1. What sum of money will purchase \$2600 6 per cent. stock at 93?

\$100 stock (st) costs \$93 in money; \$100 st. : \$2600 st. :: \$93 : req<sup>d</sup>. sum; \$100 st. : \$2600 st. :: \$93 = \$2418.

Ex. 2. Find the cost of £2353 3 per cent. Consols at 90§ brokerage being  $\frac{1}{2}$  per cent.

$$\begin{array}{c} \pounds \bar{1}00 \text{ st. costs } \pounds(90\frac{3}{2} + \frac{1}{8}), \text{ or } \pounds 90\frac{1}{2}; \\ \therefore \pounds 100 \text{ st. : } \pounds 2353 \text{ st. : } \pounds 90\frac{1}{2}; \text{ req}^{4}. \text{ cost}; \\ \text{ req}^{4}. \text{ cost} = \pounds \frac{2353 \times 90\frac{1}{2}}{100} = \pounds 2129. 9s. 3\frac{1}{4}d. \frac{2}{8}q \end{array}$$

Ex. 3. A person who has \$10000 Bank-stock, sells out when it is at 35 per cent. premium ; what amount of money does he receive, brokerage being  $\frac{1}{2}$  per cent.?

\$100 st. sells for \$ $\left(135 - \frac{1}{8}\right)$ , or \$ $134\frac{7}{3}$  money;  $\therefore$  \$100 st. \$1000 st.  $\Rightarrow$  \$ $134\frac{7}{3}$  : req<sup>d</sup>. am<sup>t</sup>. of money;  $\therefore$  req<sup>d</sup>. am<sup>t</sup>. = \$ $\frac{10000 \times 134\frac{7}{3}}{100}$  = \$13487.50.

Ex. 4. What incomes will \$5500 at 7 per cent. stock, and \$5500 invested in the 7 per cent. stock at  $102\frac{2}{3}$ , respectively produce?

1st, since every \$100 stock gives \$7 int.;  $\therefore$  income from \$5500 of 7 per cent. stock =  $\frac{5500 \times 7}{100} =$  \$385.

2nd, since \$100 stock, which gives \$7 int., costs \$1023; ... every \$1023 give \$7 int.;

.:.\$1023 : \$5500 :: \$7 req<sup>d</sup>. income :

 $\therefore$  reg<sup>4</sup>. income =  $\frac{5500 \times 7}{375}$ .

#### ARITHMETTO.

Ex. 5. One person buys £500 Consols at  $90_3^{\circ}$  and sells out at 93; another invests £500 in Consols at  $90_3^{\circ}$  and sells out at 93; what sum of money does each gain ?

1st man gains  $\pounds(93 - 90\frac{1}{3})$ , or  $\pounds2\frac{2}{3}$ , on every  $\pounds100$  stock; ... his whole gain =  $\pounds(2\frac{2}{3} \times 5) = \pounds13$ . 6s. 8d.

2d man gains  $\pounds 2_3^2$  on every  $\pounds 100$  stock, *i. e.* on every  $\pounds 90_3^1$  of his money which he invests :

 $\therefore \pm 90\frac{1}{3} : \pm 500 :: \pm 2\frac{3}{3} : \text{whole gain};$ 

: whole 
$$gain = \pounds \frac{500 \times 2\frac{2}{3}}{90\frac{1}{3}} = \pounds 14.15s.2\frac{1}{4}d.$$
, nearly.

Ex. 6. A person invested some money in the 3 per cent. Consols when they were at 90, and some money when they were at 80; find the rate of interest he obtained in each case, and the advantage per cent. of the second purchase over the first.

 $\pounds 90: \pounds 100:: \pounds 3:$  rate per cent. in 1st case,  $\pounds 80: \pounds 100:: \pounds 3:$  rate per cent. in 2d case,

 $\therefore \text{ rate per cent. in 1st case} = \pounds \frac{100 \times 3}{90} = \pounds 3. \ 6s. \ 8d.;$ 

$$2nd \dots = t \left( \frac{-1}{80} \right) = t3. 15s;$$

Ex. 7. A person invests  $\pm 1037$ . 10s. in the 3 per cents. at 83; the funds rise 1 per cent.; he then transfers his capital to the 4 per cents at 96: find the alteration in his income.

 $\pounds 83 : \pounds 1037. \ 10s. :: \pounds 100 : quantity of 3 per cent. st.;$ 

... quantity of 3 per cent st. bought =  $\pounds \frac{1037\frac{1}{2} \times 100}{80} = \pounds 1250.$ 

The funds have risen 1 per cent. therefore to transfer  $\pm 1250$  stock from the funds at 84 to the funds at 96,

£96:£84::£1250<sup>\*</sup>stock:quantity of 4 per cent. stock, (since the higher the price of the stock the less will be the amount purchased);

•. quantity of 4 per cent. stock =  $\pounds \frac{1250 \times 84}{96} = \pounds 1093.15s.$ Ist Income =  $\pounds \frac{1250 \times 3}{100} = \pounds 37.10s.$ 2nd Income =  $\pounds \frac{1093\frac{3}{4} \times 4}{100} = \pounds 43.15s.;$ 

... alteration in income = £43 15s. \_£37 10s. = £6. 5s.

#### Ex. LXXIII.

(1) Find amount of Bank of Montreal stock purchased by investing \$527.25 at 126<sup>1</sup>/<sub>2</sub>, the stock yielding 8 per cent., per annum interest?

(2) Bank of Toronto stock being at  $102\frac{1}{2}$ , how much can be purchased for \$800?

(3) Find the value of \$1556 Royal Canadian Bank stock at 98.

(4) Royal Canadian Bank stock being at 1 per cent. discount, I invest \$525.50; find my income therefrom; the Bank's dividends being 7 per cent. per annum.

(5) Montreal Bank stock being at  $125\frac{3}{8}$ , and paying yearly dividends of  $7\frac{1}{2}$  per cent.; how much money must be invested in order to secure an annual income of \$900, allowing  $\frac{1}{2}$  per cent. for brokerage?

(6) Upper Canada Bank bills are at 65; how much money could a person obtain for \$2140 of such Bank bills?

(7) If a man invest £666. 8s. 4d. in the 3 per cents. at  $90\frac{2}{3}$ , (1) what half-yearly interest will be obtain after deducting an inc<sup>6</sup>. tax of 4d. in the £? (2) What rate per cent. will be get for the money invested?

(8) What rate per cent. per annum does a person receive for his money, who invests in Bank of Montreal stock at 136; the stock yielding half-yearly dividends of 4 per cent?

(9) Which would be the better investment, Bank of Montreal stock at 136, or Bank of Toronto stock at 104; half-yearly dividends being 4 and 3<sup>2</sup>/<sub>4</sub> per cent. respectively?

(10) If a person lay out £4650 in the  $3\frac{1}{2}$  per cents. when they are at 7 per cent. discount, what will be his loss of property by the stocks falling  $\frac{1}{2}$  per cent.?

(11) If a person were to transfer £29000 stock, from the  $3\frac{1}{2}$  per cents. at 99 to the 3 per cents. at 90<sup>§</sup>, what difference would it make in his income?

(12) A person invests \$2000 in Bank of Toronto stock at 115, shortly afterwards he sells when the stock rose to 123. Find his gain?

(13) If the 3 per cents. are at 95, and Government offer to receive tenders for a loan of  $\pm 5016000$ , the lender to receive five millions in the 3 per cents. together with a certain sum in the  $3\frac{1}{2}$  per cents.; what sum in the  $3\frac{1}{2}$  per cents. ought the lender to accept?

(14) A man sells out of the  $3\frac{1}{2}$  per cents. at  $93\frac{1}{2}$  and realizes £18700: if he invest one-fifth of the produce in the 4

per cents. at 96, and the remainder in the 3 per cents. at 90; find the alteration in his income.

(15) A person invests  $\pm 5460$  in the 3 per cents. at 91; he sells out  $\pm 2000$  stock when they have risen to 93<sup>1</sup>/<sub>2</sub>, and the remainder when they have fallen to 85; he then invests the produce in the 4<sup>1</sup>/<sub>2</sub> per cents. at 102. What is the difference in his income?

(16) A person has an income of £350 from money invested in the new 3 per cents. the sells out at  $87_{3,}^{2}$  and invests in the India 5 per cents. at 104<sup>2</sup>. How will his income be affected,  $\frac{1}{2}$ th per cent. being allowed for brokerage?

## APPLICATIONS OF THE TERM "PER CENT."

133. There are many other cases in which the term PER CENT. occurs besides those already mentioned; we will mention certain cases, and give examples in each by way of illustration.

COMMISSION is the sum of money which a merchant charges for buying or selling goods for another.

BROKERAGE is of the same nature as Commission, but has relation to money transactions, rather than dealings in goods or merchandise.

INSURANCE is a contract, by which one party, on being paid a certain sum or *Premium* by another party on property, which is subject to risk, undertakes, in case of loss, to make good to the owner the value of that property. The document which expresses the contract is called *the Policy of In*surance.

LIFE ASSURANCE is a contract for the payment of a certain sum of money on the death of a person, in consideration of an annual premium to be continued during the life of the Assured, or for a certain number of years.

Questions on Commission, Brokerage, and Insurance, these charges being usually made at so much per cent., amount to the same thing as finding the interest on a given sum of money at a given rate for 1 yr., and may therefore be worked by the Rule for Simple Int. or by the Rule of Three.

Ex. 1. What is the brokerage on the purchase of \$4300 6 per cents. stock at  $\frac{1}{2}$  per cent.?

 $100:4300:3\frac{1}{5}:5\frac{1}{5}:brok^{\circ}.req^{4}.;. brok^{\circ}.req^{4}.=\frac{4300\times \frac{1}{5}}{100}$ 

\$5.371.

Ex. 2. What is the premium on a policy of insurance for £9626. 11s. 3d., at £2. 12s. per cent.?

£100 : £9626. 11s. 3d. :: £2. 12s. : premium req<sup>d</sup>.

... premium req<sup>d</sup>. =  $\pounds \frac{9626_{13}}{26} \times 2\frac{3}{5} = \pounds 250.5s.9\frac{3}{4}d.$ 

Ex. 3. What is the annual cost of insuring property to the amount of \$1600, the premium being \$1.50 per cent.?

 $100: 160: 1.50: ann! \cos t; \therefore ann! \cos t = 1.50 \times 16 = 24.$ 

134. All questions which relate to gain or loss in mercantile transactions fall under the head of PROFIT and Loss.

Tradesmen measure their Profit or Loss by the actual amount gained or lost, or by the amount gained or lost on every \$100 of the capital they invest.

Ex. 4. <sup>\*</sup> If tea be bought at 84 cts. per lb., and sold at 93 cts. per lb., find the gain per cent.

(93 cts. -84 cts.)=9 cts.; ... gain on 84 cts.=9 cts.

. . . 84 cts. : \$100 :: 9 cts. : gain per cent. ;

... gain per cent. =  $\frac{100 \times 9}{84}$  cts. = \$10.71<sup>3</sup>/<sub>7</sub>.

Ex. 5. If tea be bought at 93 cts. per lb. and sold at 84 cts. per lb., find the loss per cent.

In this case 9 cts. is lost on 93 cts.,

... 93 cts. : \$100 :: 9 cts. : loss per cent.

whence loss per cent. =  $9.67_{31}^2$ .

Ex. 6. By selling cheese at £3. 13s. 6d. a cwt. a grocer realized a profit of  $22\frac{1}{2}$  per cent., what did it cost him per cwt.? He sells cheese for which he gave £100 for £122 $\frac{1}{2}$ .

 $\therefore$  £122½ : £3. 13s. 6d. or £3 $\frac{2}{4}\frac{7}{6}$  :: £100 : prime cost per cwt ;

: prime cost per cwt. =  $\pounds \frac{3\frac{2}{40} \times 100}{122\frac{1}{2}} = \pounds 3.$ 

Ex. 7. By selling cheese at £3. 13s 6d. a cwt. a grocer lost  $22\frac{1}{2}$  per cent., find the prime cost of the cheese per cwt.

In this case he sells cheese, for which he gave £100, for  $(\pounds 100 - \pounds 22\frac{1}{2})$ , or for £77 $\frac{1}{2}$ .

 $\therefore$  £77½ : £3%7 :: £100 : prime cost of cheese per cwt. ;

: prime cost per cwt. = 
$$\pm \frac{3\frac{3}{4}\frac{1}{6} \times 100}{77\frac{1}{2}} = \pm 4.14s. 10\frac{3}{3}1d.$$

Ex. 8. By selling sheep for \$19 the seller loses 5 per cent. on his outlay; what would have been his loss or gain per cent. if he had sold the sheep for \$23.75?

1st. \$95 : \$19 :: \$100 : prime cost of sheep,  $\therefore$  prime cost of sheep = \$20.

2nd. \$20: \$100:: \$3.75: gain per cent., if the sheep be sold for \$23.75;

: gain per cent. =  $\frac{100 \times 3\frac{3}{4}}{20}$  = \$18.75.

This sum might have been worked thus,

\$19: \$232 :: \$95, i. e. what \$100 will realize if the sheep be sold for \$19: what \$100 will realize if the sheep be sold for \$233.

: \$100, if sheep sold for \$23 $\frac{2}{3}$  will realize \$ $\frac{95 \times 23\frac{2}{3}}{19}$ , or \$118 $\frac{3}{4}$ ;

 $\therefore$  gain per cent. = 1182 - 100 = 182 = 18.75.

135. Tables respecting the increase or decrease of Population, &c., are constructed with reference to the increase or decrease on every 100 of such population; Education returns are constructed in the same way; and so are other Statistical Tables.

Ex. 9. In 1852 the population of the County of Wellington was 26796, in 1861 it was 49200; find the increase per cent. 49200-26796=22404; ... 26796: 100:: 22404: incr. per cent.

.:.increase per cent.  $=\frac{2240400}{26796}=83.609....$  per cent.

Ex. 10. Between the years 1841 and 1851 the population of England increased 14.2 per cent. In 1851 it was 21121290. what was it in 1841?

For every 100 persons in 1841 there were 114.2 in 1851; ... 114.2: 21121290::100: population in 1841;

 $\frac{21121290 \times 100}{1121290 \times 100} = 18495000.$ 

Ex. 11. If of a regiment of 750 men, 26 per cent. are in hospital, 32 per cent. in trenches, and the rest in camp, how many are in hospital, trenches, and camp, respectively.

many are in hospital, trenches, and  $com_{P}$ ,  $\frac{750 \times 26}{100}$ =195.

100:750::32: no. in tren<sup>hs</sup>. ;. . no. in tren<sup>hs</sup>. =  $\frac{750 \times 32}{100}$  = 240.

... number in camp = 750 - (195 + 240) = 315.

Ex. 12. The percentage of children who are learning to

write is 65 in a school of 60 children, and 78 in another school of 10, what is the percentage in the two schools together? In the 1st school,

100:60::65:no. who write; ... no. who write =  $\frac{60 \times 65}{100} = 39$ .

In the 2nd school,

100:70::78:no, who write; ... no. who write =  $\frac{70 \times 78^3}{100} = 54\frac{3}{5}$ . ... in a school of 130, there are  $93\frac{3}{5}$  who write;

... 130 : 100 :: 933 : percent. req<sup>d</sup>. ; ... percent. req<sup>d</sup>.

$$=\frac{100 \times 93\frac{3}{5}}{130}=72$$

#### Ex. LXXIV.

(1) What will be the broker's commission on the purchase of \$4300 6 per cents. at  $90\frac{1}{2}$ , at  $\frac{1}{2}$  per cent. ?

(2) What is the premium on a policy of insurance for \$9626.55 at \$2.60 per cent.?

(3) The commission on the purchase of \$1560 Dominion stock at 104 amounted to \$4.60, what was the rate per cent.?

(4) For what sum would the life of a person aged 23 be insured by the annual payment of \$45.60, the premium for that age being \$2.40 per cent. ?

(5) A draper at Hamilton buys 25 pieces of calico, each containing 36 yds., for £32. 16s. 3d.; the carriage costs him 6s. 3d.; (1) What will he gain by selling the calico at  $10\frac{1}{2}d$ . a yard? (2) What will he gain per cent.?

(6) A merchant bought 1280 bus. of wheat at \$1.20 a bu., the expenses of carriage, &c., averaged 3<sup>2</sup>/<sub>4</sub> cts. a bu.; he sold the wheat at \$1.40 a bu. (1) What was his gain? (2) What was his gain per cent.? (3) At what price a bu. should he have sold the wheat in order to gain \$400?

(7) (1) A man buys a pig for 6s. 8d., and sells it for 7s. 4d.; find his gain per cent. (2) What would have been the loss per cent. had he bought the pig at 7s. 4d. and sold it at 6s. 8d. 1

(8) Tea is bought at \$96 per cwt., at what price per lb. must it be sold to gain 25 per cent. ?

(9) Sugar is bought at \$6 per cwt., what will be the gain per cent. if it be sold at 10 cts. per lb.?

(10) At what price must a yd. of cloth be sold, which cost 48. 8d., so as to gain 124 per cent.?

(11) If a yd. of cloth, sold at 4s. Sd., give a profit of 12; per cent.; find the prime cost.

(12) A grocer buys 40 lbs. of tea at 84 cts., 44 lbs. at 93 cts., and 55 lbs. at \$1.08; and sells the mixture for \$188.16, what is his gain per cent. ?

(13) A grocer mixes 26 lbs. of tea at 5s. 3d., 32 lbs. at 5s. 7d., and 36 lbs. at 6s. 1d.; at what rate per lb. must he sell the mixture in order to gain 40 per cent. on his outlay?

(14) If I sell for 15s. I lose 10 per cent., what must I sell at to gain 10 per cent.?

(15) A person buys a certain number of eggs and sells them again at such a price, that 11 are sold for the money 18 cost him. Find his gain per cent.

(16) A boy sells another boy a cricket-bat for \$1.56, gaining thereby 30 per cent.; what did it cost him?

APPLICATIONS OF THE TERM "AVERAGE."

136. Questions are often given, in which the term "Average" occurs; two such examples will be worked by way of illustration, and others subjoined for practice.

Ex. 1. A gentleman in each of the following years expended the following sums: in 1845 \$650, in 1846 \$675, in 1847 \$680, in 1848 \$690, in 1849 \$700, in 1850 \$715, in 1851 \$790. Find his average yearly expenditure.

The object is to find that fixed sum which he might have spent in each of the seven years, so that his total expenditure in that case might be the same as his total expenditure was in the above question.

Adding the various sums together we find that the total expenditure amounted to \$4900; this sum divided by 7 gives \$700 as the average yearly expenditure.

Ex. 2. In a school of 27 boys, 1 of the boys is of the age of 17 years, 2 of 16, 4 of  $15\frac{1}{2}$ , 1 of  $14\frac{3}{4}$ , 2 of  $14\frac{1}{2}$ , 5 of  $13\frac{3}{4}$ , 10 of  $12\frac{1}{4}$ , and 2 of 10; find the average age of the boys.

The object is to find, what must be the age of each boy, supposing all to be of the same age, that the sum of their ages may equal the sum of the ages in the question.

Sum of ages

=  $17 + 32 + 62 + 14\frac{3}{4} + 29 + 68\frac{3}{4} + 122\frac{1}{2} + 20 = 366$ .: average age = 366 yrs.  $\div 27 = 13\frac{5}{4}$  years.

#### Ex. LXXV.

(1) The highest temperature registered in the shade on
Monday 13th July, 1868, in the following towns, was:-Ottawa, 104; Montreal, 96; Toronto, 92; New York, 90; Buffalo, 82; New Orleans, 81. Find their average highest temperature?

(2) On Sunday I spent no money, on Mond. \$4.25, on Tues. \$5.75, on Wed. \$6.60, on Thurs. \$7.80, and Frid. \$3.50, on Sat. \$5.58; find my average daily expenditure during the week?

(3) The highest temperature registered in the shade in the week ending on Midsummer-day, 1865, in the following towns, was:—Birmingham, 87'8; Manchester, 87'7; London, 87'6; Bristol, 86'8; Leeds, 85'0; Salford, 84'5; Dublin, 83'8; Edinburgh, 78'0; Liverpool, 77.9; Glasgow, 77'6. Find their average highest temperature?

(4) In a school, 17 children average 6 years.; 26,  $7\frac{1}{2}$  yrs., 35,  $9\frac{1}{4}$  yrs.; 20, 10 yrs.; and 8 12 $\frac{1}{4}$  yrs. Find the average age of all the children.

(5) The average age of 27 men is 57 years, that of the first eleven is 53 years, and that of the last eight  $59\frac{1}{2}$  years. Find the average age of the rest.

(6) The populations of 3 towns in 1851 were 31326, 42324, and 0706; in 1861 the first two had increased 12, and 10 per cent. respectively, and the last had decreased 18 per cent.; find the average population of the 3 towns in 1861.

(7) A tradesman's average annual gain from the year 1853 to 1863, both inclusive, was £184. 11s. 6d.; in 1853 he lost £76. Ss. 4d., and in 1864 he gained £151. 9s. 10d. What was his average annual gain from 1854 to 1864, both inclusive?

### DIVISION INTO PROPORTIONAL PARTS.

137. To divide a given number into parts, which shall be proportional to certain other given numbers.

This is an application of the Rule of Three; still it may be well to state a general Rule, by which such Ex<sup>4</sup>. may be worked.

RULE. As the sum of the given parts : any one of them :: the entire quantity to be divided : the corresponding part of it.

This statement must be repeated for each of the parts, or at all events for all but the last part, which may either be

### ARITHMETIC.

found by the Rule, or by subtracting the sum of the values of the other parts from the entire quantity to be divided.

Ex. 1. Divide 40 dollars among A, B, C, so that their shares may be as 7, 11, and 14 respectively.

By the Rule. Sum of shares = 7 + 11 + 14 = 32.

... 32:7:: \$40: A's sh<sup>o</sup>.; 32:11:: \$40: B's sh<sup>o</sup>.; whence A's sh<sup>o</sup>. = \$8.75, B's sh<sup>o</sup>. = \$13.75. Coach = \$40. \$(c = 5, B's = 5, B

C's sh<sup>•</sup>.= \$40 - \$(8.75 + \$13.75) = \$17.50.

**Ex. 2.** Divide £45 among A, B, C, and D, so that A's share: B's share :: 1:2, B's : C's :: 3:4, and C's :: D's :: 4:5. The L. C. M., of 1, 2, 3, 4, and 5. is 60,  $\therefore$  if D has 60 shares,

C will have  $\frac{4}{5}$  of 60, or 48; B will have  $\frac{3}{4}$  of 48, or 36; and A will have  $\frac{1}{2}$  of 36, or 18.

.: (18 + 36 + 49 + 60), or  $162 : 18 :: \pounds 45 : A's sh^{\circ}$ ; whence  $A's sh^{\circ} = \pounds 5$ . Similarly  $B's = \pounds 10$ .  $C's = \pounds 13$ . 6s. 8d., and  $D's = \pounds 16$ . 13s. 4d.

#### FELLOWSHIP OR PARTNERSHIP.

139. FELLOWSHIP OF PARTNERSHIP is a method by which the respective gains or losses of partners in any mercantile transactions are determined.

Fellowship is divided into SIMPLE and COMPOUND FEL-LOWSHIP: in the former, the sums of money put in by the several partners continue in the business for the same time; in the latter, for different periods of time.

The Rule in the last Art. applies for SIMPLE FELLOWSHIP.

Ex. Two merchants, A and B, form a joint capital; A puts in \$240, and B \$360; they gain \$80. How ought the gain to be divided between them?

\$(240 + 360) : \$240 :: \$80 : A's sh. in \$'s

... A's sh<sup>o</sup>. = \$32, and B's sh<sup>o</sup>. = \$(80-32)=\$48.

#### COMPOUND FELLOWSHIP.

139. RULE. Reduce all the times into the same denomination, and multiply each man's stock by the time of its continuance, and then state thus:

The sum of all the products : each particular product :: the whole quantity to be divided : the corresponding share.

Ex. A and B'trade together; A puts in \$300 for 9 mo., and B \$240 for 6 mo; they gain \$115. How ought they to divide it?

By the Rule,

 $(300 \times 9 + 240 \times 6) : (300 \times 9) :: 115 : A's sh.,$ 

 $(300 \times 9 + 240 \times 6) : (240 \times 6) :: 115 : B's sh.,$ 

whence, A's sh<sup>•</sup>. = \$75, and B's = \$40.

Reason. \$300 for 9 mo. = 9 times \$300 for 1 mo., and \$240 for 6 mo. = 6 times \$240 for 1 mo. : the example then becomes one of Simple Fellowship.

### EQUATION OF PAYMENTS.

140. When a person owes another several sums or money, due at different times, the Rule by which we determine the just time when the whole debt may be discharged at one payment, is called the EQUATION OF PAYMENTS.

Note. It is assumed in this Rule that the sum of the interests of the several debts for their respective times equals the interest of the sum of the debts for the equated time.

RULE. Multiply each debt into the time which will elapse before it becomes due, and then divide the sum of the products by the sum of the debts; the quotient will be the equated time required.

Ex. 1. A owes B \$100, whereof \$40 is to be paid in 3 mo., and \$60 in 5 mo.; find the equated time.

By the Rule,

equated time in mo. = 
$$\frac{40 \times 3 + 60 \times 5}{40 + 60} = \frac{420}{100} = 4\frac{1}{5}$$
.

Ex. 2. A owed B \$10, to be paid at the end of 9 mo.; he pays however \$2 at the end of 3 mo., and \$3 at the end of 8 mo.; when ought the remainder to be paid?

In this case,  $2 \times 3 + 3 \times 8 + 5 \times no.$  of mo. req<sup>d</sup>. =  $10 \times 9$ , or  $6 + 24 + 5 \times no.$  of mo. req<sup>d</sup>. = 90;

or,  $30 + 5 \times no.$  of mo. req<sup>4</sup>. = 90, or  $5 \times no.$  of mo. req<sup>4</sup>. = 90 - 30, or 60,  $\therefore$  no. of mo. req<sup>4</sup>. = 12.

#### Ex. LXXVI.

(1) Divide (1) 1008 into 3 parts, which shall be to each other as the numbers 2, 3, 4, respectively. (2) \$260 into 3 parts, which shall be to each other as 5, 11, and 16. (3) 145 ac. 3 ro. 33 po. between two persons in the ratio of 5 : 6. (4) £110 between 4 persons, whose shares shall be as  $\frac{1}{2}$ ,  $\frac{1}{3}$ ,  $\frac{1}{4}$ , and  $\frac{1}{2}$ .

(2) (1) A, B, and C contribute to a fund \$320, \$560, \$720, respectively. How are they to divide a profit of \$680? (2) A, who has £422. 10s., owes B, £175; C, £210; and D, £265; what sum ought C to receive?

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(3) Sugar being composed of 48.856 per cent. of oxygen, 43.265 per cent. of carbon, and the rest hydrogen; how many lbs. of each of these materials are there in 1 ton of sugar?

(4) Archimedes discovered that the crown made for King Hiero consisted of gold and silver in the ratio of 2:1. How much per cent. was gold, and how much per cent. was silver?

(5) Find the equated time of payment of \$150 due in 2 mo., \$210 due in 6 mo., and \$120 due in 7 mo.

(6) A owes B \$1000 to be paid at the end of 6 mo.; A pays \$400 at the end of 3 mo.; when ought he to pay the remainder?

(7) A, B, and C remained partners for 2 years; A brought in \$4000, which remained the whole time; B began with \$300, and 6 months after put in \$300 more; C began with \$200, and one year after put in \$500 more. The whole gain was \$7960. Determine each partner's share.

(8) A is a working, B a sleeping partner in a bookseller's business. Their capital amounts to  $\pounds 6400$ ; of which  $\pounds 2400$  belongs to A, the rest to B. Their profits, at the end of the first year, amounted to  $\pounds 1600$ . A receives 10 per cent. of the profits for managing the business. How ought the remaining part of the profits to be divided?

(9) A, B, and C rent a field for \$60; A puts in 20 horses, B 15 oxen, and C 10 sheep; supposing the keep of a horse, ox, and sheep to be in the ratio of 3, 2, and 1; shew how the rent should be divided.

(10) Some broth was distributed among a certain number of old men, 9 widows, and 6 single women; the men had twice as much broth given among them as was given among the women; also an old man's share was to a widow's share :: 6 : 5, and a widow's share to a single woman's share :: 10 : 9. Each single woman received  $1\frac{1}{2}$  pints. How many old men were there?

#### **3QUARE ROOT.**

141. The SQUARE of a given number is the product of that number multiplied by itself. Thus  $6 \times 6$  or 36 is the square of 6, or  $36 = 6^2$ . Art. 86.

142. The SQUARE ROOT of a given number is a number,

which, when multiplied by itself, will produce the given number. Thus 6 is the square root of 36; for  $6 \times 6 = 36$ .

The square root of a number is sometimes denoted by placing the sign  $\checkmark$  before the number, or by placing the fraction  $\frac{1}{2}$  above the number a little to the right. Thus  $\sqrt{36}$ , or  $(36)^{\frac{1}{5}}$  denotes the square root of 36; so that  $\sqrt{36}$ , or  $(36)^{\frac{1}{5}}$ = 6.

### 143. Rule for extracting the Square Root of a number.

Place a point or dot over the units' place of the given number; and thence over every second figure to the left of that place; and thence also over every second figure to the right, when the number contains decimals, annexing a cy pher when the number of decimal figures is odd; thus di-viding the given number into periods. The number of points over the whole numbers and decimals respectively will shew the number of whole numbers and decimals respectively in the square root.

Find the greatest number whose square is contained in the first period at the left; this is the first figure in the root, which place in the form of a quotient to the right of the given number. Subtract its square from the first period, and to the remainder bring down, on the right, the second period.

Divide the number thus formed, omitting the last figure, by twice the part of the root already obtained, and annex the result to the root and also to the divisor.

Then multiply the divisor, as it now stands, by the part of the root last obtained, and subtract the product from the number formed, as above mentioned, by the first remainder and second period.

If there be more periods to be brought down, the operation must be repeated.

Ex. 1. Find the square root of 1369.

1369 ( 37 469

After pointing, according to the  $3^{2} = 9$   $\{2 \times 3 = 6\} \quad 67 \quad \boxed{9} \quad \text{After pointing, according to the} \\ 469 \quad 13, \text{ and find the greatest number} \\ \text{whose source is greatest number}$ Since the square of 3 is 9, and that

π

of 4 is 16, it is clear that 3 is the greatest number whose square is contained in 13, therefore place 3 in the form of a quotient to the right of the given number. Square this number, and put down the square under the 13; subtract it from the 13, and to the remainder 4 affix the next period 69, thus forming the number 469. Take  $2 \times 3$ , or 6, for a divisor ; di-

#### ARITHMETIC.

vide the 469, omitting the last figure, that is, divide the 46 by the 6, and we obtain 7. Annex the 7 to the 3 before obtained, and to the divisor 6; then multiplying the 67 by the 7 we obtain 469, which being subtracted from the 469 before formed, leaves no remainder ; therefore 37 is the square root of 1369.

Ex. 2. Find the square root of 282475249.

28247	5249	16807

2021/0249 (1000/
$\{2 \times 1 = 2\}$ 26 182 18÷2=9, but 9 will be tound too
12×16-22) 156 large, so also 8 or 7 try 6.
$32 \times 10 - 32$ 328 2647 264 $\div 32 = 8$
2624
$\{2 \times 168 = 336\}$ 336071 225240 326 is greater than 225
235249 0 after the 8 in the quotient
and the 6 in the divisor bring
down the next period. Then $23524 \div 3360 = 7$
Ex 2 Find the gauges part of 7:020856
Ex. o. Find the square root of 7 929800.
7.929856 (2.816
4 Place the first dot over the 7, the units'
48   392 place of whole numbers, and then over
384 every second figure to the right.
561 898
561
There is I dot over the integral part,
5626 33756 and 3 dots over the dec <sup>1</sup> . part, the
33796 root is 2.816.
Ex. 4. Find the square root of '001 to 3 places of deci.
.001000 / .021
0 We affir 2 amhans in orden to have
(a. a. a) CI (100 3 periods and 3 decl places in:
$\{2+3=6\}$ of 100 root since there is no number in
the units' place the first dot will be
39 over the second cypher from the
units' place and since first period is :00 we place the
first figure in the root
Ex 5 Find the square root of 529
211. 0. 1 1111 0110 Square 1000 01 2401.
± 10
43 1 129 89 801

801

. . . sq. root = 1.

148

129

Ex. 6. Find the square root of  $\frac{5}{7}$  to 3 places of des<sup>10</sup>.



### Ex. LXXVII.

Find the square roots of (1) 196; 289; 625. (2) S41; 900; 1764. (3) 2401; 7569; 9604. (4) 12321; 40000; 388129. (5) 494209; 582169; 259081. (6) 1234321; 28547649. (7) 62504336; 33016516; 49112064. (8) 182493081; 47<sup>6</sup>61. (9) 008836; 445<sup>3</sup>336609. (10) <sup>0</sup>00633679929; <sup>0</sup>00000009.

Find the square roots, each to four places of decimals, of (11) 51; 51. (12) 5<sup>-1</sup>; 051. (13) 806<sup>-52</sup>; 96304<sup>-993</sup>.

Find the square roots, each to 3 places of decimals where the root does not come out exactly, of (14)  $\cdot 3$ . (15)  $\cdot 027$ . (16)  $4\frac{36}{45}$ . (17)  $\frac{2304}{3481}$ . (18)  $\frac{4\cdot 41}{\cdot 64}$ .

(19) A father left his child a box, containing sovereigns, and shillings; the sovereigns were worth as many times the shillings, as the shillings were worth the box; the value of the box was 2s. 6d., and there were 5832 sovereigns in the box. How many shillings were there?

#### CUBE ROOT.

144. The CUBE of a given number is the product which arises from multiplying that number by itself, and then multiplying the result again by the same number. Thus  $6 \times 6$ , or 216, is the cube of 6; or 216 =  $6^3$ . Art. 86.

145, The CUBE ROOT of a given number is a number, which, when multiplied into itself, and the result again multiplied by it, will produce the given number. Thus 6 is the cube root of 216; for  $6 \times 6 = 36$ , and  $36 \times 6 = 216$ .

The cube root of a number is sometimes denoted by plac-

ing the sign  $\sqrt[4]{}$  before the number, or placing the fraction  $\frac{1}{3}$  above the number, a little to the right. Thus  $\sqrt[3]{216}$  or  $(216)^{1/3}$  denotes the cube root of 216 ; so that  $\sqrt[3]{216}$  or  $(216)^{1/3} = 6$ .

146. Rule for extracting the Cube Root of a number.

Place a point or dot over the units' place of the given number, and thence over every third figure to the left of that place; and thence also over every third figure to the right, when the number contains decimals, affixing one or two cyphers, when necessary, to make the number of decimal places a multiple of 3; thus dividing the given number into periods. The number of points over the whole numbers and decimals respectively will shew the number of whole numbers and decimals respectively in the cube root.

Find the greatest number whose cube is contained in the first period at the left; this is the first figure in the root, which place in the form of a quotient to the right of the given number.

Subtract its cube from the first period, and to the remainder bring down, on the right, the second period.

Divide the number thus formed, omitting the two last figures, by 3 times the square of the part of the root already obtained, and affix the result to the root.

Now calculate the value of 3 times the square of the first figure in the root (which of course has the value of so many tens) + 3 times the product of the two figures in the root + the square of the last figure in the root. Multiply the value thus found by the second figure in the root, and subtract the result from the number formed, as above mentioned, by the first remainder and the second period. If there be more periods to be brought down the operation must be repeated.

Ex. 1. Find the cube root of 15625.

156	625(25
$     \begin{array}{r}       156 \\       2^3 = 8 \\       3 \times 2^2 = 12 \\       3 \times (20)^2 = 3 \times 400 = 1200 \\       3 \times 20 \times 5 = 300 \\       5^2 = 25 \\       1525 \\       Multiply by 5   \end{array} $	After pointing we 7625 take the first period, or 15, and find the great- est number whose cube is contained in it. Since the cube of 2 is 8, and that of 3 is 2 or 27 it is clear that 2 is
7625	1 7625 27, it is clear that 2 is the greatest number

tained in 15; ... place 2 in the form of a quotient to the right of the given number.

Cube 2, and put down its cube, viz. 8, under the 15; subtract it from the 15, and to the rem<sup>7</sup>. 7 affix the next period 625, thus forming the number 7625. Take  $3 \times 2^2$ , or 12, for a divisor; divide 76 by 12, 12 is contained 6 times in 76; but when the other terms of the divisor are brought down 6 would be found too great, therefore try 5. Affix the 5 to the 2 before obtained; and calculate the value of  $3 \times (20)^2 +$  $3 \times 20 \times 5 + 5^2$ , which is 1525; multiplying 1525 by 5 we obtain 7625, which being subtracted from 7625 before formed leaves no rem<sup>7</sup>.;  $\cdot$  25 is the cube root req<sup>4</sup>.

Ex. 2. Find the cube root of 219:365327791.

Place the first dot over the 9 in the units' place.

219.365327791 ( 6.031

$6^3 = 216$	
$3 \times 6^2 = 108$	3365 33 is not divisible by 108:
$3 \times (60)^2 = 10800$	3365327 bring down the next pe-
$3 \times (600)^2 = 1080000$	riod and affix 0 to the root;
$3 \times 600 \times 3 = 5400$	the trial divisor will then
$8^2 = 9$	$33653 \div 10800$ goes 3 times
1085409	try 3.
3256227	3256227
	109100 bring down next pe-
$3 \times (603)^2 = 1090827$	109100791 riod 1091007÷1090\$27
$3 \times (6030)^2 = \overline{109082700}$	goes once, try 1.
$3 \times 6030 \times 1 = 18090$	
14=1	
109100791	109100791
	the cube root required. be root of '000007 to three places of
decimals.	·000007000 ( ·019
	1
3×1	<sup>2</sup> =3 6000
$3 \times (10)^{\circ} = 300$ $3 \times 10 \times 9 = 270$	
$9^2 = 81$	
651	
9	
5859	5859
	141

### ARITHMETIC.

147. Higher roots than the square and cube can sometimes be extracted by means of the Rules for square and cube root; thus the 4th root is found by taking the square root of the square root; the 6th root by taking the square root of the cube root, and so on.

### Ex. LXXVIII.

Find the cube roots of

- (1) 1728; 8000; 5832.
- (2) 74088; 421875; 778688.
- (3) 912673; 1092727.
- (4) 134217728; 64·481201.
- (5) 444194·947; ·000202262003.
- $(6) \quad 131.019108039; \quad 408518488000.$

Find the cube roots, to three places of decimals in those cases where the root does not terminate, of

(7)	27 .	(8)	4	(9)	34.	(10)	1.
(11)	•1.	(12)	•01.	(13)	10.	(14)	037.

### MISCELLANEOUS QUESTIONS.

### Ex. LXXIX.

#### PAPER I.

1. Subtract 2057312 from 5287201, and 2057312 again from the remainder. Explain how this is the same as dividing 5287201 by 2057312.

2. (1) Reduce 553553 oz. to tons, cwts., &c. (cwt. = 112 lbs.) (2) Find the proportion of the Avoird. and Troy oz., when the respective lbs. are as 175:144.

3. Find, by Practice, the cost of 16 cwt., 3 qrs., 16 lbs. at  $\pounds 2.7$  cents a cwt., (112 lbs. = cwt.)  $\pounds 1$  being = 10 florins = 100 cents = 1000 mils.

4. Define (1) the c. c. M., (2) the L. C. M., of two or more numbers, (3) a Vulgar Fraction. Find the c. c. M. of 20803 and 67273; and the L. c. M. of 8, 9, 10, 12, 15, 18, 35 and 84.

5. (1) Add together  $\frac{3}{2}$  of  $\frac{5}{11}$  of  $99\frac{1}{15}$ ,  $\frac{5}{7}$  of  $\frac{2}{9}$  of  $69\frac{3}{10}$ ,  $\frac{2}{7}$  of  $\frac{2}{5}$  of  $306\frac{1}{4}$ . (2) Express 13s.  $1\frac{1}{2}d$ . as the fraction of  $\frac{3}{4}$  of  $1\frac{1}{2}$  guinea. (3) Find the value of  $\frac{1}{2}\frac{2}{3}\frac{4}{15}$  ton (cwt. = 112 lbs.).

6. State the Rule for the division of one decimal by another. Divide (1) 7792.2 by .37, (2) .0077922 by 370; verify each result by vulgar fractions.

#### PAPER II.

1. Define Interest, Simple and Compound. How does Interest differ from Discount? Find (1) the int. on \$7300 at  $3\frac{3}{4}$  per cent. for 120 days, (2) the discount on £3204. 14s. 1d. at  $3\frac{1}{2}$  per cent. simp. int. for  $2\frac{3}{4}$  yrs.

2. A house built for \$2656 is sold for \$3320, find the gain per cent. If it had been built for \$3320 and sold for \$2656, find the loss per cent. ? Why do the rates differ?

3. Define a square. Find (1) the sq. root of 930372004, (2) the cub. root of .16777216, (3) the perimeter of a square whose surface is 2533 sq. ft., 64 sq. in.

4. Multiply 365 separately by 5, by 20, and by 300, and add the products together. Point out how the ordinary method of multiplying 365 by 325 agrees step by step with the above.

5. Define prime and composite numbers. Resolve 22932 into its prime factors.

6. A person left Toronto for Guelph at 9 A.M., and travelled the first 20 miles by rail, at the rate of 22<sup>1</sup>/<sub>2</sub> miles an hour; he then walked the remaining 32 miles at  $\frac{1}{6}$  of that rate. At what o'clock did he arrive?

#### PAPER III.

1. A and B fire at targets, having 55 cartridges each. A fires twice in 3 minutes, and B three times in 5 minutes; how many times will B have to fire after A has finished?

2. (1) Convert  $\frac{17}{20 \times 8}$  into a decimal; why is the result a terminating, and not a recurring decimal? (2) Express 3s.  $0\frac{1}{2}d$ . as the decimal of £5. (3) Which is greater, '36 of a guinea, or '36 of £1? (4) By how much?

3. What sum of money will amount to \$552.50 in 15 mo. at 5 per cent. simp. int.?

4. A room whose height is 11 ft., and length twice its breadth, takes 143 yds. of paper 2 ft. wide for its four walls; how much carpet will it require?

5. Twoclocks strike 9 together on Tuesday morning.

#### ARITHMETIC.

On Wednesday morning one wants 10 minutes to 11 when the other strikes 11. How much must the slower be put on that they may strike 9 together in the evening?

6. A person bought 43 shares in a coal mine at 354, and kept them till they declined to 114, when he sold out and bought with the proceeds 6 per cent. bank stock at 28 premium; find his annual income from the latter investment.

#### PAPER IV.

1. Define a fraction, and show from your definition that  $\frac{1}{2} = \frac{3}{6}$ . (1) Add together  $\frac{1}{5}$ ,  $\frac{3}{3}$ ,  $\frac{1}{5}$ , and  $\frac{5}{21}$ ; and find what fraction the sum is of  $1\frac{2}{3}$  of  $\frac{4}{2\frac{7}{5}}$ . (2) How many times can .027 be taken from 3.33? What fraction is the remainder of the former?

2. A person left a sum of money which was divided equally amongst 43 poor people, such that, after a deduction of 6d. in the pound, each received £3. 3s.  $4\frac{1}{2}d$ . What sum did he leave?

3. (1) If the carriage of 13 cwt., 2 qrs., 19 lbs. for 35 miles cost £4. 17s. 6d., what must be paid for the conveyance of 41 cwt., 1 lb. for 49 miles? (A cwt. ==112 lbs.) (2) A bankrupt owes \$2085, of which \$235 is due to A, \$325 to B, \$525 to C, and the rest to D. How much must he pay in the \$ so that D may receive as much as is due to C?

4. A merchant buys 2 butts of wine, one for £120, and one for £110, he also buys a third, and after mixing the three, retails the wine at 45s. per dozen, making  $12\frac{1}{2}$  per cent. on his outlay: supposing the number of dozens in a butt to be 52, find the price of the third butt.

5. The price of 2 turkeys and 9 fowls is  $\pounds 2$ . 18s. 6d., and the price of 5 turkeys and 2 fowls is  $\pounds 4$ . 8s. 2d.; find the price of a turkey and a fowl.

6. How long will it take to walk round a square field oantaining 13 ac., 81 yds., at the rate of 3<sup>1</sup>/<sub>2</sub> miles an hour?

# MENTAL ARITHMETIC.

# SECTION VI.

# MENTAL ARITHMETIC.

.48. The following table will be found useful.

Multiplication and Division Table.

_									-	-		_	the second is	-		states the second				_
	20	19	18	17	16	15	14	13	12	1	10	9	8	7	6	CT	4	ω	3	
-	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	UT	#	ω	2	-
2	40	38	36	34	32	30	28	26	24	22	20	18	16	14	12	10	00	0	#	10
e	60	57	54	51	48	45	42	39	36	33	30	27	24	21	18	15	12	9	6	ಲು
4	80	76	72	89	64	60	56	52	48	44	40	36	32	28	$\frac{1}{24}$	20	16	12	8	4
CI	100	95	90	685	08	75	70	65	60	55	50	45	40	35	30	25	20	15	10	CT
6	120	114	108	102	96	90	84	78	72	99	60	54	48	42	36	30	24	18	12	6
7	140	133	126	311	112	105	86	91	84	77	70	63	56	49	42	35	28	21	14	7
8	160	152	144	130	128	120	112	104	96	88	80	72	64	56	48	40	32	24	16	8
9	18(	171	162	15:	144	135	120	117	108	99	90	81	72	63	54	45	36	27	18	9
10	20(	190	2 180	170	16(	150	14(	13(	3 12(	11(	100	90	08	70	60	50	40	30	20	10
11	) 22(	209	198	187	170	165	15	) 14:	) 139	12	11(	66	88	77	66	55	44	3	22	11
12	) 24(	228	3 21(	20	195	18(	1 168	3 15(	2 14	132	) 12(	108	96	84	72	60	48	36	24	12
1	20	22	22	122	20	10	18	16	12	14	1:		10	9	7	6	5	00	12	
	00	17	34 2	1	8	51	32	6.6	6	5	õ	5	4	-	00	CT	10	9	6	
14	085	995	252	38	24	10	96	82	68	54	40	26	12	86	84	70	96	42	28	14
15	300	285	270	255	240	225	210	195	180	165	150	135	120	105	90	75	60	45	30	15
16	320	304	288	272	256	240	224	208	192	176	160	144	128	112	96	08	64	48	32	16
17	340	323	306	289	272	255	238	221	204	187	170	153	136	119	102	35	68	51	34	17
18	360	342	324	306	288	270	252	234	216	198	180	162	144	126	108	90	72	54	36	18
19	380	361	342	323	304	285	266	247	228	209	190	171	152	133	114	95	76	57	38	19
20	400	380	360	340	320	300	280	260	240	220	200	180	160	140	120	100	80	60	40	20

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149. Such questions as 7+8+3, &c., are how many? and 29 less 7, less 6, &c., are how many? or questions in which addition and subtraction are combined, we omit; because, any teacher, by a little practice, can very easily give such exercises to the class, and, moreover, every practical teacher knows that much of the *value* of this part of the Arithmetic depends on the pupil not having seen the questions before the lesson begins.

150. To find the value of 12 things, the value of one thing being given.

RULE. Reckon each penny in the given value as a shilling, and each farthing as 3d.

Ex. Find the value of 12 things at 15<sup>2</sup>/<sub>4</sub>d. each.

By the Rule,

The value req<sup>d</sup>. =  $1s. \times 15 + 3d. \times 3 = 15s. 9d.$ 

Reason for the Process.

12 things at 1d. each = 1s.;  $\therefore$  12 at 15d. each = 1s.  $\times$  15 = 15s 12 .....  $\frac{1}{4}d$ . .... = 3d.;  $\therefore$  12 at  $\frac{3}{4}d$ . .... = 3d.  $\times$  3 = 9d.;  $\therefore$  12 things at 15 $\frac{3}{2}d$ . each = 15s. 9d.

151. To find the value of 24 things, the value of one thing being given.

RULE. Reckon each penny in the given value as 2s, and each farthing as 6d.

152. To find the value of 48 things, the value of one thing being given.

RULE. Reduce the given value into farthings, the result reckoned as so many shillings will be the value required.

Ex. Find the value of 48 things at 18<sup>2</sup>d. each.

By the Rule, since  $18 \pm d. = 75q$ .,

the value req<sup>d</sup>. = 75s. = £3. 15s.

Reason for the Process.

48 things at  $\frac{1}{4}d. = 48q. = 1s.$ ;

 $\therefore$  48 things at  $75q. = 1s. \times 75 = 75s. = £3. 15s.$ 

153. To find the value of 144 things, the value of one thing being given.

RULE. (1) Find the value of 12 things by Rule 150: then consider this value as the value of one thing, and apply Rule 150 a second time.

Ex. Find the value of 144 things at 131d. each.

Value of 12 things = 13s. + 6d. = 13s. 6d.

Value of 144 things = 13s.  $\times 12 + 6s$ . = 156s. + 6s.  $= \pounds 3.2s$ . 154. The following general Rule may be given "for finding the value of any number of things, the value of one thing being given."

RULE. Reckon how many dozens are contained in the given number, and how many single things remain over. Then by Rule 150, find the value of one dozen, which value multiply by the number of dozens, and add to the result the price of the single things which remained over.

Ex. Find the value of 38 things at 4s. 7d. each.

 $38 = 3 \times 12 + 2,$ 

value of 12 things =  $\pounds 2$ . 8s. + 7s. =  $\pounds 2$ . 15s.  $\therefore \dots 12 \times 3 \dots = \pounds 2$ . 15s.  $\times 3 = \pounds 8$ . 5s.  $\therefore \dots 2 \dots = 4s$ . 7d.  $\times 2 = 9s$ . 2d.  $\therefore \dots 38 \dots = \pounds 8$ . 5s. + 9s. 2d. =  $\pounds 8$ . 14s. 2d.

#### Ex. LXXX.

1. Find t	the value of 1	2 articles at the	following prices
for a single a	rticle. (1) 3	l. (2) $2d.$ (3)	) $5d.$ (4) $7d.$
(5) 11d. (6)	$1\frac{1}{2}d.$ (7) $2\frac{1}{4}d$	$(8) 3\frac{3}{4}d.$ (9)	$6\frac{1}{2}d.$ (10) $8\frac{1}{4}d.$
(11) $10\frac{1}{2}d$ .	(12) 1s. $0\frac{3}{4}d$ .	(13) 1s. 4d.	$(14)$ 1s. $6\frac{1}{4}d$ .
(15) 1s. $9\frac{3}{4}d$ .	(16) 1s. 8d.	(17) 1s. 111d.	(18) 1s. $2\frac{3}{4}d$ .
(19) 2s. 7d.	$(20)$ 3s. $0\frac{1}{4}a$	(21) 4s. 4d.	(22) 6s. $1\frac{3}{4}d$ .
(23) 7s. 9d.	(24) 8s. 51d.	(25) 11s. 7 <sup>3</sup> / <sub>4</sub> d.	(26) 13s. 2d.
(27) 16s. 31d	l. (28) 18s. 14	d. (29) 19s. 9d.	(30) 19s. $6\frac{3}{4}d$ .

2. At the prices named as the value of a single article in (1) to (12) inclusive in the last question find the value of 24 articles; at the prices named in (13) to (20) inclusive find the value of 48 articles; and at the prices named in (21) to (30) inclusive find the value of 144 articles.

3. At the prices named as the value of one article in quest<sup>n</sup>. 1. (6) to (20) inclusive, find the value of (1) 13; (2) 21; (3) 28; (4) 35; (5) 41; (6) 44; (7) 57; (8) 72; (9) 153; (10) 182 articles.

155. To find the value of 20 things, the value of one thing being given.

RULE. Reckon each shilling in the given value as  $\pounds l$ , and if there be pence, reckon each penny as the twelfth of  $\pounds l$ , thus 1d. as 1s. 8d., and if there be farthings, each farthing as one-fourth the value of each penny, or 1q. as 5d. &c.

Ex. Find the value of 20 things at 2s. 8<sup>1</sup>/<sub>2</sub>d. each.

By the Rule,

The value required =  $\pounds 1 \times 2 + (1s. 8d.) \times 8 + 5d. \times 2$ . =  $\pounds 2 + 13s. 4d. + 10d. = \pounds 2. 14s. 2d.$ 

Reason for the Process.

20 things at 1s. =  $20s. = \pounds 1$ ;  $\therefore$  20 things at 2s. =  $\pounds 1 \times 2 = \pounds 2$ ,

20 things at 1d. = 1s. 8d.;  $\therefore$  20 things at 8d. = 1s. 8d.  $\times 8 = 13s. 4d.$ 

20 things at  $\frac{1}{2}d. = \frac{1s. 8d.}{2}$ , or 20 things at  $\frac{1}{2}d. = 10d.$ ;

... value of 20 things at 2s.  $8\frac{1}{2}d. = \pounds 2$ . 14s. 2d.

156. To find the value of 100 things, the value of one thing being given.

RULE. Reckon each shilling in the given value as  $\pm 5$ ; reduce the pence and farthings in the given value to farthings, then reckon each farthing as equal to 2s. 1d.

Ex. Find the value of 100 things at 2s.  $5\frac{1}{2}d$ . each.

By the Rule, since  $5\frac{1}{4}d_{1} = 21q$ .

The value req<sup>d</sup>. =  $\pounds 5 \times 2 + 2s$ .  $\times 21 + 1d$ .  $\times 21$ .

 $= \pounds 10 + \pounds 2. 2s. + 1s. 9d. = \pounds 12. 3s. 9d.$ 

Reason for the Process.

100 things at  $1s = \pm 5$ ;  $\therefore$  100 things at  $2s = \pm 5 \times 2 = \pm 10$ .

Again since 1d. = 4q., taking 1q. as equal to 1d., we multiply by 4.

Also, since  $2s_{\cdot} = 96q_{\cdot}$ , taking  $1q_{\cdot}$  as equal to  $2s_{\cdot}$ , we multiply by 96;

.: taking 1q. = 2s. + 1d., we multiply by 96 + 4, or 100.

157. To find the interest of any sum of money for any number of months at 6 per cent.

RULE. Divide the number of months by 2; the quotient is the interest in cents of \$1 for the given time; multiply the quotient by the given principal and the product is the interest required.

Ex. 1. Find the interest on \$78.56 for 2 yrs., 7 mo., at 6 per cent. per annum.

By the Rule,

2 yrs. 7 mo. = 31 months;  ${}^{s_1}_{2} = 15\frac{1}{3}$ . .: in<sup>t</sup>. req<sup>d</sup>. =  $15\frac{1}{3} \times $78.56 = $319.1768$ .

### Reason for the Process.

The interest of \$1 for 1 month --- 1 cent.

... half the number of months will express the interest in cents of \$1 for the given time.

Note 1. It will be quite easy to obtain from the above the interest at any other rate than 6 per cent.; by first obtaining the interest as directed above and then by Practice to add or subtract as the case may require.

Ex. 2. Find the interest of \$80 for 15 months at 8 per cent. per annum.

At 6 per cent. in<sup>t</sup>. = \$6, as by the above Rule;

$$at 8 per cent. in = $6 + \frac{1}{3} of $6.$$

= \$8.

Ex. 3. Find the interest on \$110 for 10 months at 5 per cent. per annum.

At 6 per cent. in<sup>t</sup>. = 5.50 by the Rule:  $\therefore$  at 5 per cent. in<sup>t</sup>. = \$5.50 -  $\frac{1}{6}$  \$5.50. = \$5.50 - 91 $\frac{2}{3}$  cents.

#### = \$4.58 $\frac{1}{3}$ .

Note 2. If there are days in the question, the interest may be found for \$1 by dividing the days by 6 and reckoning the quotient tenths of a cent. which being added to the result obtained in the Rule, will give the interest of \$1 for months and days, and consequently for any amount.

Ex. 4. Find the interest on \$90 for 6 months and 24 days at 6 per cent per annum.

In<sup>t</sup>. on 1 = 3.4 cents, by the Rule:

 $\therefore$  in<sup>t</sup>. on \$90 = 3.4 cents × 90.

= \$3.06.

#### Ex. LXXXI.

Find the interest at 6 per cent. per annum: (1) On \$37 (2) On \$42 for 6 months. (3) On \$55 for 8 for 4 months. months. (4) On \$75 for 10 months. (5) On \$110 for 7 months. (6) On \$38.50 for 9 months. (7) On \$84.25 for 12 months. (8) On \$120 for 15 months. (9) On \$228 for 18 months. (10) On \$678.50 for 8 months. (11) On \$422.25 for 9 months. (12) On \$328.50 for 9 months.

### Ex. I. (p. 10.)

1. 3, 4, 2, 7, 9, 6, 8. 2. 10, 1, 12, 19, 5, 11, 16. 3. 14, 20, 27, 33, 49, 60, 55, 17, 36. 4. 88, 35, 63, 29, 76, 80, 94, 13, 52. 5. 9, 10, 11, 12, 13, 14, 15, 16, 17; 46, 47, 48, 49, 50, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98.

### Ex. II. (p. 11.)

1. 106, 150, 200, 287, 310, 431, 555, 919, 867.

2. 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213; 612, 613, 614, 615, 616, 617, 618, 619; 948, 949, 950, 951, 952, 953, 954, 955, 956, 957, 958, 959, 960, 961, 962, 963, 964, 965, 966, 967, 968, 969.

### Ex. III. (p. 12.)

1. 4585, 7321, 9798, 7006.

2. 5004, 5400, 5040, 8036, 8306, 8360, 9909.

3. 75635, 90909, 10004, 87050, 90001, 64064, 83000.

### Ex. IV. (p. 13.)

**1.** 105, 8790, 37071, 30402, 77700, 24817. **2.** 105409, 8008013, 7650090, 64000400, 89044001.

504623024, 900300800, 53000503.

3. 6006070007, 83401001010, 7004089200, 990000000.

### Ex. V. (p. 14.)

1. Seven, thirteen, four, nine, eighteen, five, twenty, eleven, five, fifty, thirty-four, twenty-nine, three, seventeen, fiftythree.

2. Nineteen, eight, forty-one, eighty-eight, twenty-seven, seventy-two, ninety-four, forty-nine, sixteen, sixty-one, ninety-eight, eighty, fifty-six, twenty-eight.

3. One hundred and seven, one hundred and seventy, seventeen, four hundred and thirty, six hundred and ninetyone, eighty, eight hundred, eight, nine hundred and fifty-six, eight hundred and three, six hundred and eighty-four.

4. Four thousand five hundred and six, five thousand eight

hundred and seventy, five thousand and eighty-seven, six thousand nine hundred, six thousand and nine, two thousand five hundred and eighty, seven thousand and forty-five, seven thousand five hundred and ninety-one, six thousand two hundred and seventy-five.

5. Twenty-four thousand seven hundred and fourteen, twelve thousand five hundred, ten thousand and twenty-five, ten thousand two hundred and five, seventy thousand four hundred and fifty-seven, seventy-four thousand and seven, seventy-seven thousand.

6. Three hundred thousand eight hundred and sixty-three, thirty millions eighty thousand six hundred and thirty, ninety-six millions four hundred thousand two hundred and fifty, eight hundred millions four hundred thousand three hundred and seven, five hundred and seventy-two millions sixty thousand four hundred and ninety-five.

7. One hundred and twenty millions one hundred and ninety-two thousand seven hundred and three, eight hundred and ninety millions six hundred and forty-seven thousand five hundred and sixty, one billion and fifty millions sixty thousand four hundred and twenty-nine, one hundred billions and one.

### Ex. VL. (p. 16.)

1. 19. 2. 27. 3. 26. 4. 11; 16; 18; 18; 23; 17; 15; 18; 25. 5. 25; 20; 34; 28; 36; 45; 46. 6. 29 boys. 7. 12 yrs. 8. 30 chickens.

# Ex. VII. (p. 19.)

 1. 37.
 2. 69.
 3. 99.
 4. 99.
 5. 95.
 6. 71.

 7. 115.
 8. 110.
 9. 200.
 10. 214.
 11. 213.
 12. 186.

 13. 214.
 14. 241.
 15. 503.
 16. 1741.
 17. 2133.

 18. 1540.
 19. 2201.
 20. 1364.
 21. 1920.
 22. 1549.

 23. 1551.
 24. 2514.
 25. 1665.
 26. 2451.
 27. 2148.

 28. 2018.
 29. 14658.
 30. 27640.
 31. 27832.
 32. 35735.

 33. 28260.
 34. 29635.
 35. 28207.
 36. 100 marbles.

 37. 287.
 38. 9770.
 39. \$42068.
 40. 3554 oranges.

#### Ex. VIII. (p. 20.)

### Ex. IX. (p. 21.)

### Ex. X. (p. 25.)

### Ex. XI. (p. 26.)

 1. 1921.
 2. 3711.
 3. 999.
 4. 2239.
 5. 4484.
 6.

 1929.
 7. 3205.
 8. 4684.
 9. 3401.
 10. 7889.
 11. 3025.

 12. 806.
 13. 25184.
 14. 21023.
 15. 8.
 16. 18173.

 17. 168079.
 18. 8639494.
 19. 19075299.
 20. 555939946.

 21. 2399; 997833.
 22. 5986.
 23. 15022.
 24. 1891; 72.

 25. 68; 140.
 26. \$217 in debt.
 27. 19th step from bottom, 26th step from the top.
 28. 5 officers, 58 children, 47

 able-bodied, 23 infirm.
 29. 682.
 30. 45718.
 31. 7096305.

 32. 56289613.
 33. 66291414.
 34. \$260.
 35. \$\$337588.

#### Ex. XII. (p. 28.)

1. III; VII; XI; IX; XII; XVI; XVIII; XXV; XXVIII; XXXVII; XL; LIII; LIX; LXII; LXXVII; LXXXIV; CIII; CLVII; CXC; CC; DCLI; DCCLXXXIII; MCCIV; MDXXVII; MDCCCLXV.

2. three, 3; six, 6; eight, 8; thirteen, 13; fifteen, 15; seventeen, 17; twenty, 20; fifty-four, 54; eighty-one, 81; one hundred and eleven, 111; six hundred and five, 605; five thousand and two, 5002; one million one hundred thousand, 1100000; two thousand, 2000; seven hundred and forty-nine, 749; one thousand eight hundred and sixty-five, 1865.

#### Ex. XIII. (p. 30.)

1. 10	6. 2. 94	. 3. 176.	4. 112.	5. 144.	6. 180.
7. 87.	8. 225.	9. 108.	10. 204.	11. 332.	12. 450.
13. 335	. 14. 215	. 15. 216.	16. 594.	17. 468.	18. 189.
19. 371	. 20. 360	. 21. 616.	22. 621.	23. 486.	<b>24.</b> 200.

 25. 990.
 26. 583.
 27. 957.
 28. 1001.
 29. 720.
 30. 588\*

 31. 1374.
 32. 2400.
 33. 2091.
 34. 1104.
 35. 3885.

 36. 2982.
 37. 3353.
 38. 6335.
 39. 6680.
 40. 4383.

 41. 5600.
 42. 5918.
 43. 10656.
 44. 8448.
 45. 429

 bushels, 2574 shillings.
 46. 756 pence, 1764 pence, 3024

 pence.
 47. 44 cents.
 48. 44.
 49. 885.

### Ex. XIV. (p. 31.)

1. 18096. 2. 11698. 3. 29619. 4. 114228. p, 24228. 6. 485340. 7. 416160. 8. 404825. 9. 3073630. 10. 388064. 11. 231483. 12. 346284. 13. 590592. 14. 833184. 15. 234927. 16. 1098444. 17. (1) 7740984, 19352460, 11611476, 27093444, 15481968, 34534428, 23222952, 30963936, 42575412, 46445004. (2) 9219516, 23048790, 13829274, 32268306, 18439032, 41487822, 27658548, 36878064, 50707338, 55317096. (3) 171947728, 429869320, 257921592, 601817048, 343895456, 773764776, 515843184, 687790912, 945712504, 1031686368. (4) 18181706, 45454265, 27272559, 63635971, 36363412, 81817677, 54545118, 72726824, 99999383, 10990236. (5) 111760184, 279400460, 167640276, 391160644, 223520368, 502920828, 335280552, 447040736, 614681012, 670561104, (6) 1975308642, 4938271605, 2962902963, 6913580247, 3950617284, 8888888889, 5925925926, 7901234508,10864197531, 11851851852. 18. 98 miles. 19. 888 miles.

#### Ex. XV. (p. 34.)

1. 8334.	2. 18306.	3. 9108. 4. 324	154. 5. 57706.
6. 32643.	7. 23790. 8.	22385. 9. 7734	41. 10. 42182.
11. 50516.	12. 79992.	13. 218075.	14. 281504.
15. 45468.	16. 303102.	17. 6964704.	18. 4328192.
19. 183150.	20. 331200.	21. 308163.	22. 250200.
<b>23.</b> 725912.	24. 1619723.	25. 52470000.	26. 492463028.
27. 78510330	000. 28. 2	44366672.	29. 140645085.
30. 35344677	2. 31. 3	44115512.	32. 736924245.
<b>33.</b> 66350308	34. 5939	28000000.	35. 8106030522.
<b>36.</b> 62243916	<b>6. 37. 331</b> 46	651; 136850000	0; 791627400;
28081286275	15. 38. 148672	. 39. (1) 61299	; (2) 51480000.
40. See 15, 1	6, 17, 18.		

### Ex. XVI. (p. 34.)

	1.	43042883.	2.	131296032.	3.	4916047	312.	4. 43506216.
5.	3	1884470.		6. 8878998	308	18.	7.	66260991808.
8.	4	0880656300.		9. 6931223	347	60 <b>02.</b>	10.	18381130075,
11		10045336541	1.	12. 15759	361	0868.	13.	\$943214050.

L

 14.
 27416327796.
 15.
 109588282650.
 16.
 60435674536845.

 17.
 495562849756.
 18.
 67226401140.
 19.
 18834779670.

### Ex. XVII. (p. 37.)

1. 144, 97, 11; 158, 108, 118; 168, 108, 128; 171, 114, 127; 164, 111, 124.

2. 21,  $9_{11}^{6}$ ,  $10_{10}^{5}$ ; 22, 10, 11;  $23_{5}^{4}$ ,  $10_{11}^{9}$ ,  $11_{10}^{9}$ ;  $25_{5}^{3}$ ,  $11_{11}^{7}$  $12_{10}^{8}$ ;  $23_{5}^{2}$ ,  $10_{11}^{7}$ ,  $11_{10}^{7}$ .

3.  $21_{6}^{4}, 10_{12}^{10}, 11_{11}^{9}; 23_{6}^{3}, 11_{12}^{9}, 12_{11}^{9}; 25_{6}^{3}, 12_{12}^{9}, 13_{11}^{10}; 28,$ 14,  $15_{11}^{3}$ ;  $24_{6}^{3}$ ,  $12_{12}^{3}$ ,  $13_{11}^{4}$ .

4.  $28_{6}^{4}, 21_{8}^{4}, 14_{12}^{4}; 32_{6}^{3}, 24_{8}^{3}, 16_{12}^{3}; 34_{6}^{2}, 25_{8}^{6}, 17_{12}^{2}; 42_{6}^{5}, 32_{8}^{4},$  $21_{12}^{5}$ ; 40, 30, 20.

5.  $115_4^2$ ,  $46_{10}^2$ , 42;  $170_4^2$ ,  $68_{10}^2$ , 62; 210, 84,  $76_{11}^4$ ; 1014,  $40_{10}^{5}, 36_{11}^{9}; 138_{4}^{3}, 55_{10}^{5}, 50_{11}^{5}$ 

6.  $54_{11}^{e}$ , 75, 50;  $69_{11}^{4}$ ,  $95_{8}^{3}$ ,  $63_{12}^{7}$ ;  $76_{11}^{e}$ ,  $105_{8}^{2}$ ,  $70_{12}^{2}$ ;  $90_{11}^{9}$ .  $124\frac{7}{8}, 83\frac{3}{12}; 65\frac{2}{11}, 89\frac{5}{8}, 59\frac{9}{12}.$ 

7. 1344, 10018, 110; 764, 573, 6254; 7847, 5887, 6424; 5555, 416 8, 454 F.

8.  $345, 230, 276; 1200 \pm 800$  12, 960  $10; 1033 \pm 688$  12, 826  $70; 1033 \pm 688$ 818<sup>4</sup>/<sub>8</sub>, 545<sup>8</sup>/<sub>12</sub>, 654<sup>8</sup>/<sub>10</sub>.

9.  $7187_{12}^{2}$ ,  $8624_{10}^{6}$ ,  $12320_{7}^{6}$ ;  $6052_{12}^{11}$ ,  $7263_{10}^{5}$ ,  $10376_{7}^{3}$ ;  $7124_{12}^{2}$ ,  $8549, 12212\frac{6}{7}; 2941\frac{6}{12}, 3529\frac{8}{10}, 5042\frac{4}{7}.$ 

10.  $6909_{7}^{3}$ ,  $9500_{7}^{3}$ ,  $6333_{7}^{6}$ ;  $8182_{7}^{7}$ ,  $11251_{8}^{1}$ ,  $7500_{7}^{9}$ ; 4820,7, 66283, 441811.

11.  $683837\frac{2}{8}$ ,  $547069\frac{3}{10}$ ,  $497336\frac{2}{11}$ ;  $11712585\frac{2}{8}$ ,  $9370068\frac{2}{10}$ .

cents. 16. 7 plums. 17. 506. 18. 11946419. 19. Cook received \$561, man-servant \$1122, housekeeper \$2244. 20. 1728. 21. 6. 22. 26 oranges. 23. 35 penknives.

### Ex. XVIII. (p. 41.)

**1.** 12; 40; 53; 94. 2. 45; 29; 65; 97. 3. 57; 79; 88; 73. **4.** 215 798; 885; 102. 5. 805; 682; 127; 357; 460; 7090. 6. 379; 407; 940; 738; 93845796; 580073. 7. 347; 569; 3094. 8. 1987; 7071; 650. 9. 9009; 5436; 388. 10. 21503 rem. 5; 3450; 124 rem. 477. 11. 57096; 76542; rem. 136; 4655 rem. 603. 12. 103944; 175971 rem. 66; 87039; 84003; 967427210 rem. 61. 13. 190182; 4623; 50301; 87366 rem. 6076. 14. 2007 rem. 1; 20300: 65839 rem. 2; 31352. 15. 902468 ; 1754 rem. 129; 14957000; 770071. 16. 37810; 3250450. 73086413. 1. 1799. 18. 180 pairs.

19. 141. 20. 360 rem. 52. 21.  $3\frac{1}{2}\frac{1}{6}$ . 22. 3. 23. 1000. 24. 420. 25. 403. 26. 372547. 27. 17129. 28. 10.

#### Ex. XIX. (p. 43.)

1.  $3_{10}^4$ ,  $4_{10}^3$ ,  $5_{10}^6$ , 8,  $13_{10}^5$ , 26,  $150_{10}^4$ ;  $1\frac{14}{20}$ ,  $2_{20}^3$ ,  $2\frac{16}{20}$ , 4,  $6\frac{15}{20}$ , 13,  $75_{\frac{4}{20}}$ ;  $1_{\frac{4}{20}}$ ,  $1_{\frac{3}{8}}$ ,  $1_{\frac{3}{8}}$ ,  $2_{\frac{3}{8}}$ ,  $4_{\frac{1}{5}}$ ,  $8_{\frac{3}{8}}$ ,  $50_{\frac{4}{30}}$ .

2. 537, 21, 1633, 748, 15048, 19548, 203048, 8195; 357, 14,  $11_{\frac{18}{66}}, \frac{451}{66}, 100_{\frac{10}{66}}, 130_{\frac{2}{66}}, 1353_{\frac{4}{66}}, 5463_{\frac{2}{66}}; 3_{\frac{7}{6}}, 12, 9_{\frac{7}{6}}, \frac{4_{11}}{4_{16}},$  $85_{70}^{69}, 111_{70}^{59}, 1160_{70}^{29}, 4682_{70}^{69}; 2_{100}^{37}, 8_{100}^{49}, 6_{100}^{78}, 2_{100}^{91}, 60_{107}^{19},$  $78_{100}^{20}$ ,  $812_{100}^{29}$ , 3278;  $1_{200}^{37}$ ,  $4_{200}^{40}$ ,  $3_{200}^{73}$ ,  $1_{200}^{91}$ ,  $30_{200}^{19}$ ,  $39_{200}^{20}$ 406-29, 1639.

3.  $329_{246}^{38}$ ,  $28_{246}^{150}$ ,  $3708_{246}^{141}$ ;  $79_{1600}^{48}$ ,  $6_{1000}^{870}$ ,  $890_{1600}^{61}$ ;  $52_{1500}^{1048}$ ,  $4_{1500}^{870}$ ,  $593_{1500}^{561}$ ;  $30_{2600}^{1048}$ ,  $2_{2600}^{1670}$ ,  $342_{2600}^{361}$ ; 8306 78103490

4.  $88976\frac{7}{5}\frac{653}{667}$ . 5.  $8678\frac{2}{7}\frac{4919}{6602}$ . 6.  $66970\frac{7}{8}\frac{1}{9}\frac{6}{6}$ . 7.  $7096\frac{63}{2}\frac{53}{5}\frac{53}{6}$ . 8. 9992461 806. 9. 21446 5919. 10. 1302 637. 11. 1100, 916 and 800 men over. 12. 956

### Ex. XX. (p. 51.)

 
 1. 681440 far.
 2. 1085070 inches.
 3. 4167680 drs.

 4. 3842027640 sq in.
 5. 8092505 ls.
 6. 31518396 sq, in.

 7. 24480 mins.
 8. 16820 grs.
 9. 15620 yds.

 10. 1074088 c. in.
 11. 440 gills.
 12. 7040 qts.

 13. 2030400 mins.
 14. 158304 grs.
 15. 276400 grs.

 16. 96425 half-pence.
 17. 1062864 sq. yds.
 18. 3499 nls.

 19. 2231906 far.
 22.02026 far.
 24. 60400 mrs.
 21. 92160 secs.
 22. 530784 in. 23. 300362 far. 24. 604800 grs. 25. 520 nls. 26. 888 nls. 27. 544345 far. 28. 82800 scs. 29. 378 galls. 30. 192938 far.

 
 Ex. XXI.
 (p. 53.)

 1. £128 8s. 6½d.
 2. 2 lbs. 3 oz. 8 dwt. 20 grs.

 3. 2273 galls. 3 qts. 1 pt.
 4. 403 lea. 2 mls. 7 fur. 16 po.
 5. 3 tons 18 cwt. 1 qr. 14 lbs. 14 oz. 6. 586 ac. 1 ro. 27 po. 7. 29 lbs. 1 oz. 12 dwt. 4 grs. 8. 11517 mls. 1 fur. 27 po. 2 yds. 11 in. 9 ls.

9. 14997 tons 8 cwt. 1 qr. 14 lbs. 10 oz. 12 drs.

9. 14957 5018 5 CWL, 1 qr. 14 105, 10 02, 12 drs. 10. 1 ml. 7 fur. 14 po. 2 ft. 9 in. 11. 17 lbs. 3 dwt. 14 grs. 12. 3 tons 19 cwt. 1 lb. 6 oz. 13. 122 lbs. 3 drs. 17 grs. 14. 2 wks. 5 dys. 23 hrs. 58' 13". 15. 35 ac. 2 ro. 20 po. 16. 297 c. yds. 17. 198 ac. 1 ro. 15 po. 16 $\frac{1}{2}$  yds. 18. 31 yds. 1 qr. 19. 36° 24' 35". 20. 365 dys. 6 hrs. 21. 506 hhds. 19 gats. 2 qts. 22. 506 hhds. 14 gals. 1 qt. 23. 15211 bu. 55 lbs. 24. 29411 bu. 26 lbs. 25. 121 bu. 3 lbs. 26. \$307.47. 27. £1014 4s. 33d.

#### Ex. XXII. (p. 54.)

1. \$94.64. 2. £20. 12s. 3d. 3. 10 qrs., 24 lbs., 1 oz. 4. 107 lbs., 1 oz., 10 dwt., 17 grs.
 5. 55 lbs., 1 oz., 5 drs., 2 sc., 1 gr. 6. \$17255.22. 7. 288 tons, 2 cwt., 2 qrs., 23 lbs. 8. 578 yds., 2 qrs. 9. 79 mls., 3 fur., 9 per., 3 yds. 10. £145. 17s. 11d. 11. 116 dys., 8 hrs., 35', 12". 12. \$8470.12. 13. 42 ac., 2 ro., 25 po., 5 ft., 40 in. 14. 99 tons, 8 cwt., 3 qrs., 12 lbs., 11 oz., 15 drs. 15. \$11040. Ex. XXIII. (p. 56.) 1. £15. 8s. 6d. 2. 9 lbs., 11 oz., 3 drs., 16 grs. 3. 2 lbs., 10 oz., 7 dwt. 4. 2 mls., 6 fur., 35 po., 1 yd. 5. 13 yds., 1 qr., 2 nls., 2 in. 6. 28 e. yds., 23 c. ft., 1443 in. 7. 1 ac., 2 ro., 38 po., 1 yd., 2 ft., 142 in. 9. £53. 17s. 10<sup>2</sup>d. 8. 5 dys., 9 hrs., 49 min., 57 sec. 10. 2 qrs., 15 lbs., 11 oz., 14 drs. 11. \$1068.89. 12. 95 cords, 110 c. ft. 13. \$27.69. 14. 107 ac., 2 ro., 34 po., 29 yds., 7 ft., 118 in. 15. 79 c. yds., 21 c. ft., 1377 c. in. 16. 27 mls., 29 per., 1 ft., 10 in. 1 18. 5 tons, 16 cwt., 2 qrs., 23 lbs., 11 oz., 1 dr. 17. 6°, 39′, 39″. 19. 10 yds., 2 qrs., 2 nls., 2 in. 20. 70 bu., 2 pks., 1 gal., 2 qts. 21. 673 bu., 1 gal., 2 qts. Ex. XXIV. (p. 58.) 2. 52 lbs., 5 oz., 4 drs. 1. £24. 19s. 3. 74 lbs., 1 oz., 1 dwt., 16 grs. 4. 139 yds., 2 qrs., 3 nls. 5. 167 mls., 6 fur., 1 per., ½ yd. 6. \$1660.33. 7. 129 cwt., 1 qr., 11 lbs., 7 oz., 8 drs. 8. 58 mls., 5 fur., 18 po., 1 yd., 9 in. 9. \$6099.30. 10. 86 wks., 8 hrs., 56 min. 11. 95 ac., 36 per., 3 ft. 12. £146. 3s. 61d. 13. 899 lbs., 8 oz., 4 drs. 14. 23 bu., 1 pk., 3 qts. 15. 21 dys., 15 hrs., 50 min. 16. 50103 gals., 2 qts., 1 pt. 17. 4382 dys., 21 hrs., 47 min., 24 sec. 18. £812. 15s. 01d. 19. 134 ac., 3 ro., 31 po. 20. \$3572.16. 22. £840. 11s. 6d. 21. 25043 bu., 2 pks., 1 gal. 23. 219 lbs., 8 oz., 10 dwt., 12 grs. 24. \$7342. 25. £159. 15s. 6<sup>3</sup>/<sub>4</sub>d. 26. \$22503. 27. 381 mls., 12 po., 2 yds. Ex. XXV. (p. 59.) 1. 1583 ac., 2 ro., 12 po. 2. 1500 mls., 6 po. 3. £2817. 128.

4. 1621 lbs., 4 oz., 15 dwt., 13 grs. 5. £351. 13s. 9d.

6. 1484 yds., 2 qrs., 2 nls. 7. 188 cwt., 22 lbs., 11 oz., 10 drs. 8. £5912. 4s. 92d. 9. \$7321.30. 10. 1493 c. yds., 11 c. ft., 1332 in.

11. 182 lbs., 10 oz., 1 dwt., 13 grs. 12. £3743. 7s. 10d. 13. 688 dys., 6 hrs., 40 min. 14. 6297 lbs., 11 oz., 4 drs.

15. 33272 Ibs., 1 oz., 18 dwt., 6 grs. 16. £3676. 13s. 10<sup>1</sup>/<sub>2</sub>d. 17. 1319 ac., 0 ro., 0 po., 13 yds., 4 ft., 48 in.

1034 mls., 2 fur., 4 po., 3 in.
 19. £2100. 18s. 9d.
 20. \$118575. 21. 8500 bushels.

#### Ex. XXVI. (p. 61.)

1. 352 cwt., 2 qrs., 21 lbs., 13 oz. 2. 33772 lbs., 10 oz., 18 dwt., 15 grs. 4. 1870 cwt., 3 qrs., 23 lbs., 4 oz., 5 drs. 6. 10826 lbs., 8 oz., 5 drs., 2 sc., 4 grs. 8. \$66.04. 9. \$97.50. 10. 12 cwt., 1 qr., 7 lbs., 8 oz. 11. \$40000.

### Ex. XXVII. (p. 63.)

1. £55. 15s. 1#d. 2. 29 lbs., 8 oz., 3 dwt., 6 grs. 3. 24 mls. 1 fur., 19 po., 3 yds., 10 in. 4. 23 yds., 2 nls. 5. 144 lbs., 3 oz., 4 drs., 8 1 grs. 6. £188. 19s. 93d. 7. 2 tons, 10 cwt., 12 lbs., 10 oz., 102 drs. 8. 17 ac., 1 ro., 30 po., 10 yds., 6 ft., 5513 in. 9. 3 qrs., 11 lbs., 13 oz., 5488 drs. 10. 6 mls., 7 fur., 14 po., 3,687 in. 11. 6 bu., 1 pk., 1 gal., 58 pt. 12. £52. 16s. 23d. 13. 4 lbs., 4 oz., 1 dr., 1 scr., 1153 grs. 14. 7 fur., 23 po., 5 yds., 1 in., 1211 ls. 15. 1 ac., 1 ro., 9 po., 22 yds., 5 ft., 14192 in. 16. 1 ton, 1 cwt., 3 qrs., 2 lbs., 12 oz., 10564 drs. 17. 5 c. yds., 11 c. ft., 961128 c. in. 18. 4 lbs., 4 oz., 3 drs., 1 sc., 1112 grs. 19. 4 lbs. 10 oz., 1 dwt., 9390 grs. 20, £2. 10s. 6137d. 21. 13s. 71d. 22. 115 dys., 5 hrs., 54 min., 22389 sec. 23. \$8.49181. 34. \$13.39398. 25. \$1.64142. \$1.91417. 26. \$4.65. 27. \$1.15. 28. \$2.5344. Ex. XXVIII. (p. 64.) 1. 9 times. 2. 3 times. 3. 436 times. 4. 3 times. 5. 25335 times. 6. 8252 times. 7. 9 times. 8. 24 times. 9. 75 times. 10. 65 times. 11. 100 times. Ex. XXIX. (p. 65.)

1. \$101.25. 2. \$231.85. 3. \$831.531. 4. \$615.681.

5. 9. 13.	$\$3650.50.$ 10. $\$279.12\frac{1}{2}.$ $\$3650.50.$ 10. $\$2845.09\frac{1}{2}.$ $\$8069.33\frac{1}{3}.$ 14. $\$301.94\frac{1}{2}.$	7. \$2451.982. 11. \$4468.125. 15. \$151.725.	8. \$253.96 <sup>1</sup> . 12. \$189.55. 16. \$350.75.
1. 4. 7. 10.	Ex. XXX           £54. 6s. 3d.         2. £81           £21. 2s. 6d.         5. £18.           £216. 19s. 4½d.         8. £2           £484. 6s.         11. £555. 1	. (p. 66.) . 17s. 9d. 19s. 9d. 6. 290. 12s. 9. Is. 5§d. 12.	3. £4. 6s. 9d. £31. 6s. 10½d. £348. 8s. 1½d. £946. 7s. 4§d.
	Ex. XXXI	(p. 66.)	1
1. 5. 6.	117984. 2. 107766. 2 mls., 6 fur., 13 per., 5 yds 1st, \$5.60, \$17.17; 2nd, \$11	3. 3653012. s., 1 ft., 10 in. l.57.	4. 1898307.
	PAPE	R II.	
1. 3.	£362. 19s. 9d. 183 ac., 1 ro., 24 per., 26 yd	ls., 7 <del>155</del> ft.	2. \$63.47.
4.	$$9.48\frac{4}{27}$ . 5. 5 dresses, £2.	15s. $7\frac{1}{4}d$ . each.	6. \$3227.42.
1. 4. 5. 6.	£46. 14s. 6d. 2. \$7000, \$21 1 ro., 18 po., 5 yds., 2 ft., an 17 cwt., 1 qr., 8 lbs., 10 oz., 6 hours, 54 min.	6 111. 000, \$35000. 3. ad 16 <u>4</u> ft. over. 5 drs., and 89 d	£13. 12s. 9d. Irs. over.
1. doz 5.	\$148.15. 2. 11, 18. 3. 9 sen; owner of boat, 16 d 2301696 pores. 6. 42000, 42	0, 18, 27. 4. o ozen; each ma 2889.	wner of net, 8 n, 32 dozen.
	PAPE	R. V.	
1. 5.	6255647664981. 2. 861447 465335. 6. 95587.	920. 3. 11904	. 4. 12752.
1. 5.	PAPER 657872. 2. \$16496471. 3. 136 ac., 3 ro., 14 po., $24_{1270}^{$75}$	8 VI. \$10444830.63. yds. 6. 63433	4. 62284 lbs. 38.
	Ex. XXXII	(p. 71.)	
1. 2 10. 17. 23.	2.         2.         3.         2.         4.         4.         5.         2.         11.         58.         12.         63.         13.         none.         18.         8.         19.         26.         2         7056.         24.         11.         25.         17.         25.         17.	4. 6. 3. 7. 2. 2. 14. 30. 14 20. 352. 21. 13 26. 31.	8. 6. 9. 4. 5. 10. 16. 8. 1. 22. none.

### Ex. XXXIII. (p. 72.)

1. 20. 2. 72. 3. 144. 4. 1260. 5. 240. 6. 168. 7. 525. 8. 1056. 9. 1050. 10. 2520. 11. 11088. 12. 450. 13. 1080. 14. 840. 15. 840. 16. 16380. 17. 1386. 18. 21000. 19. 43890. 20. 95040. Ex. XXXIV. (p. 74.) 10 14 18 24 34 51 85 6 7' (1) 7' 7, 7; 19' 7' 19' 119 153 204 19' 19' 19'  $\frac{504}{84}$ ,  $\frac{693}{84}$ , 693 570 378 6678 9891 760 84; (2)84' 84' 107' 107 14915 1045 10070 107, 107 107 Ex. XXXV. (p. 75.) 3 3 3 7 3 3 (1) 36' 48' 18' 12' 20' 24' 7 7 54' 81' 108  $\frac{16}{319}$ ,  $\frac{16}{1624}$ 16 16 16 (2)2900; 87' 145 77 77 77 4984' 8900 979' Ex. XXXVI. (p. 75.)  $\frac{65}{13}$ ;  $\frac{16}{2}$ , 39 10 45 104 (1) <u>q</u>'  $\frac{13}{13}; \frac{1}{2};$ 30 135 195 9, 2' 13  $\frac{514}{57}$ ;  $\frac{96}{8}$ ,  $\frac{120}{10}$ , 72 514 . 684 57; 90 136 170 (2)10' 296 370 2109 969 ; 10' 8' 57 Ex. XXXVII. (p. 76.) 1. 3. 2. 21. 3. 41. 4. 4. 5. 31. 6. 65. 7. 55. 8. 614. 9. 7. 10. 8. 11. 815. 12. 1833. 13.  $9_{1}^{3}_{177}$ . 14.  $102_{2}^{2}_{10}$ .

15.  $12\frac{133}{133}$ .

|       |       | E                   | x. XXXV.            | III. (p. '           | 76.)               |                             |
|-------|-------|---------------------|---------------------|----------------------|--------------------|-----------------------------|
| 1.    | 4     | 2 25                | 2 16                | A 88                 | 5 89               | e 3874                      |
|       | 3     | 12                  | 15                  | - 5                  | 0. 7               | 0                           |
| -     | 141   | 239                 | . 88716             | 3                    | 60931              | 3407                        |
| 7.    | 65    | 8                   | 9                   | 10                   | 401                | 11                          |
|       | 2970  | 0                   | 140                 | 000                  | 401                | 080                         |
| 12.   | 3370  | 13.                 | 20203               | 14. 690              | 27                 | 15. $\frac{29160}{29160}$ . |
|       | 63    |                     | 1250                | 46                   | 5                  | 2160                        |
| 16.   | 60389 | 17. 6               | 08543               |                      |                    |                             |
|       | 2400  |                     | 3084                |                      |                    |                             |
|       |       | 1                   | Ex. XXXII           | X. (p. 77            | .)                 |                             |
| 1 3   | , 2   | . 9                 | , 12                | - 35                 | . 5                | - 5945                      |
| 1.5   | - 3   |                     | <b>4</b> .55        | 16                   | 0. 6               | 6                           |
| ~ 33  | 363   | . 35                | 15                  | 1                    | 1                  | 375                         |
| 8     | 25    | 9                   | $10.\frac{10}{2}$ . | 11. $\frac{1}{26}$ . | $12. \frac{1}{11}$ | 13. 44                      |
| 0 E   | 175   | 4                   | 2 000               | 30                   | 11                 | 44                          |
| 14.   | 175   | 15. 14.             | $16. \frac{639}{2}$ | 9                    |                    |                             |
|       | 8     | 15                  | 22                  |                      |                    |                             |
|       |       |                     | Ex. XL.             | (p. 78.)             |                    |                             |
| 1.1   | 2.    | 2 3.                | 2 4 5               | 5.4                  | 6, 16              | 7.7                         |
| 2     |       | 3                   | 3 8                 | 9                    | 21                 | · · īī·                     |
| s 3   | 0     | 7 1                 | . 11                | 11 7                 | 10 13              | 10 31                       |
| 17    |       | ī3 <sup>1</sup>     | 13 .                | 11                   | 12 20              | 10                          |
|       | 3     | 35                  | - 8                 |                      | 191                | 827                         |
| 14.   | 4     | 15. $\frac{1}{114}$ | 16.                 | . 17.                | 270                | 18. 7227                    |
|       | 0.95  | 111                 |                     | 0                    | 215                | 1001                        |
| 19.   | 200   | 20                  | 21.                 | - 22                 | 940                | $23. \frac{20}{-}$          |
|       | 397   | 13                  | 3                   | 7                    | 1529               | 21                          |
| 24.   | 23    |                     |                     |                      |                    |                             |
|       | 33    |                     | TO YEAR             | ( =                  |                    |                             |
| 0     | 10    | 0                   | EX. ALI.            | (p. 79.)             | 7 95               | 99 40                       |
| 1     | , 10  | 2                   | 3                   | - 4                  | 1 30               | 5                           |
| 12    | 12    | 12 1                | 2 8                 | 8 6                  | 3 63               | 48' 48                      |
| 6. 11 | 0 81  | 7. 14               | 0 183               | 8 2712               | 3689               | o 48                        |
| 12    | 0 120 | 20                  | 0 200               | 6720                 | 6720               | . 60,                       |
| 55    | 9     | 10                  | 189 384             | 560                  |                    | 98 110                      |
| 60    | 60    | 10,                 | 1008' 100           | 8 1008               | п.                 | 210' 210'                   |
| 16    | 1     | 654                 | 5 6120 '            | 7993 445             | 5                  | 1170                        |
| 010   |       | 12. 001             | 5' 0415'            | 200 410              | F                  | 13. 1170,                   |
| 210   |       | 041                 | 0 0410              | 0410 041             | 0                  | 1200                        |

1. 105 102 130 135 84 1225 1176 800 180' 1260' 1260 180' 180' 180' 180 1260 3744 6075 4200 6000 399330 448630 16. 15. 7200' 7200' 7200' 7200' 7200' 621180 621180 319464 340170 484155 80 96 149940 17. 120' 621180' 621180' 621180' 621180 120 90 100 105 108 45 112 48 60 18. 19. 120' 120 120' 120' 120' 120' 72 63 40 220 264 165 45 - 90 20. 330' 330' 330' 330' 72' 72' 72 Ex. XLII. (p. 80.) 4 392  $3. \frac{221}{312}, \frac{228}{312}.$ 10 27 315 12 28 1. 36' 36 15' 15 504 504 5. 315, 396, 672 6, 3339 396 3528 3420 882' 882' 882 5040 5040 5040 504 8. 220, 255 252 290 7. 40 9, 16704 1239 36 168' 168' 168 300' 300' 300' 300 6336 1728 5445 103040 99 420 28 10. 63' 63' 63 6336' 6336' 6336 11.  $\frac{5}{7}$  yd. is greater by  $\frac{1}{75}$  yd. 12.  $\frac{3}{7}$  yd. is greater by  $\frac{1}{7}$  yd. 13.  $1\frac{7}{7}$  of  $1\frac{3}{7}$  of  $1\frac{3}{7}$  of  $\frac{3}{7}$  of  $\frac{3}{7}$  of a loaf is greater by  $\frac{3}{74}$  of a loaf. Ex. XLIII. (p. 82.) 2.  $1_{\overline{12}}^{5}$ . 3.  $3_{\overline{3}}^{1}$ . 4.  $1_{\overline{12}}^{7}$ . 5.  $\frac{53}{60}$ . 6.  $1_{\overline{5}}^{1}$ . 7.  $1_{\overline{55}}^{3}$ . 8. 41 9. $\frac{37}{90}$ . 10.  $2\frac{1}{2}$ . 11.  $15\frac{1}{2}$ . 12.  $9\frac{1}{12}$ . 13. 275. 14.  $5\frac{5}{72}$ . 15.  $9\frac{59}{126}$ . 16.  $22\frac{35}{27}$ . 17.  $2\frac{5}{13}$ . 18.  $2\frac{43}{66}$ . 19.  $15\frac{17}{46}$ . 20. 21,747. 21. 46383. 22. 2943. 23. 11617. 24. £11114. 25. 1346 lbs. Ex. XLIV. (p. 83.) 2.  $\frac{3}{8}$  3.  $\frac{1}{3}$  4.  $\frac{5}{72}$  5.  $1\frac{1}{2}$  6.  $4\frac{1}{10}$  7.  $1\frac{35}{36}$ 9.  $\frac{41}{100}$ , 10.  $1_{\frac{9}{140}}^{\frac{9}{140}}$ , 11.  $7_{\frac{19}{21}}^{\frac{19}{140}}$ , 12.  $12_{\frac{113}{664}}^{\frac{113}{140}}$ , 13.  $\frac{1}{2}$  of 8. 311. cake. 14. (1) $\frac{8}{9}$ . (2)  $5\frac{7}{19}$ . 15.  $\frac{5}{79}d$ .

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Ex. XLV. (p. 84.) 1.  $12_{\frac{1}{2}\frac{1}{6}}^{1}$ , 2.  $\frac{1}{c}$ , 3.  $20_{\frac{9}{17}}^{9}$ , 4.  $36_{\frac{2}{3}\frac{3}{6}}^{2}$ , 5. 1. 6.  $1\frac{15}{3\frac{9}{2}}$ , 7.  $3\frac{9}{20}$ . 8. B, C, D, and A had respectively  $\frac{1}{4}$ ,  $\frac{1}{5}$ ,  $\frac{1}{9}$ , and  $\frac{2}{9}$  of cheese. Ex. XLVI. (p. 86.)  $\mathbf{I}. \quad \frac{1}{12}. \quad 2.\frac{35}{72}. \quad 3.\frac{5}{26}. \quad 4.\frac{1}{12} \quad 5.25. \quad 6.25. \quad 7.\frac{13}{40}.$ **8.** 10. 9.  $4\frac{5}{7}$ . 10.  $329\frac{1}{10}$ . 11.  $4\frac{5}{7}$ . 12.  $6\frac{15}{10}$ . 13.  $\frac{17}{20}$ . 14. 538. 15. 73. Ex. XLVII. (p. 86.) 1.  $1_{\frac{1}{20}}$  2.  $\frac{2}{3}$  3.  $\frac{10}{11}$  4.  $\frac{116}{165}$  5.  $9\frac{4}{5}$  6.  $1\frac{3}{45}$  7.  $\frac{2}{3}$ 8.  $1\frac{44}{77}$ . 9.  $3\frac{11}{374}$ . 10.  $\frac{27}{88}$ . 11.  $\frac{1}{32}$ . 12.  $\frac{3}{8}$ . 13.  $\frac{13}{15}$ . Ex. XLVIII. (p. 87.) 1.  $1\frac{1}{1}\frac{9}{28}$  2.  $2\frac{3}{2}$  3.  $\frac{3}{8}$  4.  $1\frac{3}{4}$  5.  $1\frac{19}{21}$  6.  $\frac{23}{725}$  7.  $2\frac{1}{8}$ 8.  $\frac{76}{153}$ . 9.  $12\frac{11}{13}$ . 10.  $1\frac{397}{2465}$ . 11.  $\frac{8}{9}$ . 12.  $\frac{810}{102949}$ 13.  $\frac{25}{144}$ . 14.  $3\frac{1153}{1630}$ .

### Ex. XLIX. (p. 88.)

1. 40 cents. 2. 3 fur. 3. 1 qr., 17 lbs., 13 oz., 11<sup>2</sup> drs. 4. 19 cwt., 1 qr., 10 lbs. 5. 4 fur., 35 per. 6. 2 ac., 1 ro., 25 per., 20 yds., 4 fb., 136<sup>4</sup> in. 7. 4 lbs., 2 oz., 10 dwt. 20 grs. 8. 59 yds., 2 qrs., 1<sup>3</sup> nls. 9. £7. 4s. 3d. 10. 109 lbs., 8 oz., 5 drs. 8<sup>4</sup> grs. 11. 5 hrs., 36 min. 12. 7 lbs., 9 oz., 9<sup>2</sup> drs. 13. \$24. 14. 7 hrs. 12 min. 15. 13 cords, 64 c. ft.

|       |      | Ex. L          | (p. 88.) |       | 0     |
|-------|------|----------------|----------|-------|-------|
| 1     | 2 31 | 3 15128        | . 263    | 5 408 | 6 175 |
| 1. –. | 160  | J. <u>15</u> . | 480      | 577   | . 44  |

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| 7. $\frac{1}{45}$ .   | $8.\frac{19}{70}$ . 9. | $\frac{6}{11}$ . 10.     | $\frac{1}{27}$ . 11.  | $\frac{1}{28}$ . | 12. $\frac{144}{175}$ |
|-----------------------|------------------------|--------------------------|-----------------------|------------------|-----------------------|
| 13. $\frac{3}{224}$ . | 14. $\frac{3}{149}$    | <u>.</u> 15.             | $\frac{325}{7850601}$ |                  |                       |
|                       |                        | Ex. LI.                  | (p. 89.)              |                  |                       |
| $1.\frac{1}{2}$       | $2.\frac{1080}{241}$ . | $3. \frac{5445}{5762}$ . | 4. 357                | 5.7.             | $6.\frac{56}{3}$      |
| $7.\frac{18}{35}$     | $8.\frac{21}{2}.$      | 9. $\frac{27}{14}$       | 10. $\frac{156}{5}$   | 11               | $\frac{21625}{432}$   |
| 12. $\frac{8}{7}$ .   | 13. $\frac{351}{224}$  | . 14.                    | $\frac{115}{96}$      |                  |                       |

### Ex. LII. (p. 92.)

1. A will have  $\frac{4}{5}$  of the farm,  $B \frac{4}{15}$  of farm, and  $C \frac{3}{5}$  of farm. 2. (1) 24 boys; (2)  $7\frac{4}{5}$ . 3.  $\frac{3}{50}$  and  $\frac{1}{30}$ . 4. (1)  $1\frac{4}{247}$ ; (2)  $2\frac{24}{5}$ . 5. A has twice as much as D. 6. \$25.20. 7. \$110. 8. \$900. 9. \$36. 10.  $\pounds70$ . 11.  $385\frac{4}{57}$  rounds. 12. \$33.60. 13.  $13\frac{14}{7}$  days. 14. (1) A has \$56.70, B has \$37.80; (2) A has \$63, B has \$31.50. 15.  $\$\frac{24}{5}$ ,  $\$255.10\frac{4}{5}$ . 16.  $\frac{4}{5}$ . 17. 250 boys. 18.  $5\frac{4}{57}$  days. 19. Elder son received \$3250, younger son \$1560, and widow \$1440. 20. A has 24 ac., 3 ro.; B has 13 ac., 2 ro.; and C has 47 ac., 1 ro. 21. 48 boys. 22. 42 min. 23. (1)  $52\frac{1}{2}$  days; (2)  $\frac{1}{7}$ . 24.  $15\frac{14}{5}$  days. 25. 1st cask contains 140 gals.; 2d, 60 gals.; 3d, 45 gals.; 4th, 80 gals. 26. 20 days.

|    |                              | Ex        | . LIII.  | (p. 95. | )      |         |                |
|----|------------------------------|-----------|----------|---------|--------|---------|----------------|
| 1. | $\frac{3}{3}; \frac{13}{3};$ | 19        | 301;     | 270;    |        | 2. 5    | 04;            |
|    | 10 100                       | 100       | 1000     | 1000    |        | 10      | 000            |
|    | 73201 79                     | 1003 3    | . 45     |         | 3 300  | 18741   | 21.            |
|    | 100000' 10                   | 00000' 10 | 0' 10000 | )       | 1000   | 1000'   | 10'            |
|    | 1.5                          | 0007      | 4 347    | 702007  | 500005 | 5607468 | 305.           |
|    | 1000000' 10                  | 0000      | 1. 10    | 00000   | 1000 ' | 100000  | <b>)</b> ))))) |
|    | 500                          | 5 29      | 0050_20  | 607.50  | 0038   |         |                |
|    | 10000000                     | 10        | 0000' 10 | 000' 10 | 0000   |         |                |

Ex. LIV. (p. 96.)

1. '4; 2'3; 23'5; '04; '147; '047. 2. 500'1; 9'51; '0C9E1; 5'02; '00502. 3. 35'6; 17'00701; '0050005; '0000002;

20.76854; 0000053052. 4. 7; 030. 5. 300.003; 0001. 6. 4.000504; 0000070.

7. Six tenths; seventeen hundredths; seven hundredths.

8. Seven thousandths; seven hundred thousandths, or seven tenths; six and three thousand and four ten thousandths.

9. Thirty-five and two hundred and five hundred thousandths; four hundred and thirty-four thousand one hundred thousandths, or four hundred and thirty-four hundredths.

### Ex. LV. (p. 97.)

 1. 560·34603.
 2. 214·03691.
 3. 10061·33654.

 4. 345·608037.
 5. 40·23111.
 6. 585·07805.
 7. 7332·0773.

 8. 93·69602912.
 9. 1393·7111.
 6.
 7. 7332·0773.

#### Ex. LVI. (p. 98.)

1. 2.258. 2. 7.0456. 3. 5.9697. 4. 1.0991. 5. (1) 1.17; 204.93. (2) 68.67; .2803. (3) 72.09544; 5270.76. (4) 4.41958; .0069993. 6. 20.93. 7. .095; 19.98. 8. .613 of it left. 9.  $\frac{1257}{2}$ . 10. (1) 79.8665. (2) 82.9319.

### Ex. LVII: (p. 98.)

 1. 1·1375.
 2. 16·2945.
 3. 81·20812.
 4. 3·333715.

 5. 4246·48449.
 6. 667·81; 114·364272; 3752; 356·40164745.

 7. 01778479;
 488·745015235; 000642.
 8. (1) ·9150625.

 (2) ·3689.
 9. 278·1975 yds.
 10. 346<sup>2</sup> loaves.

#### Ex. LVIII. (p. 100.)

1.  $12\cdot36$ . 2.  $1\cdot236$ . 3. 01236. 4. 123600. 5. 123600000. 6.  $1737\cdot1$ . 7. 17371000. 8. 17371. 9. 173710000. 10.  $170\cdot01$ ; 170010. 11. 00521; 521. 12. 00003; 03; 000000003. 13.  $108971\cdot6$ ;  $1\cdot089716$ . 14. 011; 00011; 110. 15. 2040000; 204; 00204. 16. 18030; 001803. 17.  $213\cdot2$ ; 002132. 18. 0101. 19. 0008. 20. 124 tays. 21.  $85\cdot5$  times. 22. 03054.

### Ex. LIX. (p. 101.)

3

1. 6333; 63·333; 006. 2. 031; 3·105; 003. 3. 6221·584; 62215843 056; 62·215.

### Ex. LX. (p. 102.)

1. 25; 6; 1.5; 6.2; 7.8; 625; 5.3. 2. 1875; 8.9375; 95; 96875; 7.925. 3. 94; 4.056; 006; 1584; 84.0029296875. 4. 5078125; 8.75; 76.234375. 5. 3.9125; 16.36.

### Ex. LXI. (p. 104.)

1. ·6; ·1; 857142; ·583; ·73. 2. 6·037; 7·135; 100·1590;  $2 \cdot \dot{\$} 82352941176470 \dot{\$}$   $4 \cdot \frac{2}{9}; \frac{5}{99}; \frac{2}{11}; \frac{31}{198}; \frac{1}{37}; \frac{2}{7}$ 3. 11.135 : 23.01236.  $5.\frac{17}{30};\frac{368}{495};\frac{20233}{99990};$  $19\frac{11}{36}$ ;  $20\frac{7}{240}$ . 6.  $6\frac{403}{2220}$ ;  $15\frac{9}{13}$ . 7. 96.523114. 8. 37.443543. 9. 1·817686. 10. 44·494309. 11. 40·8; ·258722.....: ·01185. 12. 2·5416; ·136; ·0743; 30·833953.

### Ex. LXII. (p. 105.)

1. 75 cents. 2. \$4.371 cts. 3. 621 cts. 4. 2 qr., 12 lbs., 8 oz. 5. 3 fur. 6. 3 cwt., 2 qr. 7. £1. 3s. 54d. 8. 54d., 5 q. 9. 3 lbs., 2 oz., 2 dwt. 10. 20 ac., 3 ro., 28 po. 11. 6 ac., 1 ro., 4 po. 12. £1. 8s. 13. 17 wks., 6 days, 5 hrs., 15 min. 

 14. 16 dys., 12 hrs., 5 min., 45 6 sec.
 15. 15 lbs., 3 oz.,

 2 drs., 2 grs.
 16. £12. 3s. 8‡d. 048q.
 17. 12 ac., 2 re.,

 4 po., 20 yds., 7 ft., 122 76 in.
 18. 80 lbs., 6 oz., 13 23 grs.

 19.
 66<sup>2</sup>/<sub>3</sub> cents.
 20. 9 shillings.
 21. 4 cwt., 3 qr. 11 lb., 10 oz., 10<sup>3</sup>/<sub>3</sub> dr.
 22. £34. 3s. 4d.
 23. 5 lbs., 11 oz., 10 dwt.,
 24. 6 c. yds., 6 c. ft. 25. 18 ac., 211 ro. 26. £2166. 10s. 27. £5. 8s. 3<sup>3</sup>/<sub>4</sub>d. 28. 3 ro., 11 po., 9 yds., 1 ft., 72 in. 29. 1s. 5<sup>2</sup>/<sub>31</sub>d.

Ex. LXIII. (p. 106.)

1. ·3. 2. ·25. 3. ·14583. 4. ·81875. 5. ·5416. 6. 00022095. 7. 22083. 8. 48 083. 9. 2785493827160. 10. ·82285714. 11. ·5375. 12. ·87916. 13. 4.90. 14. ·15972.

### Ex. LXIV. (p. 107.)

#### PAPER I.

2. Seventy thousand three hundred and forty; one hundred and twenty-five millions four thousand three hundred and twenty one; five trillions six hundred and seven billions six hundred and five millions two hundred and thirteen thousand four hundred and three.

**3.** (1) 54502043294; (2) 99276. **4.** (1) 1525515655; (2)  $3875398\frac{1}{6}\frac{57}{4}$ . 5. 1372869823. 6. 777348.

#### PAPER II.

1. 3024, 3. 90 pints. 4. 56 feet; 17 times. 5. (1) 2391; (2) \$22540000. (3) \$91870.42 and \$8.06 over.

#### PAPER III.

1. (1)  $2_{1612}^{102}$ ; (2)  $2_{1625}^{67}$ , 2. \$5000. 3. (1)  $3_{75}^{7}$ ; (2)  $3_{754}^{101}$ , 4. £24. 15s. 5. 58 yards. 6.  $\frac{1}{3}$  of the orange.

#### PAPER IV.

1. 60. 2. 84.875 or  $84\frac{7}{4}$ . 3. 01236. 4.  $$416.27\frac{4}{5}$ . 5. 21 on smaller side, 24 on larger side, and 72 lookers on. 6. One side scores seven times as many runs as the other, and therefore that side wins.

#### PAPER V.

1. 12s. 6d. 2. 275s. 3.  $42_{13}^{s}$ . 4. \$19.90. 5. \$5.92. 6. \$48.27 $\frac{1}{2}$ .

# Ex. LXV. (p. 112.)

1. 27. 2.  $6\frac{3}{4}$ . 3. 15. 4.  $\frac{1}{6}$ . 5. 12.64. 6. 15. 7.  $\frac{3}{2}$ . 8. 36. 9.  $\frac{3}{4}$ . 10. 3.2.

### Ex. LXVI. (p. 115.)

1. §48. 2. §18.15, 3. §17.33 $\frac{1}{2}$ . 4. 38 bus.,  $21\frac{1}{7}$  lbs. 5. 20 bus.,  $28\frac{1}{7}$  lbs. 6. £82. 2s. Sd. 7. 28 cwt., 3 qr., 14 lbs. 12 oz. 8. 44 cents. 9. 29 cents. 10. §8126 01 $\frac{1}{79}$ . 11. 21 cwt., 3 qr., 18 lbs., 12 oz. 12. §1638  $\cdot 40\frac{5}{15}\frac{5}{35}$ . 13. 61 $\frac{1}{4}$ . 14. 2 mo. 15. 15s. 9 $\frac{3}{4}$ d. 16. £2675. 8s. 17. 3420 steps. 18. £4754. 10s. 10 $\frac{1}{2}$ d. 19. \$5606.75. 20. 20 min. 21. 26 yds. 2 ft. 22. 528 pairs. 23. 171 men. 24. 3 $\frac{1}{3}$  cts., \$\$7.812 $\frac{1}{2}$ . 25. \$4.12 $\frac{1}{2}$ . 26. 135 men. 27. 11 hrs., 38 min. 28. \$\$2234.31. 29. 7 $\frac{1}{2}$ d. 30. 12 days. 31. 5s. 6d. 32. \$151.14 $\frac{1}{14}\frac{1}{5}$ . 33. £900. 34. (1) £1000; (2) £960. 35. £8. 14s. 11 $\frac{1}{2}$ d.  $\frac{4}{7}\frac{6}{23}$ q, 36. 30 days. 37. \$1902.56 $\frac{1}{3}\frac{5}{3}$ . 38. 3s. 6d. 39. £90. 40. 104 lbs., 2 $\frac{3}{2}$  oz. 41. 11 hr., 53 $\frac{1}{3}\frac{4}{3}$ . 42.  $5\frac{1}{74}$  past 1 o'clock. 43. 35.15625 cents. 44.  $\frac{5}{3}\frac{1}{6}\frac{1}{9}$  days. 45. £4005. 46. £132.08.  $\frac{47}{9}$ d.  $\frac{47}{9}$ . 21 days. 48. 10 $\frac{1}{9}$  hrs. 49. 9 $\frac{1}{9}$  mo. 50. 12.30 P. M. 10 mi. from place. 51.  $5\frac{1}{7}\frac{57}{9}^{4}$ .

### Ex. LXVII. (p. 121.)

1. 8 wks. 2. 112 men. 3. 64 days. 4. \$307.44. 5. \$87500. 6. 174 miles. 7. \$202.50. 8. 200 horses. 9. 100 months. 10. 2808 qrs. 11. 39 ac., 1 ro. 20 po. 12. 9 mo. 13. 60 men. (cwt. = 112 lbs.) 14. 91 men. 15.  $2\frac{1}{2}$  days. 16. 45 men. 17. 178 qrs., 4 bus. 18. \$1608. 19. \$7.20. 20. 4 days. 21. 2 days. 22.  $13\frac{1}{2}$  days. 23. 3 lbs., 11 oz.,  $7\frac{5}{7}$  drs. 24. 25 horses. 25. 180 men. 26.  $2\frac{1}{7}$  ft.

### Ex. LXVIII. (p. 124.)

15. \$267911.87<sup>1</sup>/<sub>2</sub>. 16. \$715024.80. 17. \$72562.35. 18. \$9611.25. 19. £2764. 11s. 3d. 20. £14. 1s. 92d.

#### Ex. LXIX. (p. 126.)

1. \$66.50. 2. \$167. 3. \$1496.71875. 4.  $\pounds11.$  11s.  $3\frac{1}{2}d.$ 5.  $\pounds9.$  18s.  $3\frac{1}{3}d.$  6.  $\pounds350.$  13s.  $7\frac{1}{2}d.$  7. \$125468.75.8.  $\$84.06\frac{1}{2}$  9. \$173. 10. \$98.60. 11. \$477.5475.12.  $\$127.57\frac{9}{2}\frac{1}{2}4.$  13.  $\$9.61\frac{5}{4}3.$  14.  $\$15.69\frac{4}{5}0\frac{9}{2}.$ 

### Ex. LXX. (p. 128.)

1. \$17.38, \$234.63. 2. \$34.76, \$252.01. 3. \$110.74875, \$638.12375. 4. \$11.22, \$104.72. 5. \$13.25625, \$89.00625. 6. £17. 12s. 5½d. +, £80. 11s. 3d. 7. \$365.755, \$1441.505. 8. \$310.08, \$994.08. 9. £111. 14s.  $7_{7_{3}}^{s_{3}}d.$ , £7611. 14s.  $7_{7_{3}}^{s_{3}}d.$ 10. £171. 9s. 9.94...d, £5037. 1s. 2.94...d. 11. 6 years. 12. 8<sup>1</sup>/<sub>2</sub>. 13. £130. 14. £32; 5 fl., 3 c., 0.078125 m. 15. 4.

### Ex. LXXI. (p. 130.)

1. \$115.92, \$915.92. 2. \$192.70, \$934.70. 3. \$341.88, \$901.88. 4. \$28.78, \$336.78. 5. \$103.61, \$713.61. 6. \$229.25, \$1229.25. 7. (1) £1. 1s. 61/2d. 88q., (2) £6. 19s. 23d. 136q.

#### Ex. LXXII. (p. 133.)

1. \$200. 2. \$800. 3. \$1200. 4. \$209.53+. 5. \$900. 16. 5 per cent.

Ex. LXXIII. (p. 137.) 1. \$416.79+. 2.  $$780.483_{1}^{2}$ . 3. \$1524.88. 4.  $$37.15_{25}^{2}$ . 5. \$15069. 6. \$1391. 7. (1) £10. 16s. 4d.; (2) £3. 4s.  $11\frac{67}{727}d$ . 8. 6 per ct. per ann<sup>m</sup>. nearly. 9. Bank of Toronto. 10. £25. 

 10. His income less by £64. 12s. 12. \$139 $\frac{3}{23}$ .
 13. £240000

 stock.
 14. Loss of income = £45. 10s.
 15. £52. 10s.

 16. Increase of income = £135. 5s. 11 $\frac{3}{4}d$ .  $\frac{8}{95}\frac{7}{3}q$ .
 15. £52. 10s.

### Ex. LXXIV. (p. 141.)

1. \$5.37½. 2. \$250.2903. 3. 29½ cents. 4. \$1900. 5. (1) £6. 58.; (2) £18. 178. 44. 119. 6. (1) \$208; (2) \$13.13; 12

(3) §1.55. 7. (1) 10 per cent.; (2) £9. 1s.  $9\frac{3}{2}d$ .  $\frac{3}{11}q$ . 8. §1.20. 9. 663. 10. 5s. 3d. 11. 4s.  $1\frac{3}{4}d$ .  $\frac{1}{4}q$ . 12.  $40\frac{1}{2}\frac{4}{7}g$ . 13. 7s. 11 $\frac{1}{4}d$ .  $\frac{1}{4}\frac{1}{4}q$ . 14. 18s. 4d. 15. £63. 12s.  $8\frac{1}{2}d$ .  $\frac{1}{4}\frac{4}{7}q$ . 16. §1.20.

### Ex. LXXV. (p. 142.)

1. 90.83. 2. \$5.58. 3. 83.67. 4. 8.667...yrs. 5. 601 yrs. 6. 20046 813. 7. £191. 8s.

### Ex. LXXVI. (p. 145.)

1. (1) 224, 336, 448; (2) \$40.62 $\frac{1}{2}$ , \$89.37 $\frac{1}{2}$ , \$130; (3) 66 ac., 1 ro., 15 po., 79 ac., 2 ro., 18 po.; (4) £42. 17s. 1 $\frac{1}{2}d. \frac{3}{7}q.$ , £28. 11s. 5 $\frac{1}{7}d.$ , £21. 8s. 6 $\frac{3}{8}d.\frac{3}{7}q.$ , £17. 2s. 10 $\frac{1}{2}d.\frac{1}{7}q.$  2. (1) A is to have \$136, B \$238, and C \$306. (2) £136. 10s. 3. 1094 3744 lbs. of oxygen, 969 136 lbs. of carbon, 176 4896 lbs. of hydrogen, (cwt. = 112 lbs.). 4. 33 $\frac{1}{2}$  per cent. silver. 5. 5 mo. 6. 8 mo. 7. A ought to have \$6400, B \$\$40, C \$720. 8. A ought to have received £700, and B £900. 9. A should pay \$36, B \$18, and C \$6. 10. 24 men.

### Ex. LXXVII. (p. 149.)

#### Ex. LXXVIII. (p. 152.)

1. 12; 20; 18. 2. 42; 75; 92. 3. 97; 103. 4. 512; 4.01. 5. 76.3; .0587. 6. 5.079; 7420. 7.  $\frac{3}{4}$ . 8. .643. 9. 1.560. 10. 1. 11, .464. 12. .215. 13. 2.154. 14. .333.

#### Ex. LXXIX. (p. 152.)

#### PAPER I.

1. 2 rem. 117257. 2. (1) 15 tons, 8 cwt., 3 qrs., 17 lbs., 1 oz. (cwt.=112 lbs.) (2) 1 oz. Avoird.= $\frac{1}{14}$  of 1 oz. Troy. 3. £34. 9 fl. 6 c. 8·2142857 i m. 4. 1; 2520. 5. (1) 63. (2)  $\frac{5}{2}$ . (3) 4 cwt., 3 qrs., 3 lbs. (cwt.=112 lbs.) 6. (1) 21060. (2) ·00002106.

#### PAPER II.

1. (1) \$90. (2) £281. 7s. 5d. 2. Gain per cent.= \$25; Loss per cent.= \$20. 3. (1) 30502. (2) 256. (3) 67 yds., 4 in. 4. 118625. 5. 2 × 2 × 3 × 3 × 7 × 7 × 13. 6. 34'. 27 \$\*7 past 6 o'clock P. M.


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